

Metallicity - Basics

- Metallicity as [X:Y:Z]
- X = Hydrogen
- Y = Helium
- Z = „the rest“

$$X \equiv \frac{m_H}{M} \quad Y \equiv \frac{m_{He}}{M} \quad Z = \sum_{i>He} \frac{m_i}{M} = 1 - X - Y$$

Metallicity - designations

- In the literature you will find
 - [Z]
 - [Fe/H]
 - [M/H]
 - [Element 1 / Element 2]
- Relations for the transformation are necessary

$$[\text{Fe}/\text{H}] = \log_{10} \left(\frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\text{star}} - \log_{10} \left(\frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\text{sun}}$$

$$[\text{O}/\text{Fe}] = \log_{10} \left(\frac{N_{\text{O}}}{N_{\text{Fe}}} \right)_{\text{star}} - \log_{10} \left(\frac{N_{\text{O}}}{N_{\text{Fe}}} \right)_{\text{sun}}$$

$$= \left[\log_{10} \left(\frac{N_{\text{O}}}{N_{\text{H}}} \right)_{\text{star}} - \log_{10} \left(\frac{N_{\text{O}}}{N_{\text{H}}} \right)_{\text{sun}} \right] - \left[\log_{10} \left(\frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\text{star}} - \log_{10} \left(\frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{\text{sun}} \right]$$

Metallicity – designations

$$[\text{M}/\text{H}] = \log_{10} \left(\frac{N_{\text{M}}}{N_{\text{H}}} \right)_{\text{star}} - \log_{10} \left(\frac{N_{\text{M}}}{N_{\text{H}}} \right)_{\text{sun}}$$

$$\log_{10} \left(\frac{Z/X}{Z_{\text{sun}}/X_{\text{sun}}} \right) = [\text{M}/\text{H}]$$

Table 2. Transformation of $[\text{Fe}/\text{H}]$ to $[\text{Z}]$ using $[\text{Y}] = 0.23 + 2.25[\text{Z}]$ from Girardi et al. (2000) applied in this work.

| $[\text{Fe}/\text{H}]$ | $[\text{Z}]$ | $[\text{Fe}/\text{H}]$ | $[\text{Z}]$ | $[\text{Fe}/\text{H}]$ | $[\text{Z}]$ |
|------------------------|--------------|------------------------|--------------|------------------------|--------------|
| -0.729 | 0.004 | -0.030 | 0.018 | +0.253 | 0.032 |
| -0.525 | 0.006 | +0.019 | 0.020 | +0.288 | 0.034 |
| -0.387 | 0.008 | +0.077 | 0.022 | +0.312 | 0.036 |
| -0.282 | 0.010 | +0.116 | 0.024 | +0.343 | 0.038 |
| -0.224 | 0.012 | +0.152 | 0.026 | +0.371 | 0.040 |
| -0.149 | 0.014 | +0.185 | 0.028 | | |
| -0.086 | 0.016 | +0.225 | 0.030 | | |

Metallicity - designations

- [dex], e.g. $[\text{Fe}/\text{H}] = -0,5 \text{ dex}$

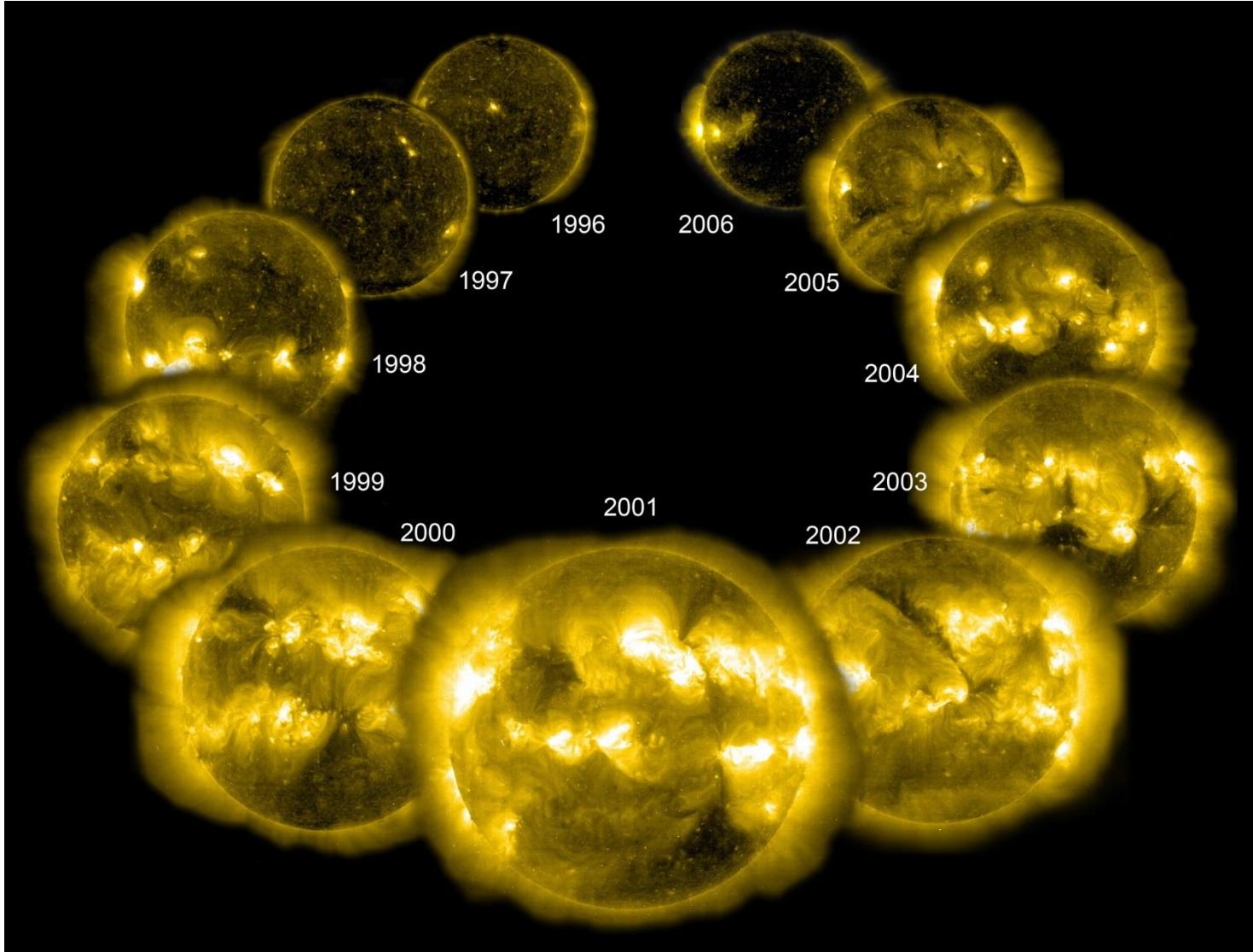
| | |
|------|--------|
| -2 | 0,01 |
| -1,5 | 0,03 |
| -1 | 0,10 |
| -0,9 | 0,13 |
| -0,8 | 0,16 |
| -0,7 | 0,20 |
| -0,6 | 0,25 |
| -0,5 | 0,32 |
| -0,4 | 0,40 |
| -0,3 | 0,50 |
| -0,2 | 0,63 |
| -0,1 | 0,79 |
| 0 | 1,00 |
| 0,1 | 1,26 |
| 0,2 | 1,58 |
| 0,3 | 2,00 |
| 0,4 | 2,51 |
| 0,5 | 3,16 |
| 0,6 | 3,98 |
| 0,7 | 5,01 |
| 0,8 | 6,31 |
| 0,9 | 7,94 |
| 1 | 10,00 |
| 1,5 | 31,62 |
| 2 | 100,00 |

