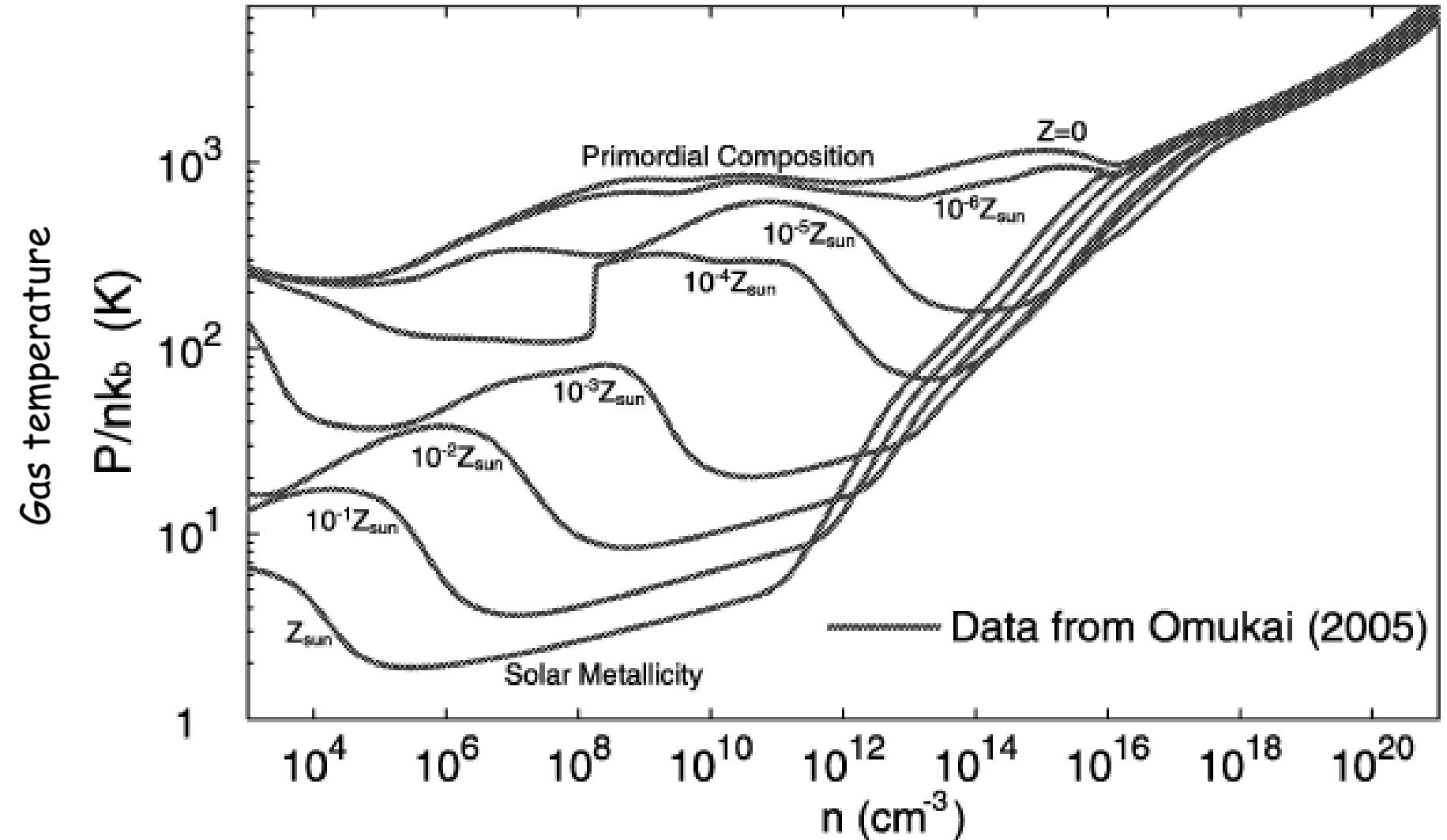
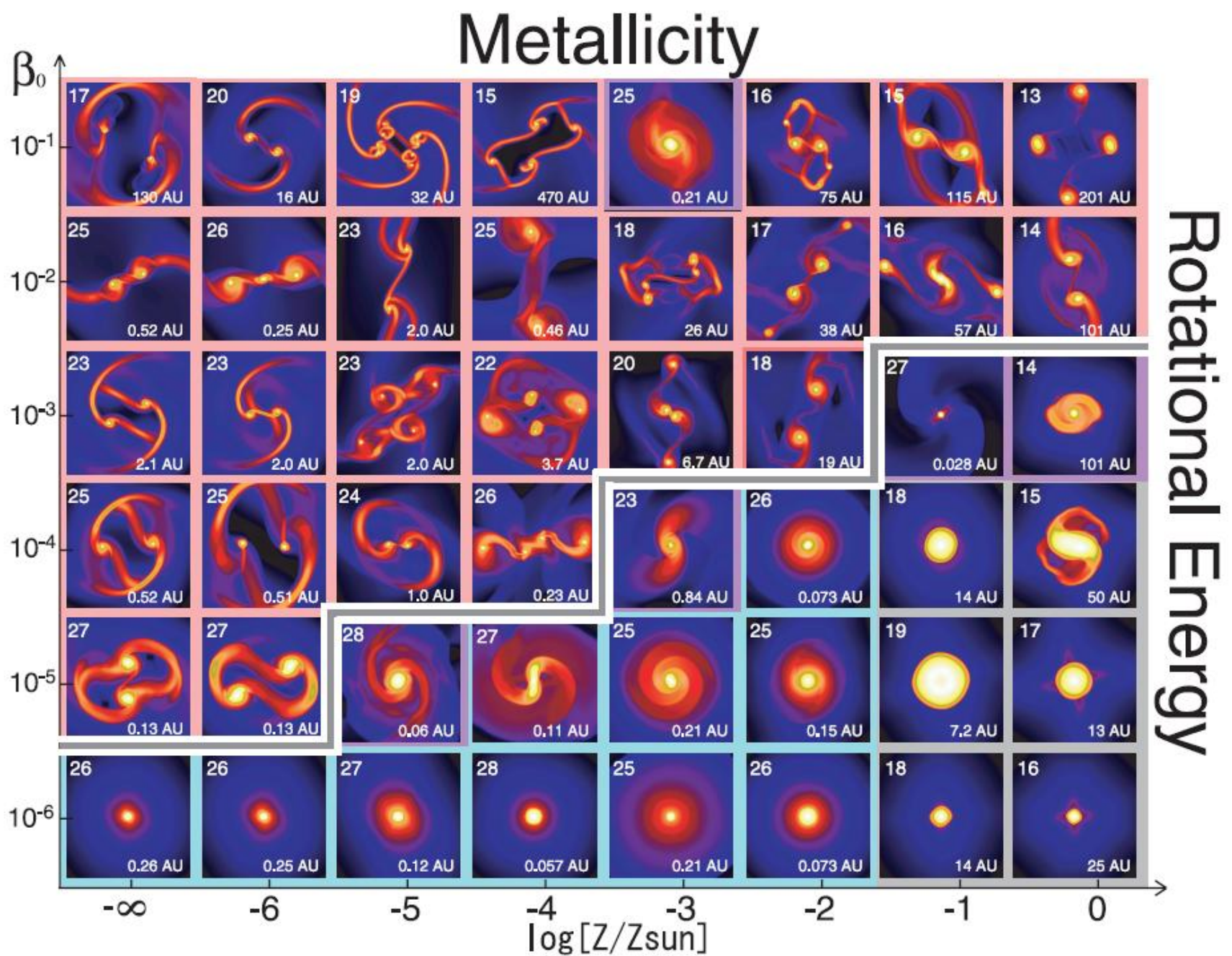


Binary fraction

- Important for the **formation** and **evolution** of star clusters
- Critical parameter for the **IMF**
- Needed for **N-body numerical simulations**
- Observations are biased in many respects
- Many different types of binary systems



