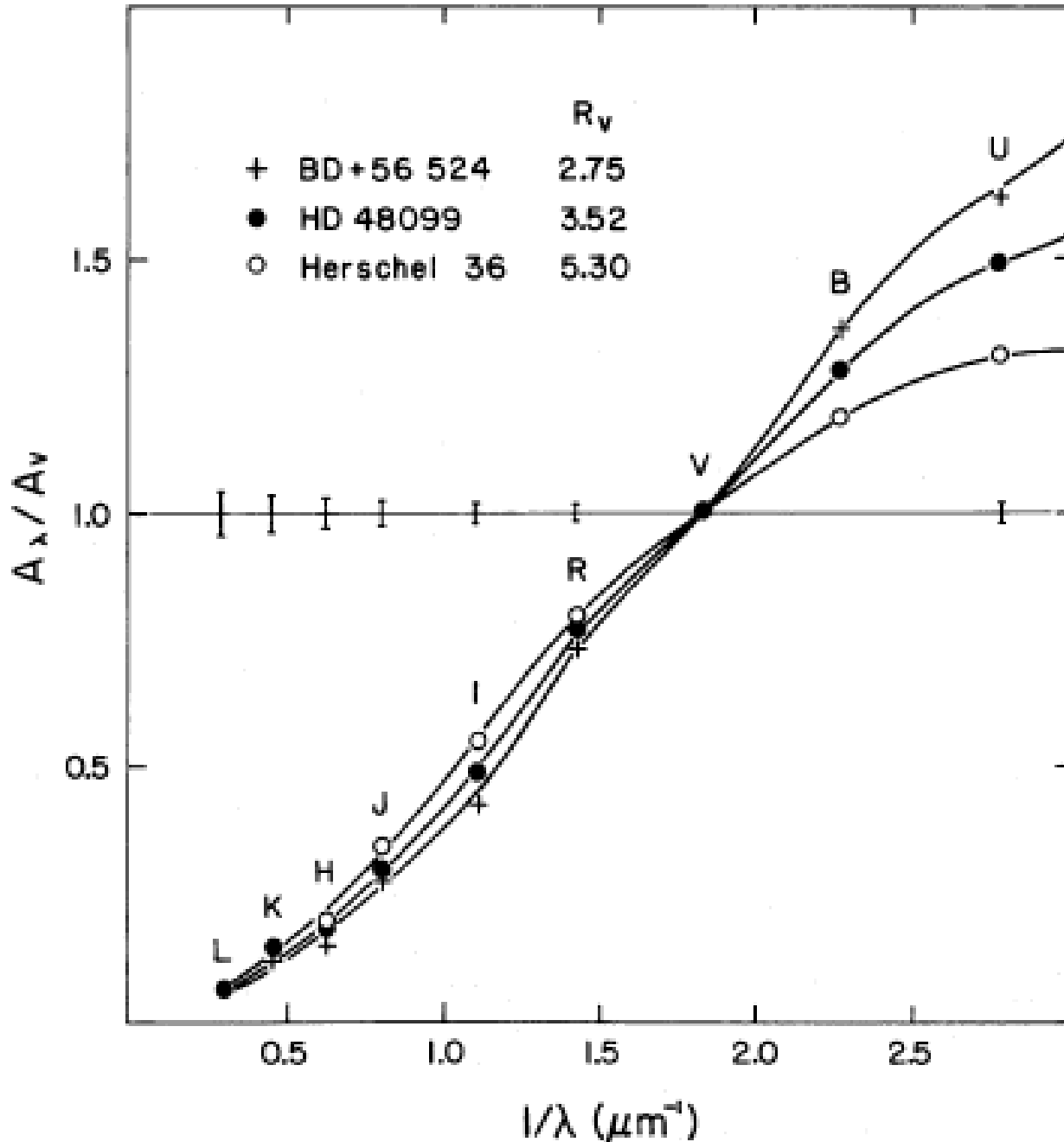


Extinction = Absorption = Reddening

- **General extinction** because of the ISM characteristics between the observer and the object
- **Differential extinction** within one star cluster because of local environment
- Both types are, in general **wavelength dependent**