The Sun as standard star

- „Our“ standard star for the normalisation of the metallicity is the Sun
- We define:
 - Mass
 - Luminosity = absolute (bolometric) magnitude
 - Temperature = spectral type = color
 - Age
 - Chemical composition
 - Internal structure (rotation, magnetic field, convection, diffusion, pulsation, ...)

Abundance analysis - Sun

- *Review article:* Asplund et al., 2009, Annual Review of Astronomy & Astrophysics, 47, 481
- Ingredients:
 - Stellar atmosphere
 - Atomic line data
 - High resolution spectra
 - Analysis method
 - Starting parameter
- Gray, 2005, The Observation and Analysis of Stellar Photospheres, Cambridge University Press

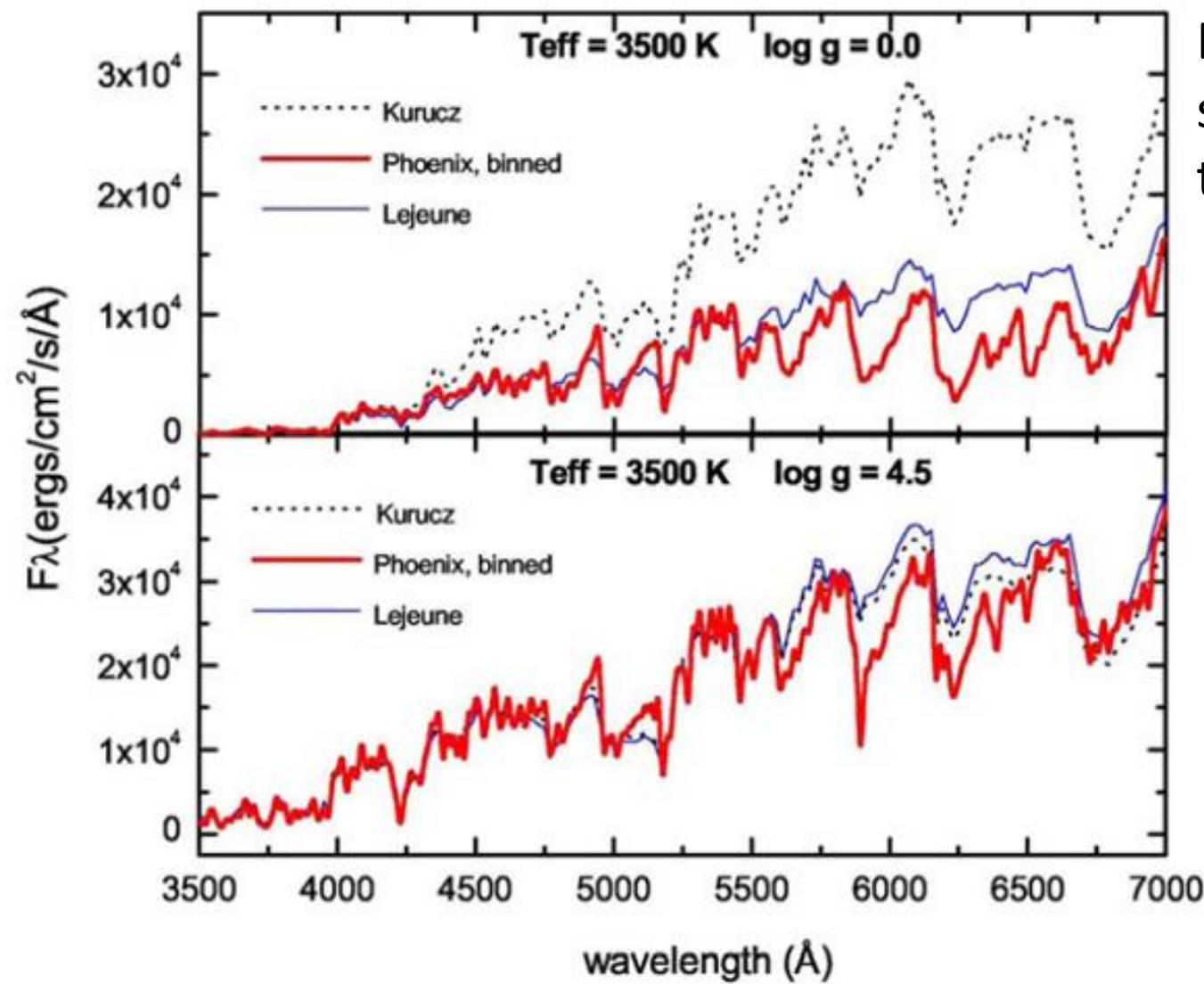


Should we care about it?