Different metallicity means different opacity



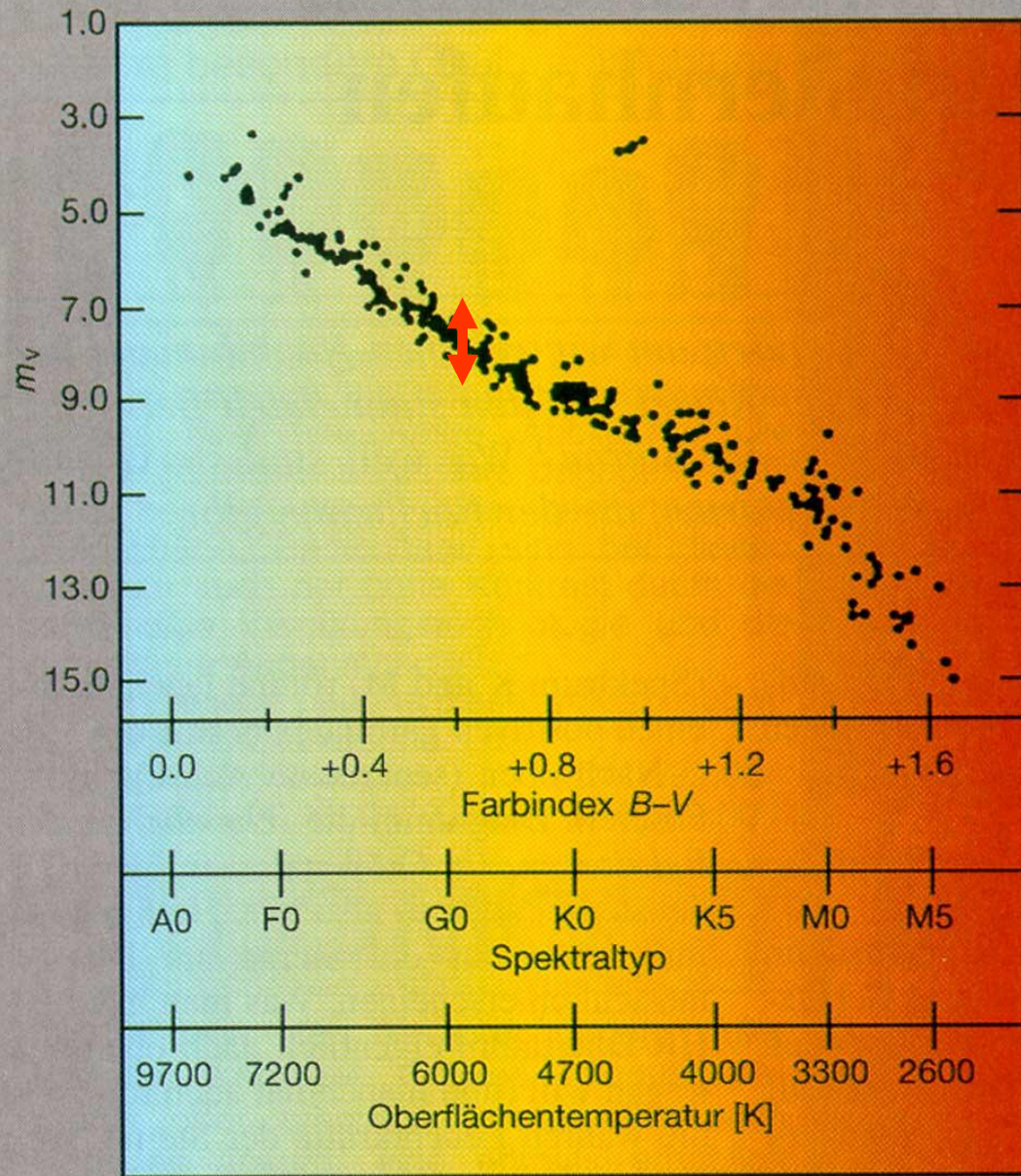
Lower metallicities seem to favour binary formation

Hyades

$\log t = 8.90$

$d = 45 \text{ pc}$

$[\text{Fe}/\text{H}] = +0.17 \text{ dex}$



↕ Width of Main Sequence
about 1.8 mag in M_V

NO
Observational error

Binary system with two components: A and B

Magnitudes in Johnson B and V: B_A , V_A , B_B , V_B , B_{AB} and V_{AB}

Colors: $C_A = B_A - V_A$, $C_B = B_B - V_B$ and $C_{AB} = B_{AB} - V_{AB}$

Basic equations for the combined colors:

$$B_{AB} - B_A = -2.5 \log (1 + 10^{-0.4(B_B - B_A)})$$

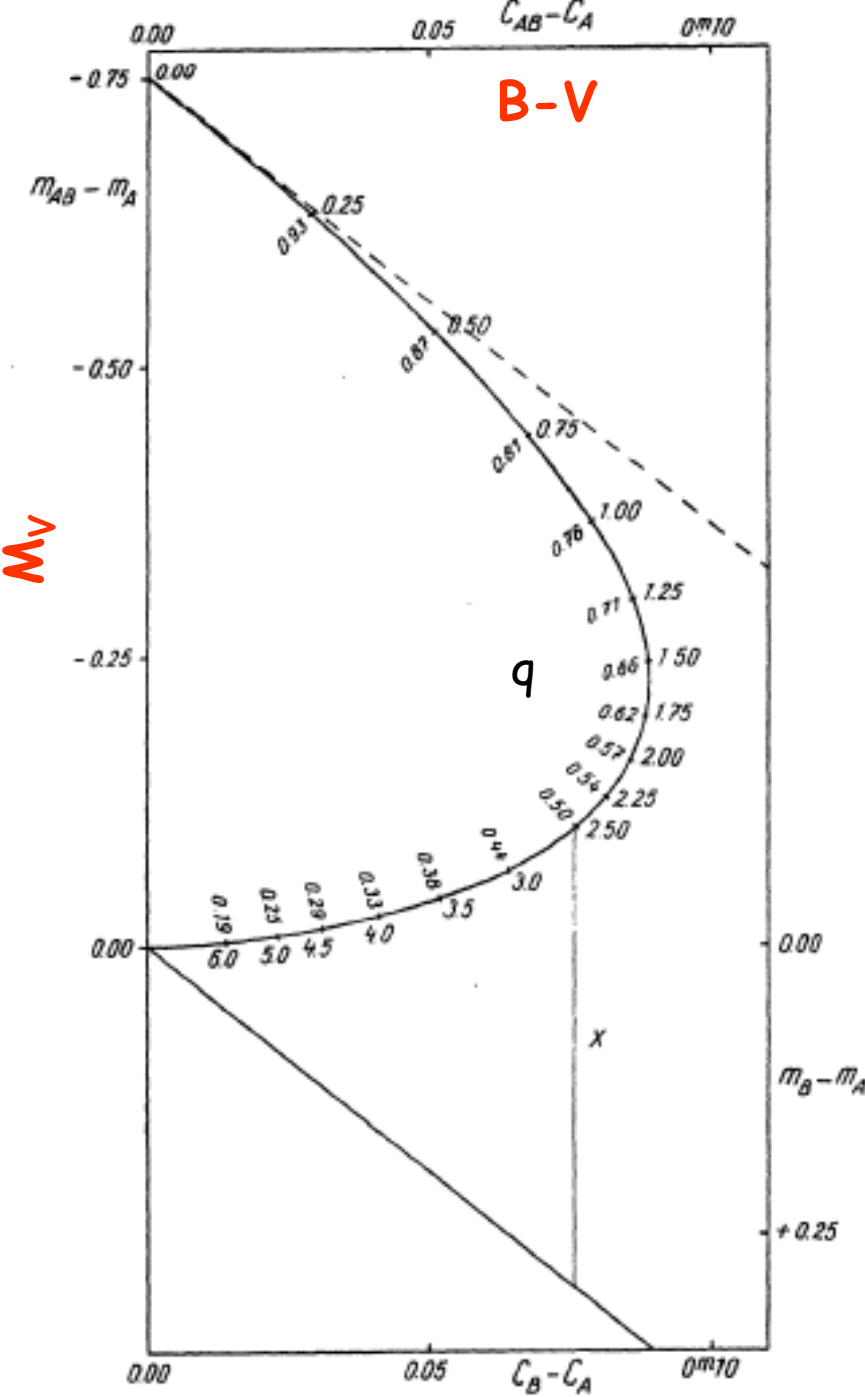
$$V_{AB} - V_A = -2.5 \log (1 + 10^{-0.4(V_B - V_A)})$$

$$C_{AB} - C_A = -2.5 \log [(1 + 10^{-0.4(B_B - B_A)}) / (1 + 10^{-0.4(V_B - V_A)})]$$

Linear correlation on the MS: $V = a C = a (B - V)$

$$V_B - V_A = [(a - 1)/a] (B_B - B_A)$$

- What do we need as input?
 1. B and V magnitudes for stars on the main sequence [known]
 2. Magnitude - Color function [known]
 3. Luminosity - Mass function, for example: $L \sim M^3$
 4. Membership probabilities
 5. Reddening free observations