Reasons for the interstellar extinction

- Light scatter at the interstellar dust
- Light absorption => Heating of the ISM
- Depending on the composition and density of the ISM
- Main contribution due to dust
- Simulations and calculations in Cardelli et al., 1989, ApJ, 345, 245



Important parameter:

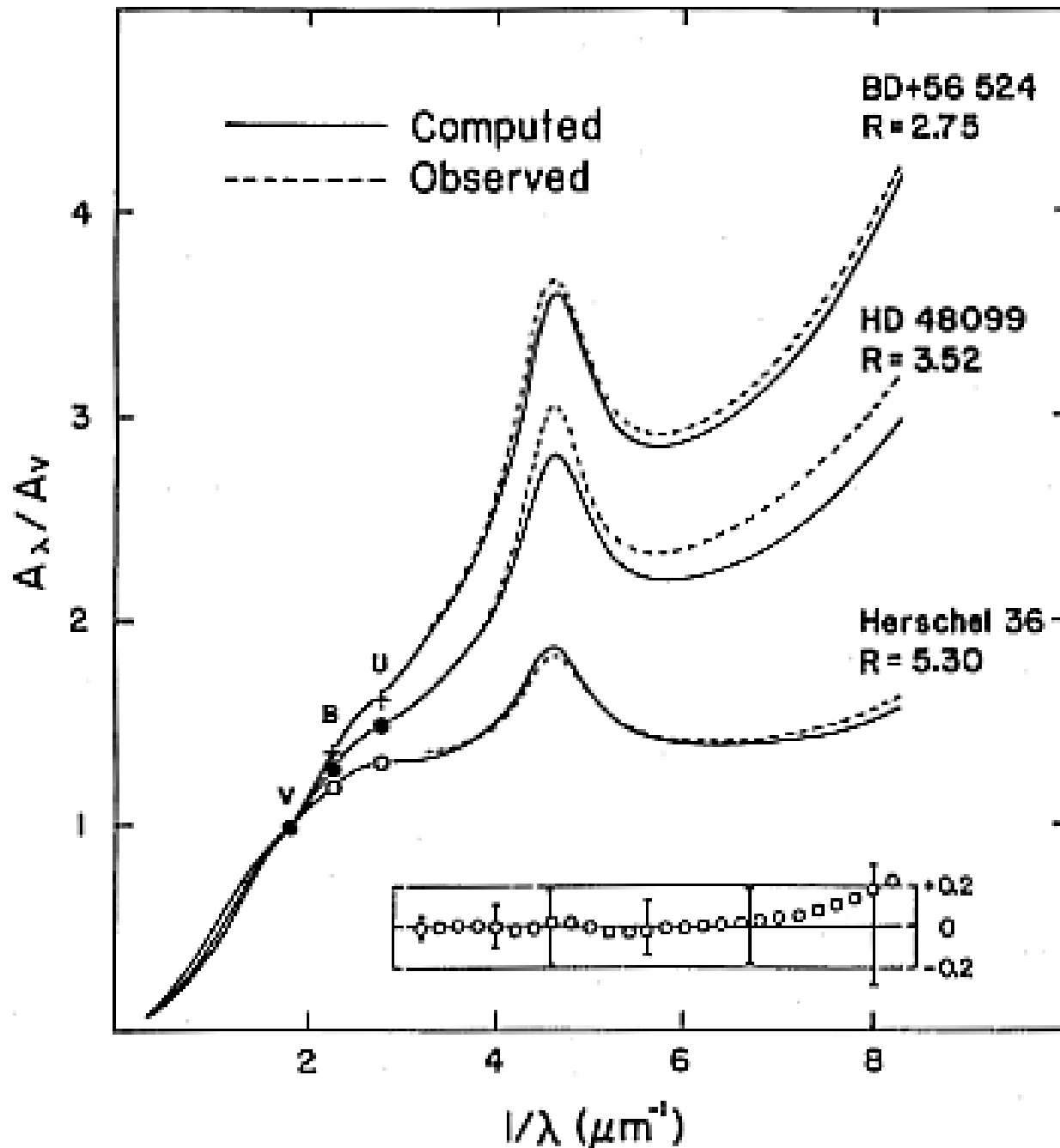
$$R_V = A_V/E(B-V)$$

Normalization factor

Standard value used is 3.1

Be careful, different values used!