Stellar atmospheres

- **ATLAS** (<http://atmos.obspm.fr/>)
- **MARCS** (<http://marcs.astro.uu.se/>)
- **NEMO** (<http://www.univie.ac.at/nemo>)
- **PHOENIX** (<http://www.hs.uni-hamburg.de/EN/For/ThA/phoenix/index.html>)
- **TLUSTY** (<http://nova.astro.umd.edu/>)

Stellar atmospheres



Different synthesized stellar spectra “for the same star”

Abundance - Sun

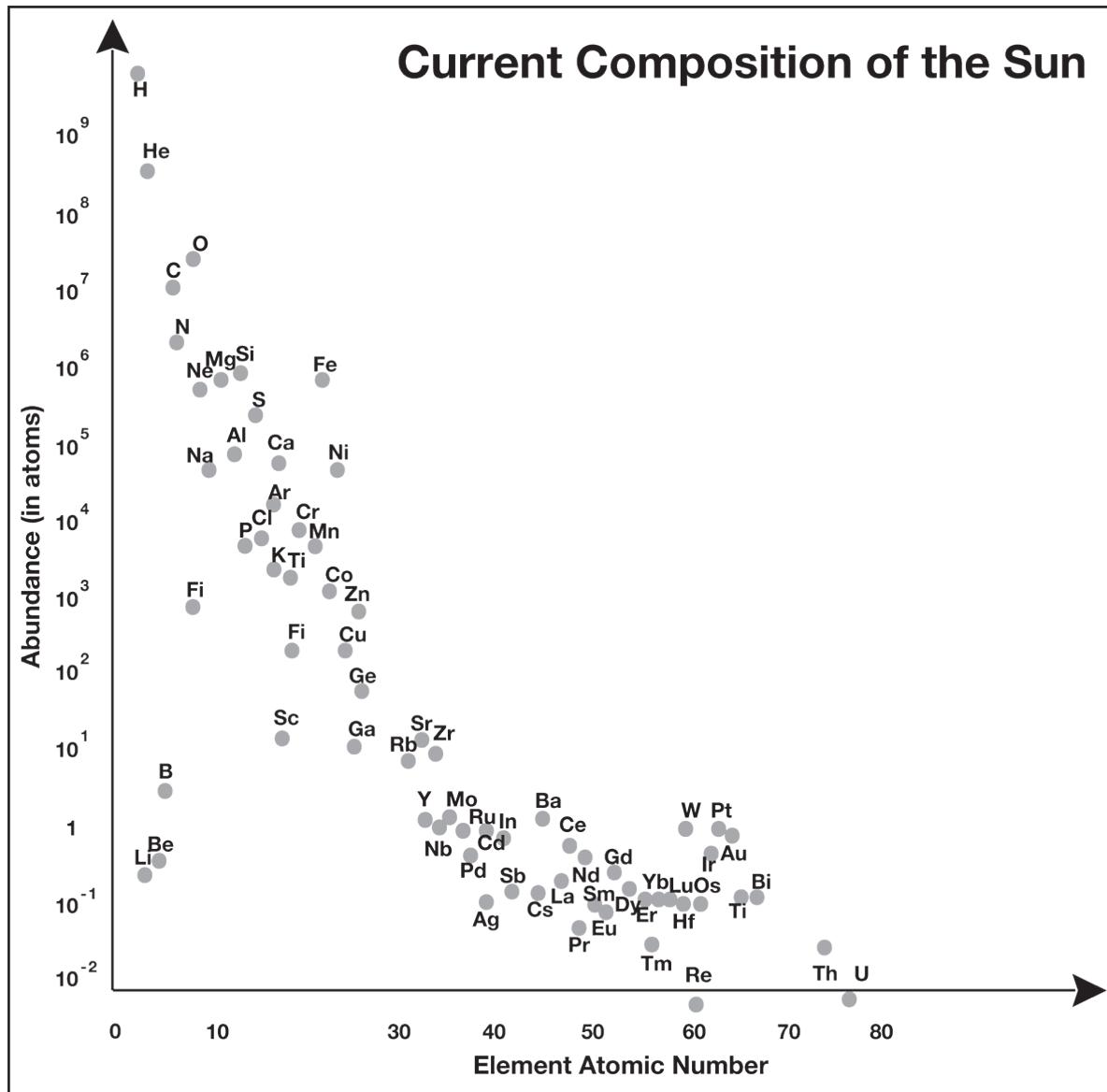
- Problems with
 - Hydrogen
 - Helium
 - Elements with only a few lines
 - Elements with only weak lines
- LTE versus NLTE (Local Thermodynamic Equilibrium)