Vertical distance from the main sequence

$$x = a(C_{AB} - C_A) + V_A - V_{AB}$$

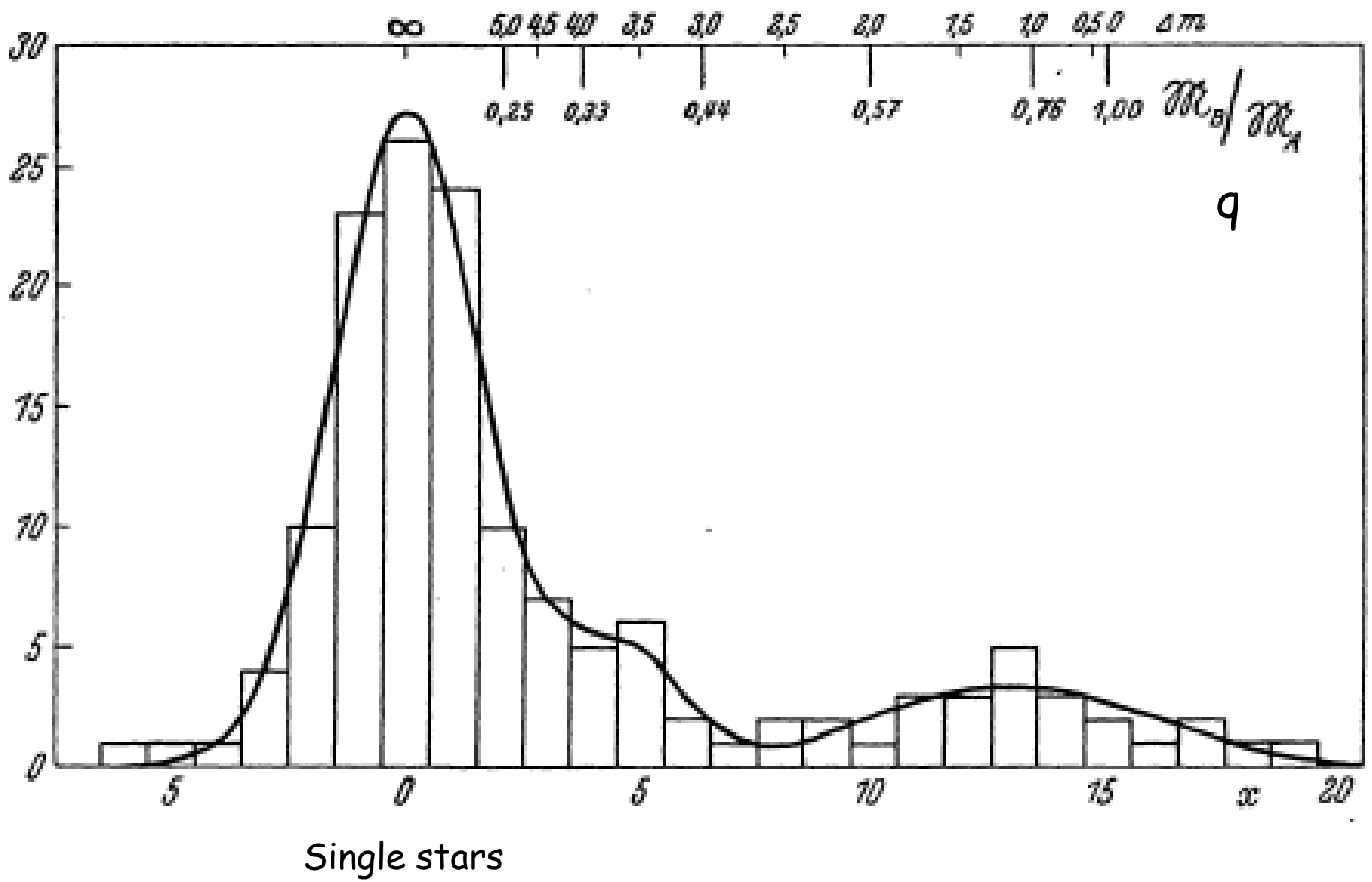
Absolute magnitude:

$$M_V = -2.5 \log (L_1 + L_2)$$

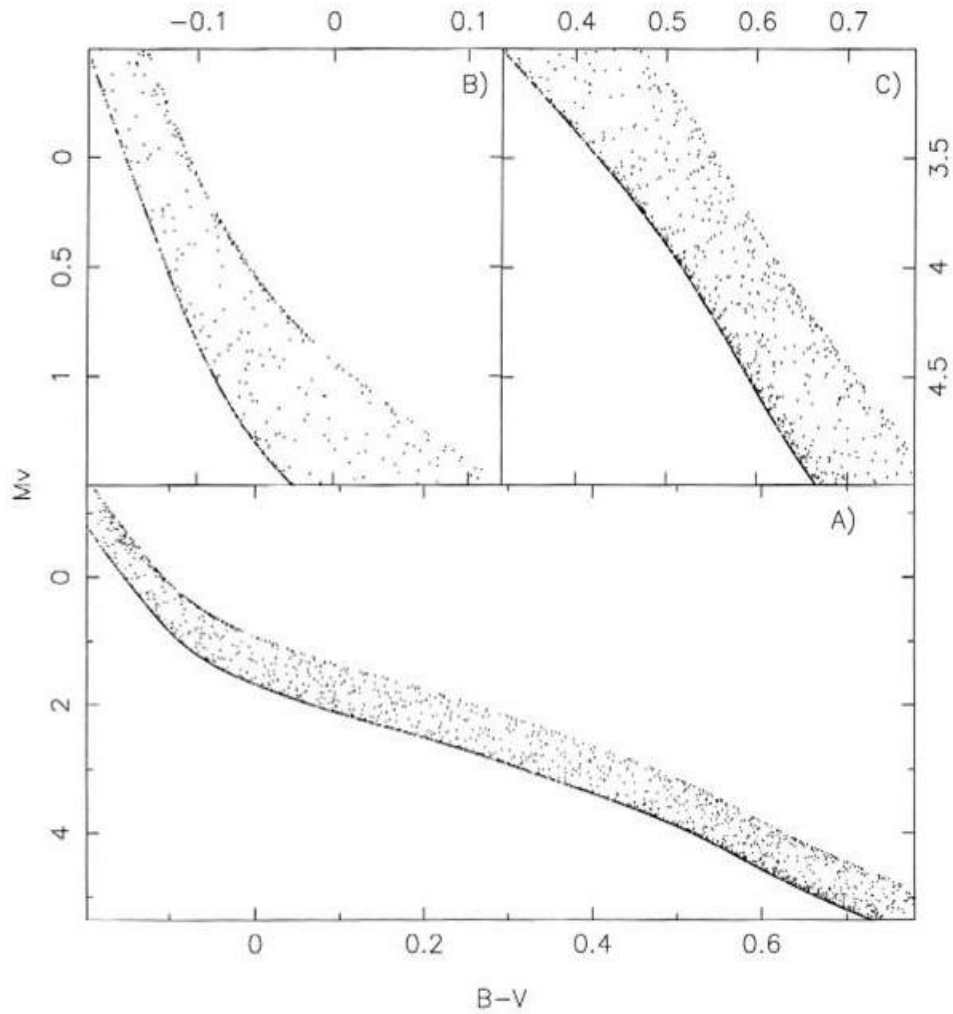
Maximum at $L_1 = L_2 \Rightarrow$

$$M_V = -0.753 \text{ mag}$$

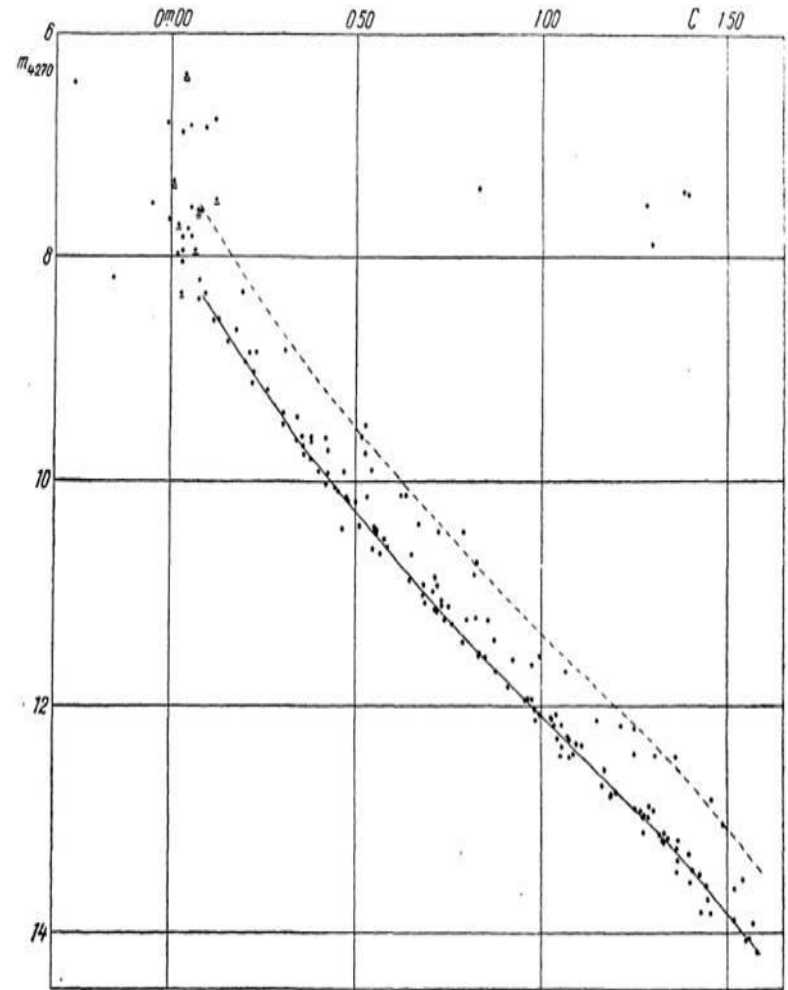
The maximal width of the main sequence due to binary systems is 0.753 mag