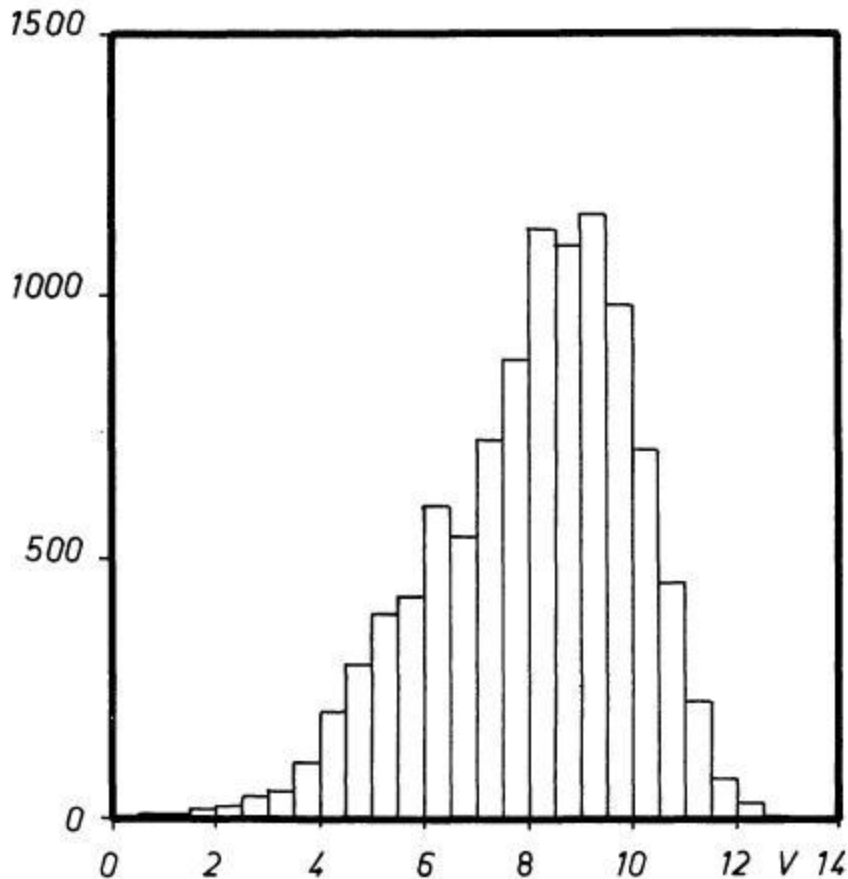
Depending on the line of sight



Dependency of
the extinction
from R_V

How to derive the reddening?

- From photometric and spectroscopic observations



Classical approach: Neckel & Klare, 1980, A&AS, 42, 251

Take all available UBV and Strömberg β photometry

MK classifications

FIGURE 2. — Distribution of the stars versus apparent V-magnitude.

4. **Extinction values and distances.** — The visual extinction A_v can be derived from

$$A_v = R \{ (B - V) - (B - V)_0 \}. \quad (2)$$

For R we take the value 3.1.

The intrinsic color $(B-V)_0$ follows directly from the MK calibration, if the MK type is known. In addition, $(B-V)_0$ can also be derived from the UBV and β data. The distance moduli are then given by

$$V - M_v - A_v = 5 \lg r - 5. \quad (3)$$

If we could derive A_v and r by both methods, we could use the mean values of extinction and distance moduli. This was possible for 1 020 stars. Figure 4 shows the frequency distribution of the differences

$$D = (V - M_v(\text{MK}) - A_v(\text{UBV}, \text{MK})) - \\ - (V - M_v(\beta) - A_v(\text{UBV}, \beta)). \quad (4)$$