Abundance - Sun

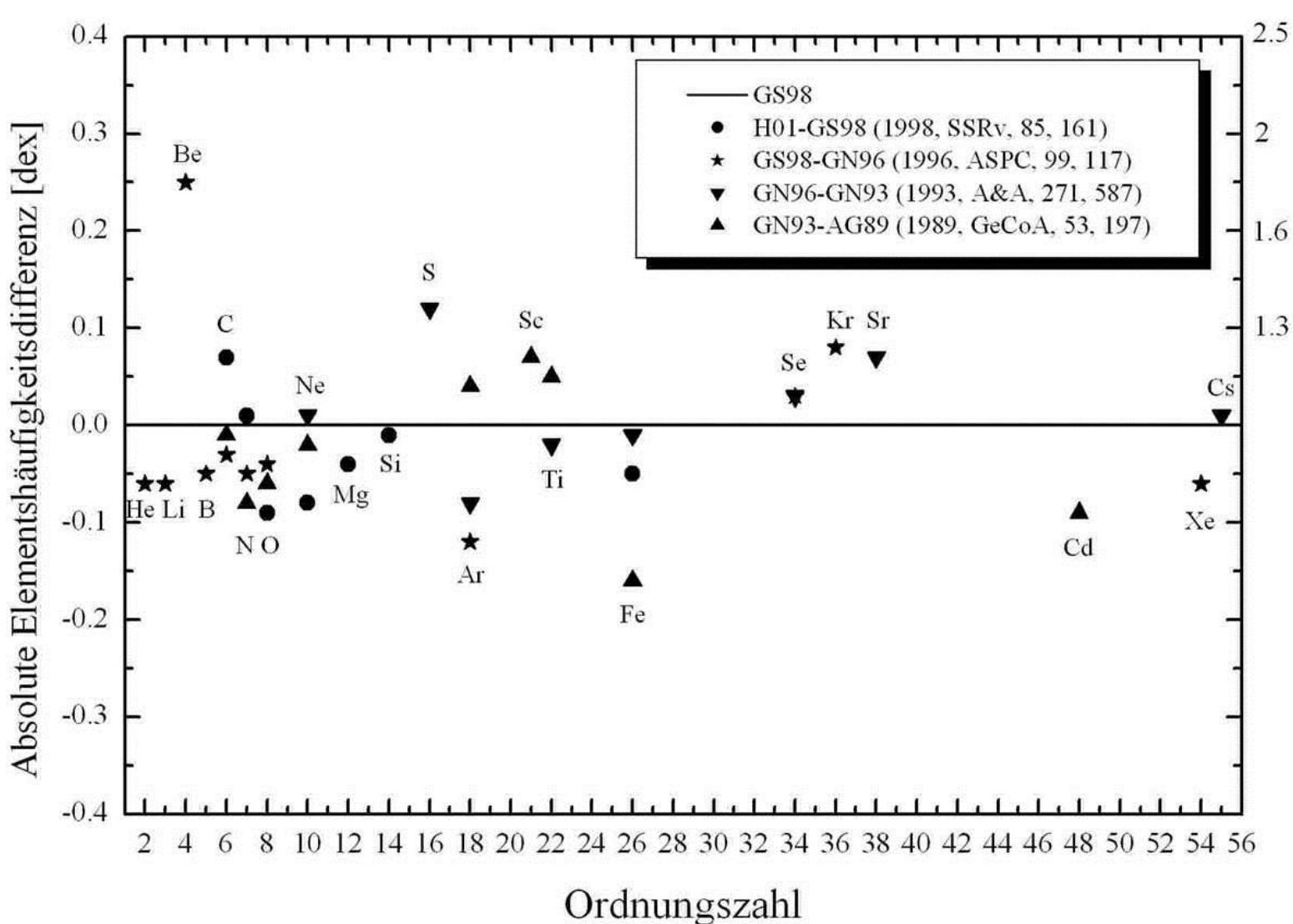
| | Elem. | Photosphere | Meteorites | | Elem. | Photosphere | Meteorites | | | | | | | | |
|----|-------|----------------------|-----------------|----|-------|---------------------|-----------------|----|----|---------------------|-----------------|----|----|-----------------|------------------|
| 1 | H | 12.00 | 8.22 ± 0.04 | 44 | Ru | 1.75 ± 0.08 | 1.76 ± 0.03 | | | | | | | | |
| 2 | He | [10.93 ± 0.01] | 1.29 | 45 | Rh | 0.91 ± 0.10 | 1.06 ± 0.04 | | | | | | | | |
| 3 | Li | 1.05 ± 0.10 | 3.26 ± 0.05 | 46 | Pd | 1.57 ± 0.10 | 1.65 ± 0.02 | | | | | | | | |
| 4 | Be | 1.38 ± 0.09 | 1.30 ± 0.03 | 47 | Ag | 0.94 ± 0.10 | 1.20 ± 0.02 | | | | | | | | |
| 5 | B | 2.70 ± 0.20 | 2.79 ± 0.04 | 48 | Cd | | 1.71 ± 0.03 | | | | | | | | |
| 6 | C | 8.43 ± 0.05 | 7.39 ± 0.04 | 49 | In | 0.80 ± 0.20 | 0.76 ± 0.03 | | | | | | | | |
| 7 | N | 7.83 ± 0.05 | 6.26 ± 0.06 | 50 | Sn | 2.04 ± 0.10 | 2.07 ± 0.06 | | | | | | | | |
| 8 | O | 8.69 ± 0.05 | 8.40 ± 0.04 | 51 | Sb | | 1.01 ± 0.06 | | | | | | | | |
| 9 | F | 4.56 ± 0.30 | 4.42 ± 0.06 | 52 | Te | | 2.18 ± 0.03 | | | | | | | | |
| 10 | Ne | [7.93 ± 0.10] | -1.12 | 53 | I | | 1.55 ± 0.08 | | | | | | | | |
| 11 | Na | 6.24 ± 0.04 | 6.27 ± 0.02 | 54 | Xe | [2.24 ± 0.06] | -1.95 | | | | | | | | |
| 12 | Mg | 7.60 ± 0.04 | 7.53 ± 0.01 | 55 | Cs | | 1.08 ± 0.02 | | | | | | | | |
| 13 | Al | 6.45 ± 0.03 | 6.43 ± 0.01 | 56 | Ba | 2.18 ± 0.09 | 2.18 ± 0.03 | | | | | | | | |
| 14 | Si | 7.51 ± 0.03 | 7.51 ± 0.01 | 57 | La | 1.10 ± 0.04 | 1.17 ± 0.02 | 23 | V | 3.93 ± 0.08 | 3.96 ± 0.02 | 67 | Ho | 0.48 ± 0.11 | 0.47 ± 0.03 |
| 15 | P | 5.41 ± 0.03 | 5.43 ± 0.04 | 58 | Ce | 1.58 ± 0.04 | 1.58 ± 0.02 | 24 | Cr | 5.64 ± 0.04 | 5.64 ± 0.01 | 68 | Er | 0.92 ± 0.05 | 0.92 ± 0.02 |
| 16 | S | 7.12 ± 0.03 | 7.15 ± 0.02 | 59 | Pr | 0.72 ± 0.04 | 0.76 ± 0.03 | 25 | Mn | 5.43 ± 0.05 | 5.48 ± 0.01 | 69 | Tm | 0.10 ± 0.04 | 0.12 ± 0.03 |
| 17 | Cl | 5.50 ± 0.30 | 5.23 ± 0.06 | 60 | Nd | 1.42 ± 0.04 | 1.45 ± 0.02 | 26 | Fe | 7.50 ± 0.04 | 7.45 ± 0.01 | 70 | Yb | 0.84 ± 0.11 | 0.92 ± 0.02 |
| 18 | Ar | [6.40 ± 0.13] | -0.50 | 62 | Sm | 0.96 ± 0.04 | 0.94 ± 0.02 | 27 | Co | 4.99 ± 0.07 | 4.87 ± 0.01 | 71 | Lu | 0.10 ± 0.09 | 0.09 ± 0.02 |
| 19 | K | 5.03 ± 0.09 | 5.08 ± 0.02 | 63 | Eu | 0.52 ± 0.04 | 0.51 ± 0.02 | 28 | Ni | 6.22 ± 0.04 | 6.20 ± 0.01 | 72 | Hf | 0.85 ± 0.04 | 0.71 ± 0.02 |
| 20 | Ca | 6.34 ± 0.04 | 6.29 ± 0.02 | 64 | Gd | 1.07 ± 0.04 | 1.05 ± 0.02 | 29 | Cu | 4.19 ± 0.04 | 4.25 ± 0.04 | 73 | Ta | | -0.12 ± 0.04 |
| 21 | Sc | 3.15 ± 0.04 | 3.05 ± 0.02 | 65 | Tb | 0.30 ± 0.10 | 0.32 ± 0.03 | 30 | Zn | 4.56 ± 0.05 | 4.63 ± 0.04 | 74 | W | 0.85 ± 0.12 | 0.65 ± 0.04 |
| 22 | Ti | 4.95 ± 0.05 | 4.91 ± 0.03 | 66 | Dy | 1.10 ± 0.04 | 1.13 ± 0.02 | 31 | Ga | 3.04 ± 0.09 | 3.08 ± 0.02 | 75 | Re | | 0.26 ± 0.04 |
| | | | | | | | | 32 | Ge | 3.65 ± 0.10 | 3.58 ± 0.04 | 76 | Os | 1.40 ± 0.08 | 1.35 ± 0.03 |
| | | | | | | | | 33 | As | | 2.30 ± 0.04 | 77 | Ir | 1.38 ± 0.07 | 1.32 ± 0.02 |
| | | | | | | | | 34 | Se | | 3.34 ± 0.03 | 78 | Pt | | 1.62 ± 0.03 |
| | | | | | | | | 35 | Br | | 2.54 ± 0.06 | 79 | Au | 0.92 ± 0.10 | 0.80 ± 0.04 |
| | | | | | | | | 36 | Kr | [3.25 ± 0.06] | -2.27 | 80 | Hg | | 1.17 ± 0.08 |
| | | | | | | | | 37 | Rb | 2.52 ± 0.10 | 2.36 ± 0.03 | 81 | Tl | 0.90 ± 0.20 | 0.77 ± 0.03 |
| | | | | | | | | 38 | Sr | 2.87 ± 0.07 | 2.88 ± 0.03 | 82 | Pb | 1.75 ± 0.10 | 2.04 ± 0.03 |
| | | | | | | | | 39 | Y | 2.21 ± 0.05 | 2.17 ± 0.04 | 83 | Bi | | 0.65 ± 0.04 |
| | | | | | | | | 40 | Zr | 2.58 ± 0.04 | 2.53 ± 0.04 | 90 | Th | 0.02 ± 0.10 | 0.06 ± 0.03 |
| | | | | | | | | 41 | Nb | 1.46 ± 0.04 | 1.41 ± 0.04 | 92 | U | | -0.54 ± 0.03 |
| | | | | | | | | 42 | Mo | 1.88 ± 0.08 | 1.94 ± 0.04 | | | | |