Determination of q = Mass ratio of binaries



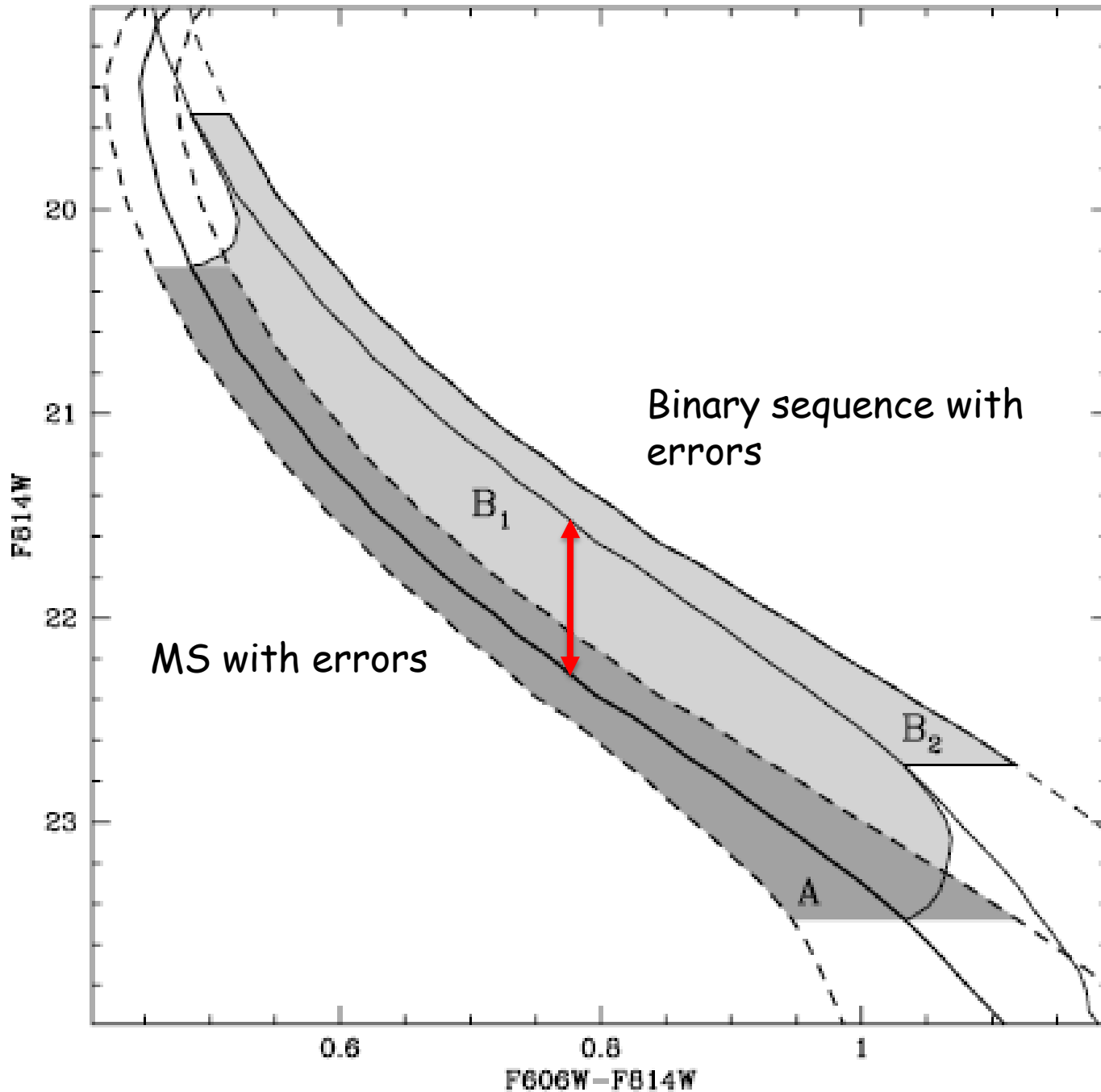
Simulation with randomly distributed mass ratios



Observations of Praesepe with known binary systems

How to observe the binary fraction?

- Photometric observations of star clusters
 1. "Cluster main sequence"
 2. Eclipsing binaries
 3. Positions (astrometric binaries)
- Spectroscopic observations
 1. Radial velocity variability
 2. Direct detection in spectrum (SB2)