Asplund et al.

Abundance - Sun



Abundance - Sun



Abundance - Sun

Table 4: The mass fractions of hydrogen (X), helium (Y) and metals (Z) for a number of widely-used compilations of the solar chemical composition.

| Source | X | Y | Z | Z/X |
|---------------------------------------|--------|--------|--------|--------|
| Present-day photosphere: | | | | |
| Anders & Grevesse (1989) ^a | 0.7314 | 0.2485 | 0.0201 | 0.0274 |
| Grevesse & Noels (1993) ^a | 0.7336 | 0.2485 | 0.0179 | 0.0244 |
| Grevesse & Sauval (1998) | 0.7345 | 0.2485 | 0.0169 | 0.0231 |
| Lodders (2003) | 0.7491 | 0.2377 | 0.0133 | 0.0177 |
| Asplund, Grevesse & Sauval (2005) | 0.7392 | 0.2485 | 0.0122 | 0.0165 |
| Lodders, Palme & Gail (2009) | 0.7390 | 0.2469 | 0.0141 | 0.0191 |
| Present work | 0.7381 | 0.2485 | 0.0134 | 0.0181 |
| Proto-solar: | | | | |
| Anders & Grevesse (1989) | 0.7096 | 0.2691 | 0.0213 | 0.0301 |
| Grevesse & Noels (1993) | 0.7112 | 0.2697 | 0.0190 | 0.0268 |
| Grevesse & Sauval (1998) | 0.7120 | 0.2701 | 0.0180 | 0.0253 |
| Lodders (2003) | 0.7111 | 0.2741 | 0.0149 | 0.0210 |
| Asplund, Grevesse & Sauval (2005) | 0.7166 | 0.2704 | 0.0130 | 0.0181 |
| Lodders, Palme & Gail (2009) | 0.7112 | 0.2735 | 0.0153 | 0.0215 |
| Present work | 0.7154 | 0.2703 | 0.0142 | 0.0199 |

Table 2. Transformation of [Fe/H] to [Z] using $[Y] = 0.23 + 2.25[Z]$ from Girardi et al. (2000) applied in this work.

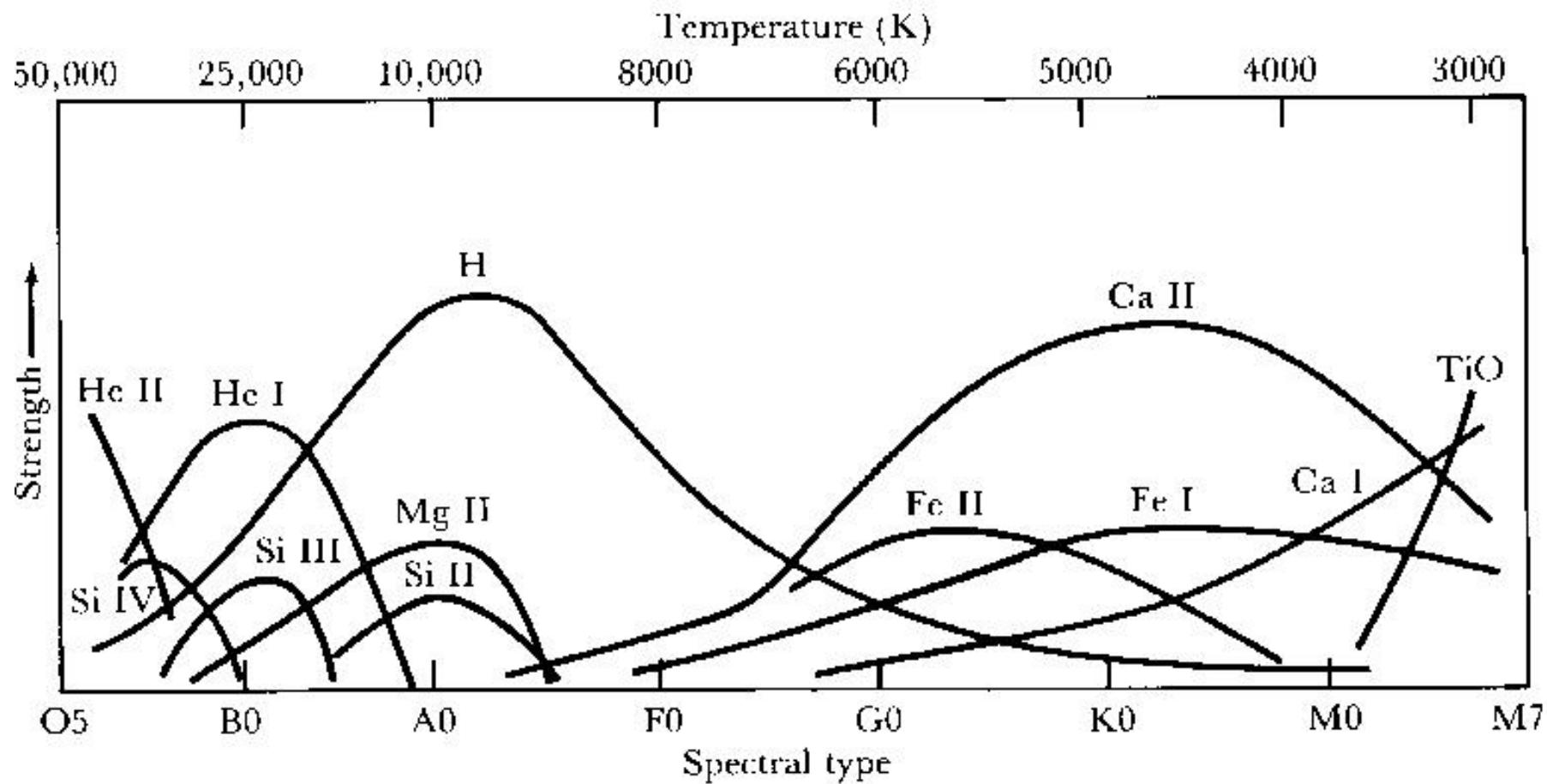
| [Fe/H] | [Z] | [Fe/H] | [Z] | [Fe/H] | [Z] |
|--------|-------|--------|-------|--------|-------|
| -0.729 | 0.004 | -0.030 | 0.018 | +0.253 | 0.032 |
| -0.525 | 0.006 | +0.019 | 0.020 | +0.288 | 0.034 |
| -0.387 | 0.008 | +0.077 | 0.022 | +0.312 | 0.036 |
| -0.282 | 0.010 | +0.116 | 0.024 | +0.343 | 0.038 |
| -0.224 | 0.012 | +0.152 | 0.026 | +0.371 | 0.040 |
| -0.149 | 0.014 | +0.185 | 0.028 | | |
| -0.086 | 0.016 | +0.225 | 0.030 | | |

^a The He abundances given in Anders & Grevesse (1989) and Grevesse & Noels (1993) have here been replaced with the current best estimate from helioseismology (Sect. 3.9).

Determination of the metallicity

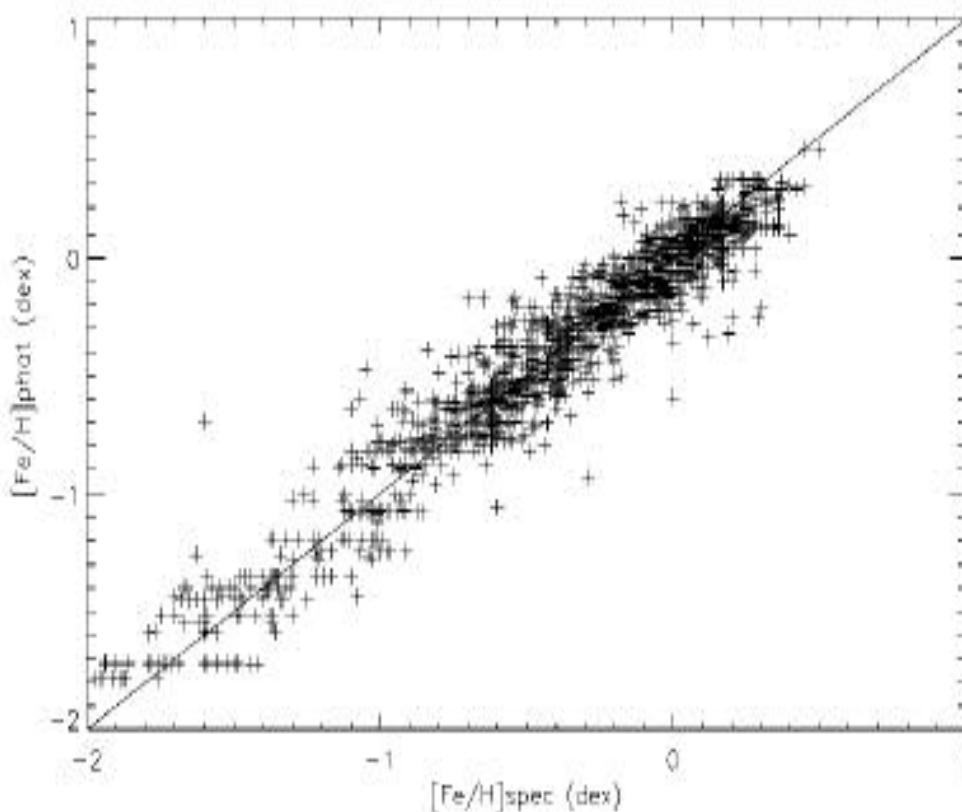
- The determination of the metallicity can be done in three ways:
 1. Spectroscopic abundance analysis
 2. Fitting of isochrones
 3. Photometric calibrations