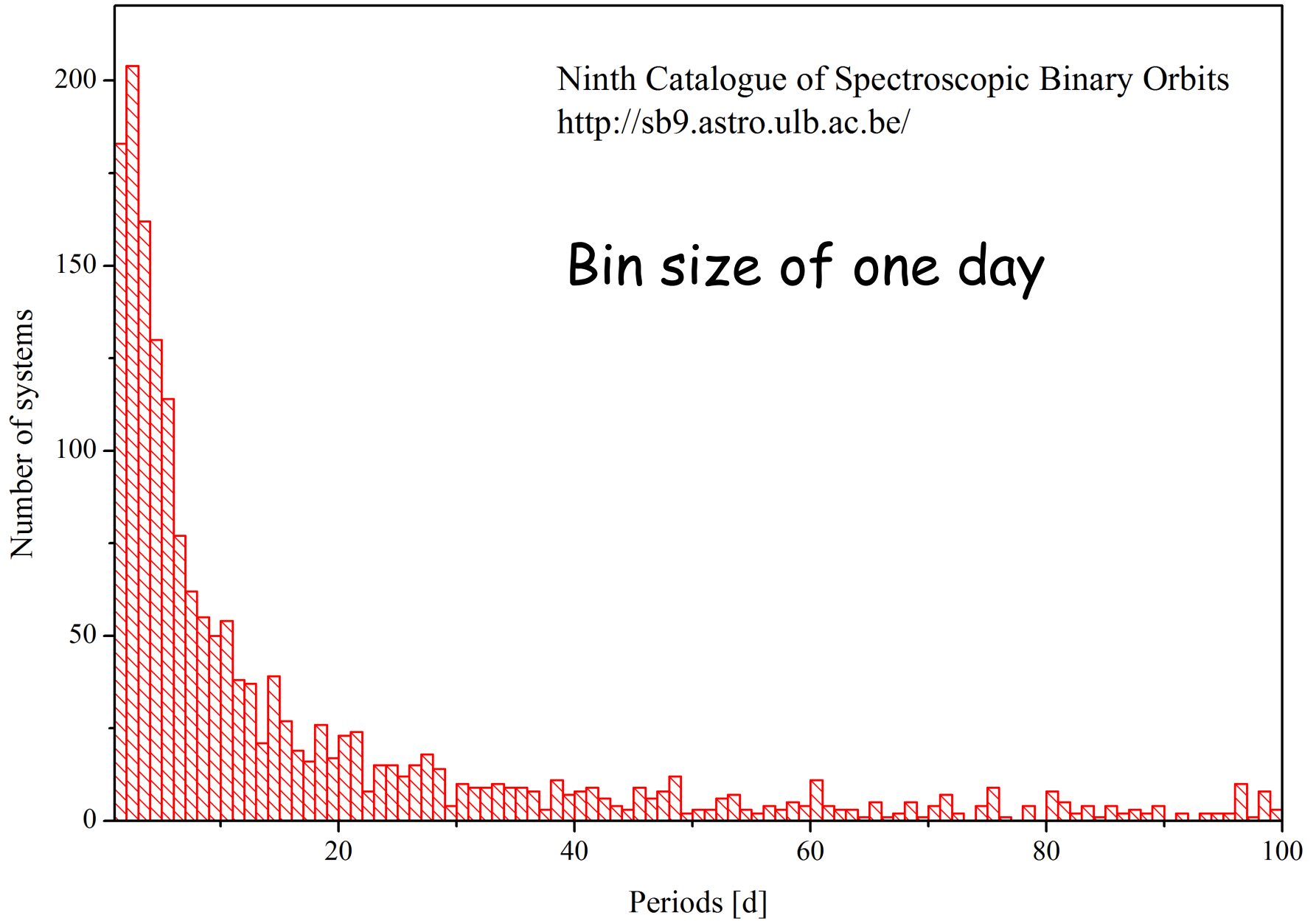
Sollima et al.,
2007, MNRAS,
380, 781

HST photometry
of Globular
Clusters

Count in the
areas and do
proper statistics

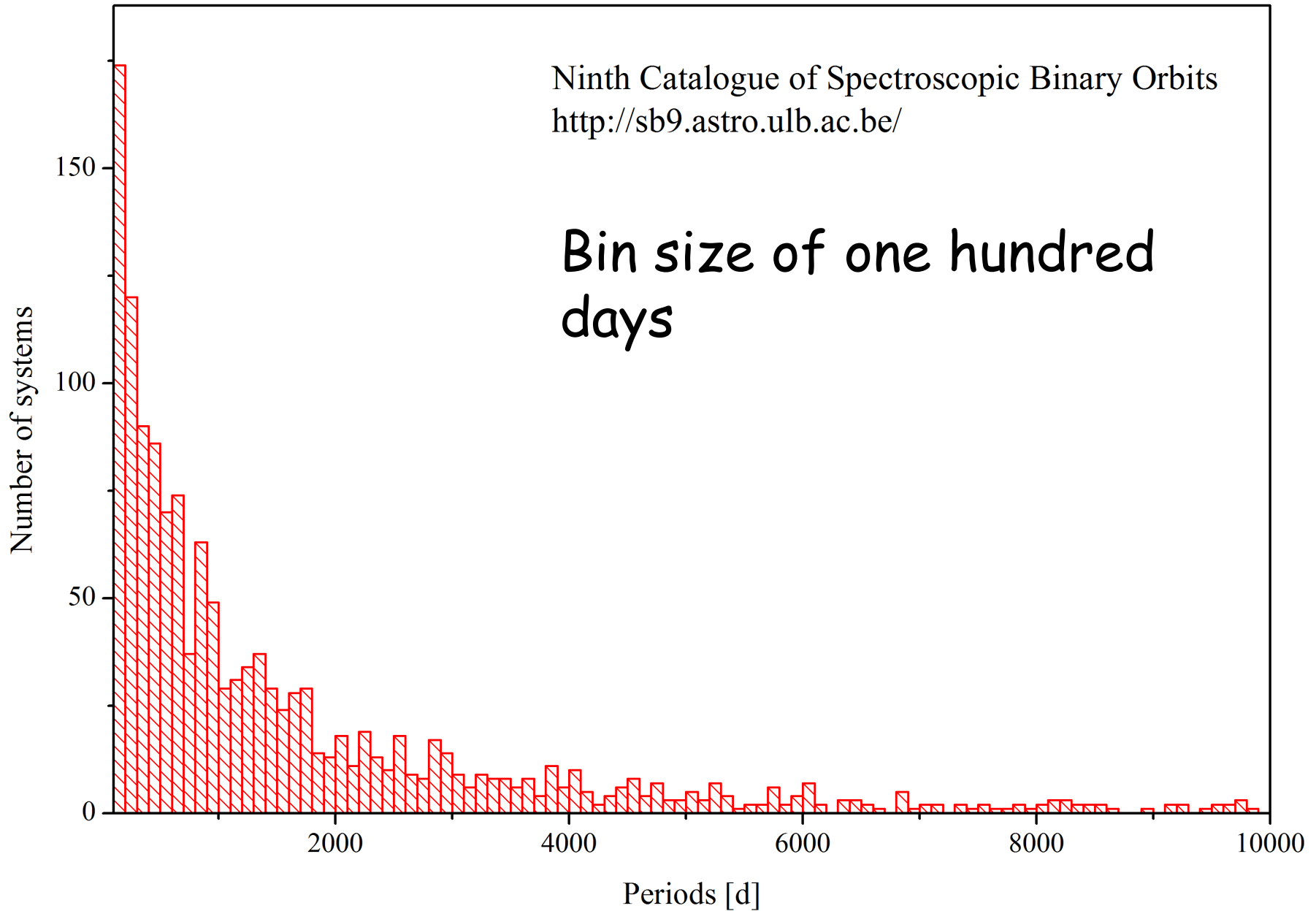
Ninth Catalogue of Spectroscopic Binary Orbits
<http://sb9.astro.ulb.ac.be/>

Bin size of one day



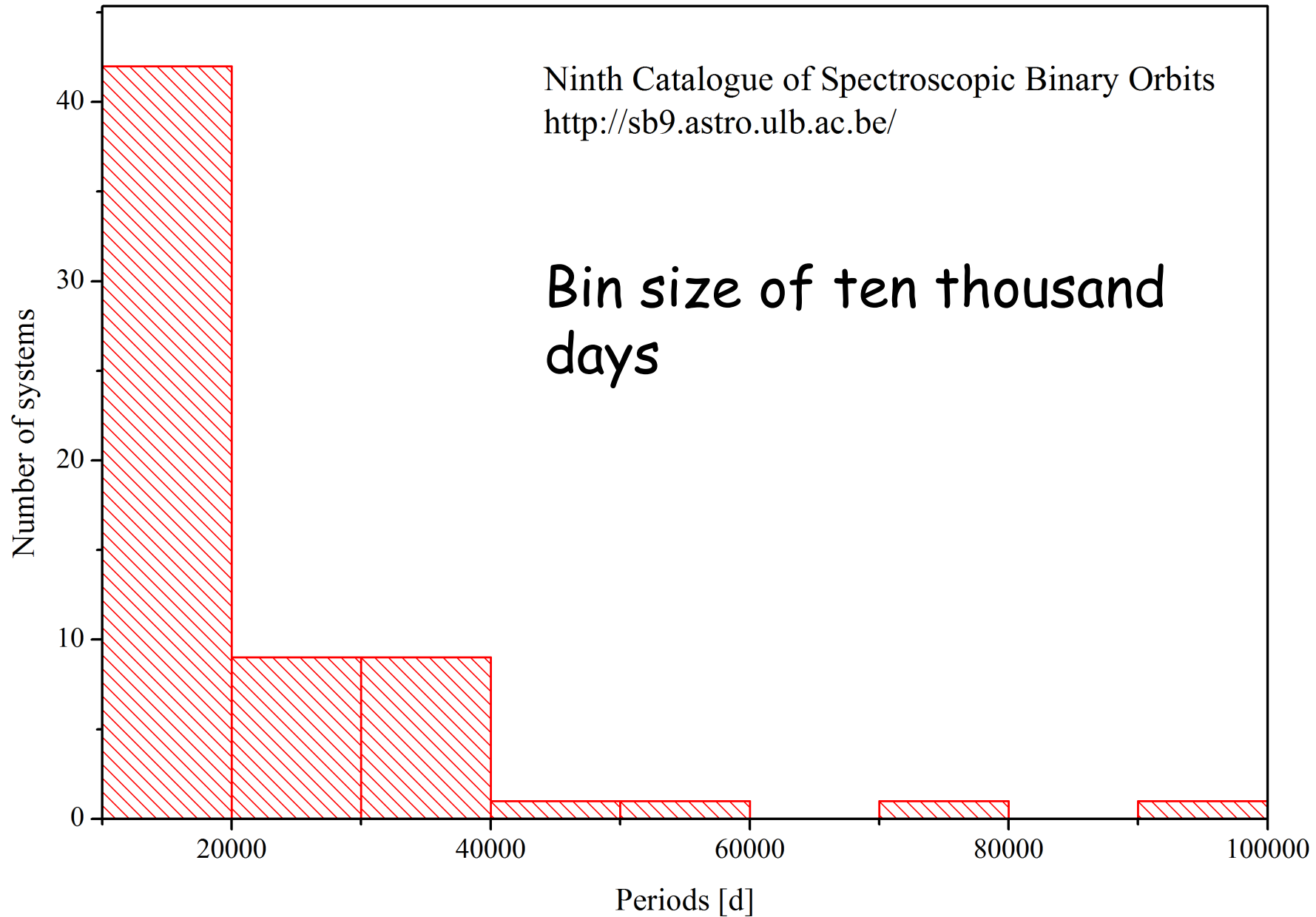
Ninth Catalogue of Spectroscopic Binary Orbits
<http://sb9.astro.ulb.ac.be/>