„Metals“ in stars



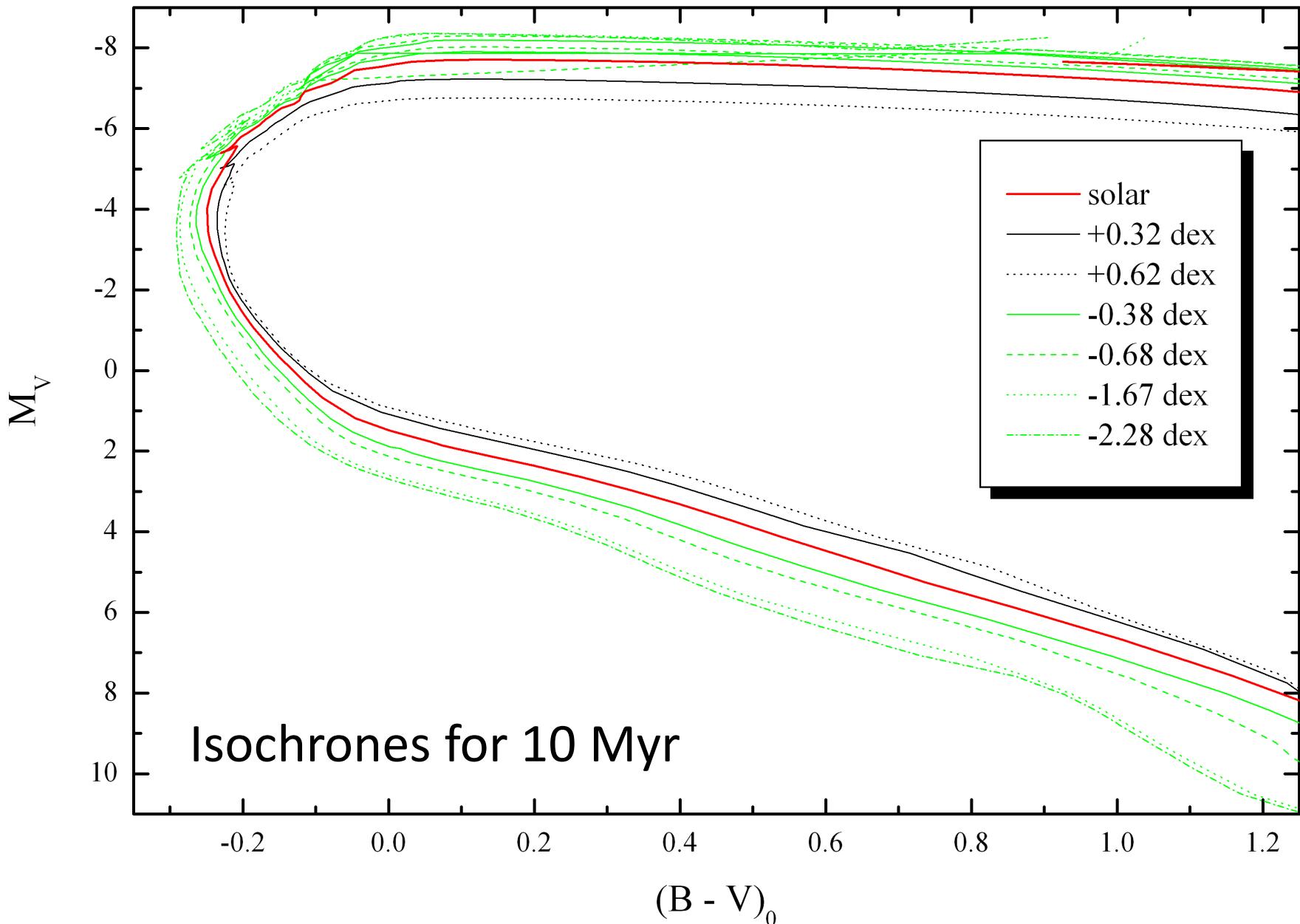
Photometric calibrations

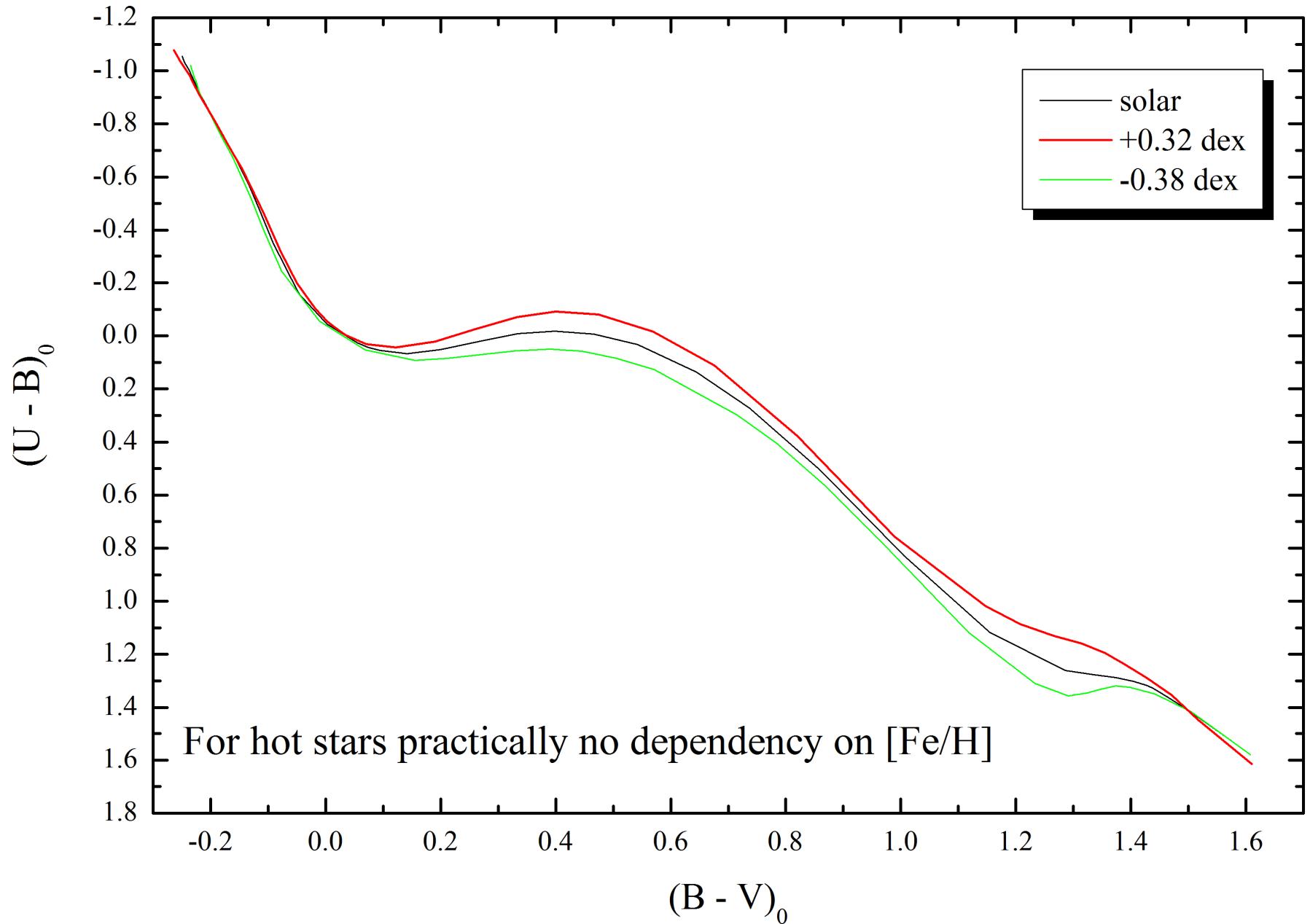
Error: +0.10 dex



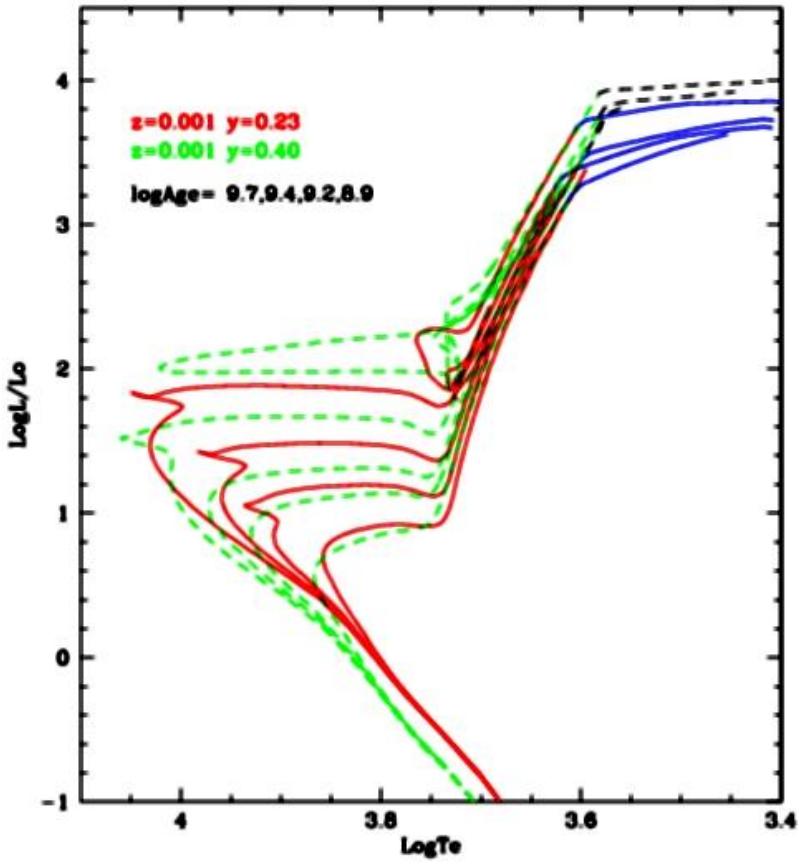
$$\begin{aligned} [\text{Fe}/\text{H}]_{\text{phot}} = & -10.424602 + 31.059003(b-y) \\ & + 42.184476m_1 + 15.351995c_1 \\ & - 11.239435(b-y)^2 - 29.218135m_1^2 \\ & - 11.457610c_1^2 - 138.92376(b-y)m_1 \\ & - 52.033290(b-y)c_1 + 11.259341m_1c_1 \\ & - 46.087731(b-y)^3 + 26.065099m_1^3 \\ & - 1.1017830c_1^3 + 138.48588(b-y)^2m_1 \\ & + 39.012001(b-y)^2c_1 \\ & + 23.225562m_1^2(b-y) - 69.146876m_1^2c_1 \\ & + 20.456093c_1^2(b-y) - 3.3302478c_1^2m_1 \\ & + 70.168761(b-y)m_1c_1 \end{aligned}$$

Metallicity => different opacity

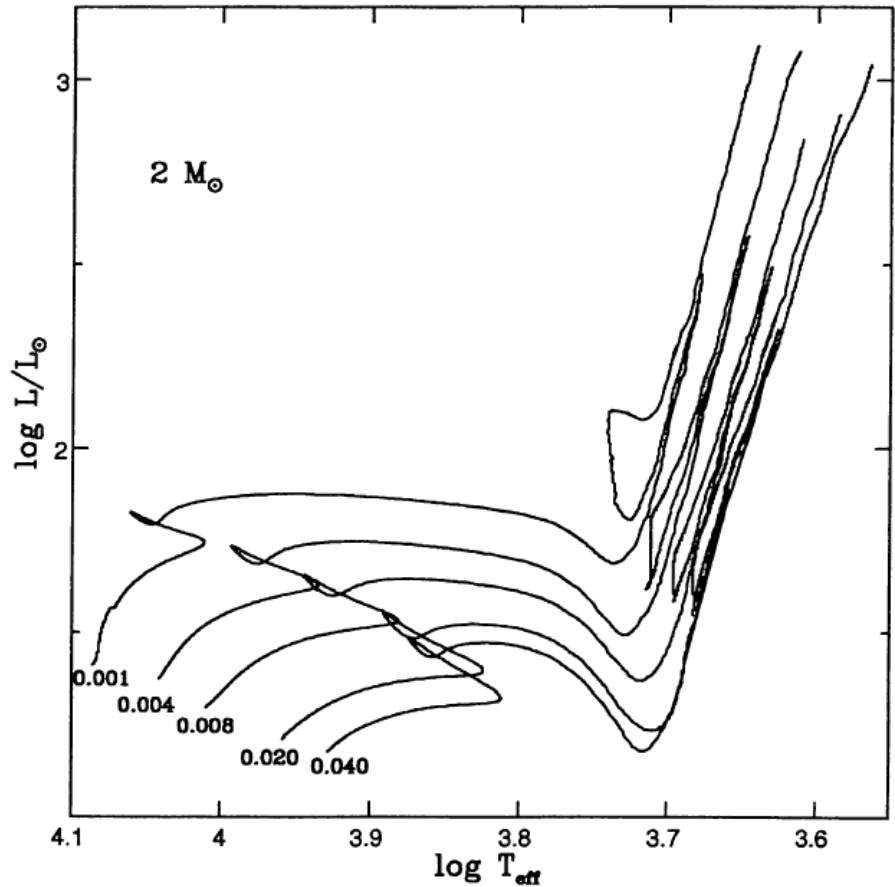




Metallicity - isochrones



Different He abundances – [Z]
constant



Schaller et al., 1993, A&AS, 101, 415