Bin size of one hundred
days



Ninth Catalogue of Spectroscopic Binary Orbits
<http://sb9.astro.ulb.ac.be/>

Bin size of ten thousand
days



Results for open clusters

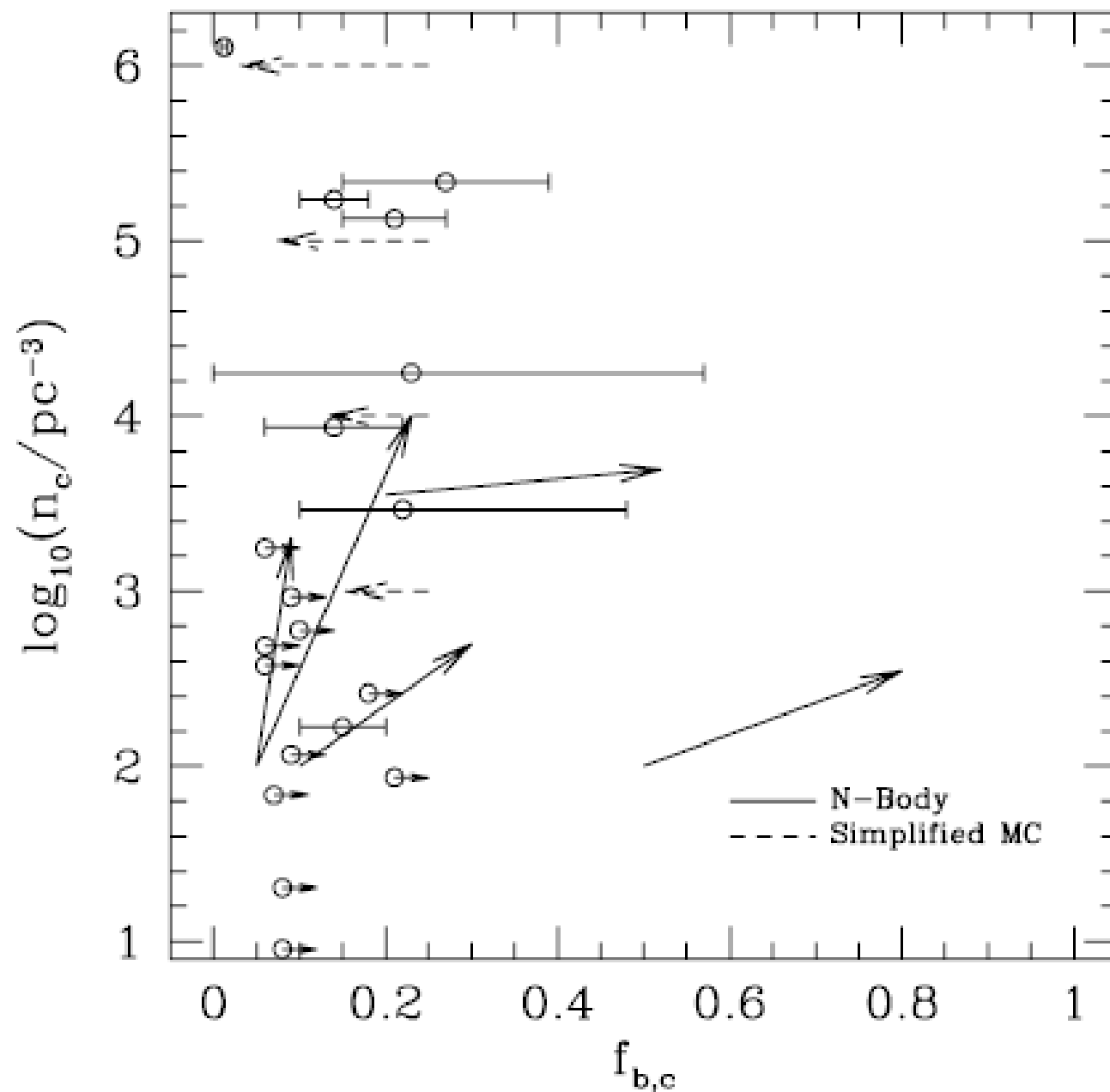
- Sollima et al., 2010, MNRAS, 401, 577
 - NGC 188 (9.63): 21 - 58%
 - NGC 2204 (9.20): 12 - 36%
 - NGC 2243 (9.58): 34 - 70%
 - NGC 2420 (9.08): 17 - 51%
 - NGC 2516 (8.52): 25 - 66%
- Sana et al., 2009, MNRAS, 400, 1479
 - NGC 6611 (6.50): 44 - 67%
- Sana et al., 2008, MNRAS, 386, 447
 - NGC 6231 (6.50): 63% - ?
- Bica & Bonatto, 2005, A&A, 431, 943
 - IC 4651 (9.26): 50 +- 11%
 - NGC 2287 (8.20): 48 +- 45%
 - NGC 2447 (8.60): 21 +- 9%
 - NGC 2548 (8.56): 48 +- 23%
 - NGC 2682 (9.51): 39 +- 16%
 - NGC 3680 (9.20): 25 +- 5%
 - NGC 5822 (9.00): 16 +- 8%
 - NGC 6208 (9.11): 54 +- 30%
 - NGC 6694 (7.85): 18 +- 12%
- Sandhu et al., 2003, A&A, 408, 515
 - NGC 2099 (8.60): ~30%
 - King 5 (9.00): ~30%
 - King 7 (8.80): ~20%

Fregeau et al., 2007,
ApJ, 707, 1503

Start at 4 Gyr with
50% binary fraction

Destruction due to

- Stellar evolution
- Dissipation
- Collisions in the core



	f		
NGC 288	0.15 ± 0.05	M3	
	>0.06		
NGC 362	0.21 ± 0.06		0.14 ± 0.08
NGC 2808		M4	$0.23^{+0.34}_{-0.23}$
NGC 3201		M15	~ 0.07
NGC 4590	>0.09	M22	
NGC 5053	>0.08	M30	
NGC 5466	>0.08	M55	>0.06
NGC 5897	>0.07	M71	$0.22^{+0.26}_{-0.12}$
NGC 6101	>0.09	M92	
NGC 6362	>0.06	Arp 2	>0.08
NGC 6397	<0.07	Terzan 7	>0.21
NGC 6723	>0.06	Palmoar 12	>0.18
NGC 6752	0.27 ± 0.12	Palmoar 13	0.30 ± 0.04
NGC 6792		47 Tucane	0.14 ± 0.04
NGC 6981	>0.10		

Designation of open clusters

- IAU:
 - $C aa bb \pm ccd$
 - $aa^h bb^m \pm cc^o.d$, Coordinates (1950.0)
- Catalogues:
 - IC, M(essier), NGC, and OCL
- „Discoverer“, surveys and „special names“
 - Basel, Bochum, Lynga, Melotte, Stock, Trumpler and much more
- Pleiades: C 0344+239, M45, Melotte 22

Classification of open clusters

- Trumpler, 1930, Lick Observatory Bulletin, 420, 154, **three criteria**
 1. Degree of Concentration
 2. Range of Brightness
 3. Number of Stars in the Cluster
- Janes & Adler, 1982, ApJS, 49, 425: definition of a so-called **richness class**
- Open clusters can also be classified on the basis of color-magnitude diagrams

Trumplers classification

- **Degree of Concentration**
 - **I** ... Detached clusters with strong central concentration
 - **II** ... Detached clusters with little central concentration
 - **III** ... Detached cluster with no noticeable concentration
 - **IV** ... Clusters not well detached, but has a strong field concentration

Trumplers classification

- **Range of Brightness**
 - **1** ... Most of the cluster stars are nearly the same apparent brightness
 - **2** ... A medium range of brightness between the stars in the cluster
 - **3** ... Cluster is composed of bright and faint stars

Trumplers classification

- **Number of Stars in the Cluster**
 - **p** ... Poor clusters with less than 50 stars
 - **m** ... Medium rich cluster with 50 to 100 stars
 - **r** ... Rich clusters with over 100 stars
- Open clusters with any type of nebulosity are denoted with an "n" at the end of the classification.



I

II

III

IV

r

m

p

NGC 6791

NGC 7789

NGC 6940

NGC 1817

NGC 436

NGC 7790

NGC 129

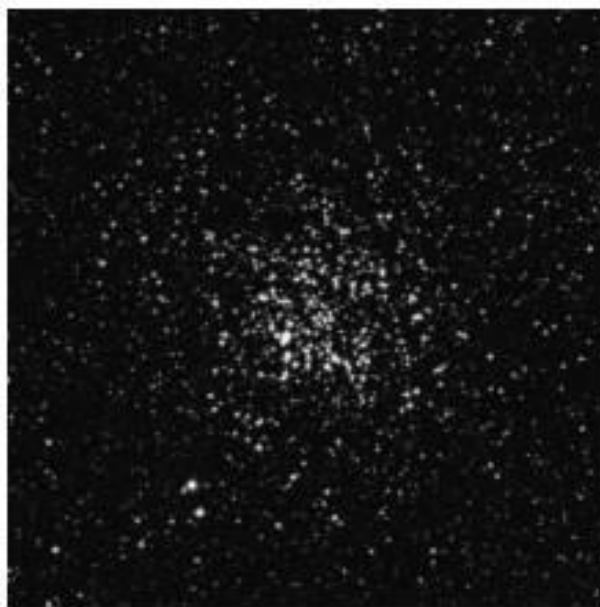
DoDz 9

NGC 7788

NGC 1807

NGC 7686

Stock 12



M11 15.0'
Class: I 2 r



M46 15.0'
Class: II 2 r



NGC 6664 15.0'
Class: III 2 m



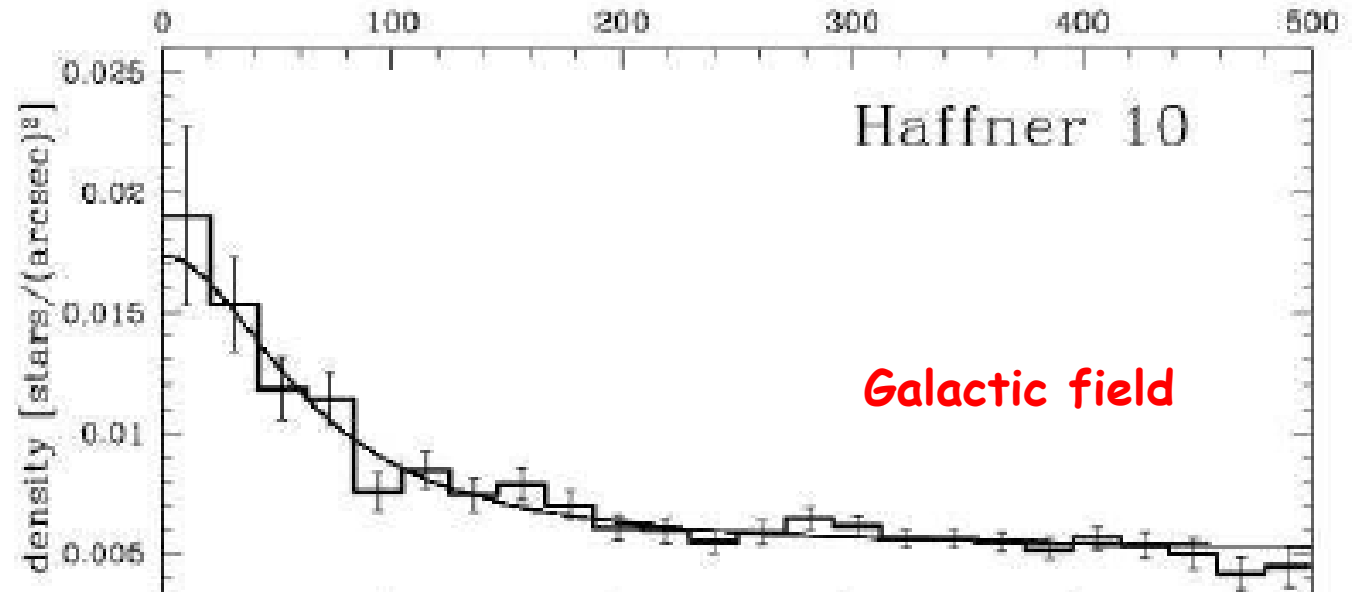
NGC 6568 25.0'
Class: IV 1 m

- **Richness Class**
 - **1** ... Less than 25 stars
 - **2** ... Between 25 and 50 stars
 - **3** ... Between 50 and 100 stars
 - **4** ... Between 100 and 250 stars
 - **5** ... More than 250 stars
- How "good" can the number of members be established?

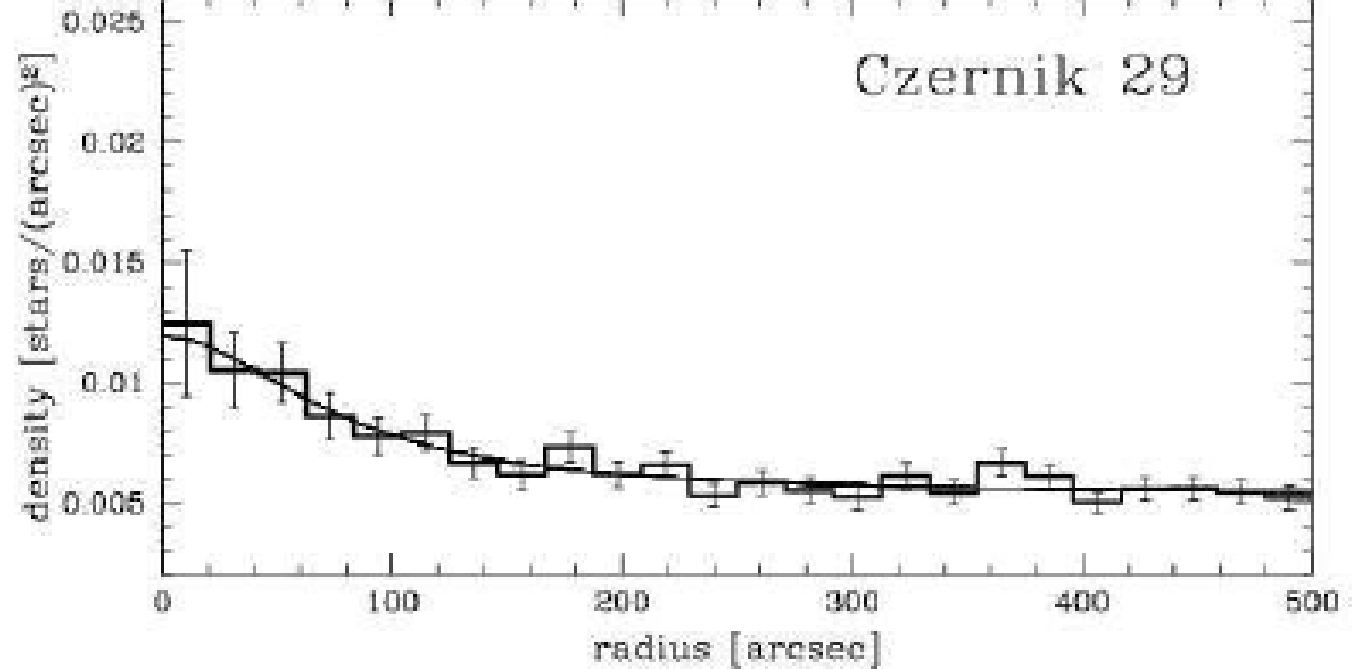
Diameters of open clusters

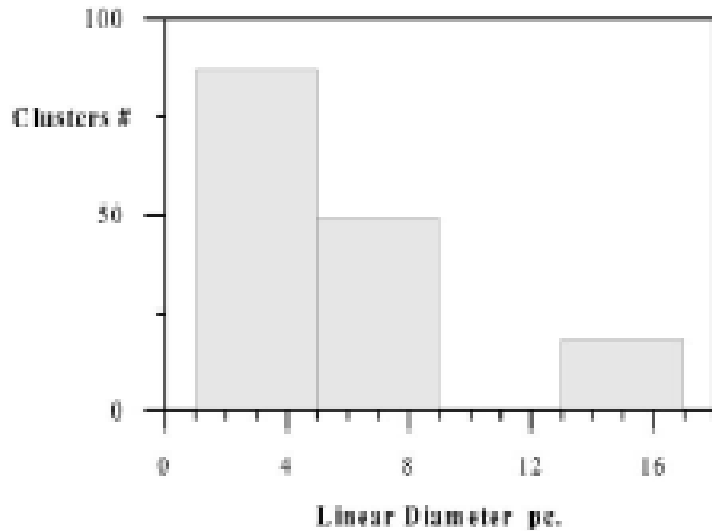
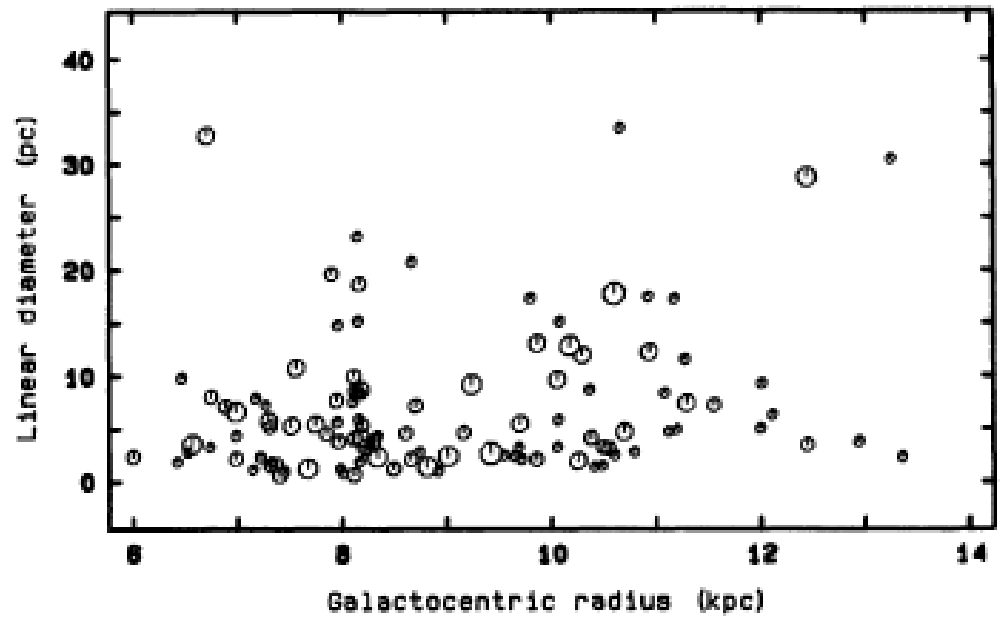
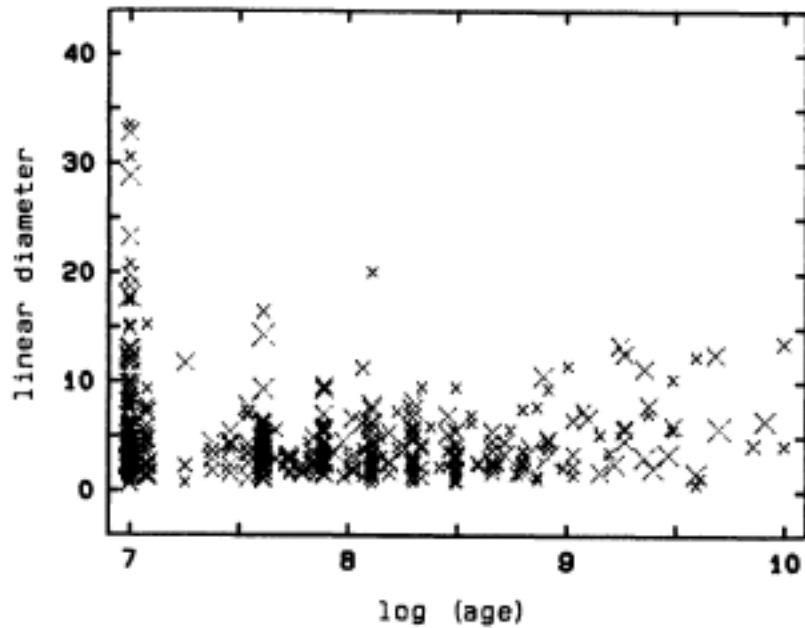
- How could we determine the diameter of a star cluster?
 1. The determination, for example inspection by eye, should be no problem. Be careful, most open clusters show no real concentration
 2. Count the number of stars (members) in concentric rings around the cluster center
 3. If the derived distribution is not symmetric => go to 1. and shift the coordinates of the center
- This procedure could be easily done via a computer program

III 2 m



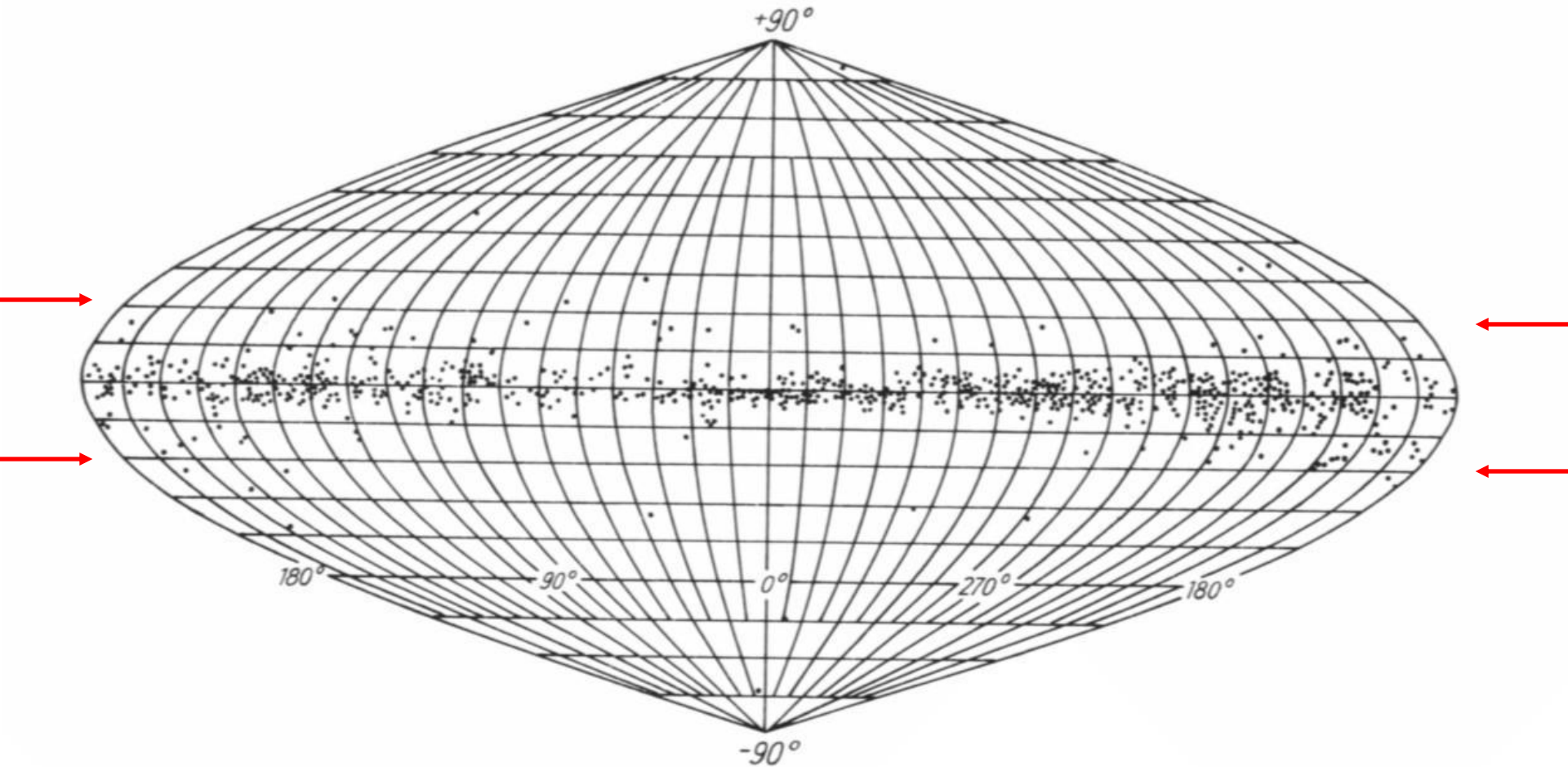
II 2 m



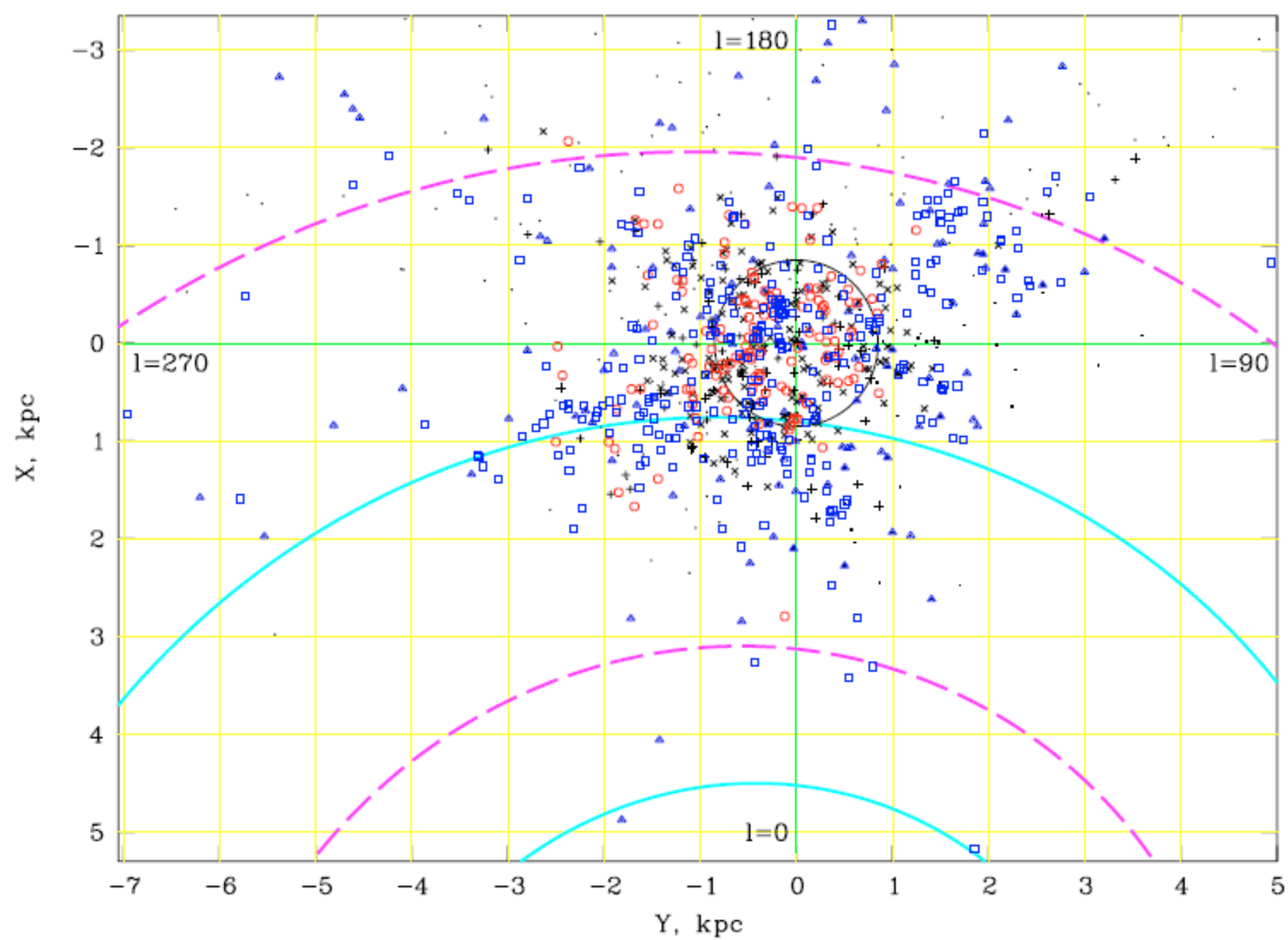


No correlation with the age
and the distance to the
Galactic distance

Galactic Distribution



± 20 degree Galactic latitude



Piskunov et al., 2006, *A&A*, 445, 545