Bailer-Jones,
1996, PhD,
Cambridge
University

SpT	Spectral Type	II	II/III	III	III/IV	IV	IV/V	V
1	O3	-	-	-	-	-	-	-
2	O4	-	-	-	-	-	-	-
3	O5	-8.20	-7.70	-7.20	-6.80	-6.40	-5.90	-5.60
4	O6	-7.60	-7.20	-6.85	-6.50	-6.10	-5.70	-5.40
5	O7	-7.00	-6.80	-6.60	-6.30	-5.90	-5.50	-5.20
6	O8	-6.50	-6.30	-6.20	-5.90	-5.60	-5.30	-5.00
7	O9	-6.00	-5.85	-5.70	-5.50	-5.30	-5.00	-4.70
8	B0	-5.40	-5.20	-5.00	-4.90	-4.80	-4.50	-4.20
9	B1	-5.00	-4.70	-4.40	-4.20	-4.00	-3.80	-3.60
10	B2	-4.80	-4.20	-3.60	-3.35	-3.10	-2.80	-2.50
11	B3	-4.60	-3.85	-3.10	-2.80	-2.50	-2.10	-1.70
12	B4	-4.50	-3.57	-2.55	-2.40	-2.15	-1.75	-1.35
13	B5	-4.40	-3.30	-2.20	-2.00	-1.80	-1.40	-1.00
14	B6	-4.20	-3.05	-1.90	-1.70	-1.50	-1.20	-0.70
15	B7	-4.00	-2.80	-1.60	-1.40	-1.20	-0.80	-0.40
16	B8	-3.80	-2.60	-1.00	-0.85	-0.70	-0.35	0.00
17	B9	-3.60	-2.45	-0.40	-0.30	-0.20	0.15	0.50
18	A0	-3.20	-1.90	0.10	0.20	0.30	0.65	1.00
19	A1	-3.00	-1.75	0.50	0.60	0.70	1.00	1.30
20	A2	-2.90	-1.65	0.70	0.85	1.00	1.30	1.60
21	A3	-2.80	-1.60	0.90	1.05	1.20	1.40	1.80
22	A4	-2.80	-1.55	1.05	1.15	1.30	1.63	1.95
23	A5	-2.70	-1.50	1.10	1.25	1.40	1.75	2.10

Assume $V = 10$ mag
and no reddening

O5: $-5.6 \Rightarrow 13\ 000$ pc

A0: $+1.0 \Rightarrow 630$ pc

G0: $+4.5 \Rightarrow 125$ pc

M0: $+8.9 \Rightarrow 15$ pc

Assume $V = 20$ mag
and no reddening

O5: $-5.6 \Rightarrow 1.3$ Mpc

A0: $+1.0 \Rightarrow 63$ kpc

G0: $+4.5 \Rightarrow 12.5$ kpc

M0: $+8.9 \Rightarrow 1.5$ kpc

24	A6	-2.65	-1.45	1.15	1.35	1.60	1.95	2.30
25	A7	-2.60	-1.40	1.20	1.50	1.80	2.10	2.40
26	A8	-2.60	-1.40	1.30	1.65	2.05	2.25	2.50
27	A9	-2.55	-1.35	1.40	1.75	2.10	2.35	2.60
28	F0	-2.50	-1.30	1.50	1.85	2.20	2.45	2.70
29	F2	-2.50	-1.30	1.60	2.00	2.40	2.75	3.10
30	F3	-2.40	-1.20	1.65	2.10	2.45	2.90	3.35
31	F5	-2.30	-1.10	1.70	2.10	2.50	3.05	3.60
32	F6	-2.25	-1.05	1.75	2.15	2.55	3.18	3.80
33	F7	-2.20	-1.00	1.75	2.15	2.60	3.30	4.00
34	F8	-2.20	-1.00	1.75	2.20	2.80	3.50	4.20
35	G0	-2.10	-0.95	1.70	2.15	2.90	3.70	4.45
36	G1	-2.05	-0.90	1.70	2.10	3.00	3.80	4.70
37	G2	-2.00	-0.90	1.60	2.10	3.00	3.90	4.80
38	G3	-2.00	-0.85	1.60	2.05	3.05	4.00	5.00
39	G5	-2.00	-0.85	1.60	2.00	3.10	4.15	5.20
40	G6	-2.00	-0.80	1.50	2.00	3.15	4.23	5.30
41	G8	-2.00	-0.80	1.35	1.95	3.20	4.35	5.50
42	K0	-2.00	-0.80	1.20	1.87	3.20	4.50	5.80
43	K1	-2.00	-0.85	1.00	1.80	3.30	4.70	6.10
44	K2	-2.00	-0.90	0.80	1.80	3.30	4.80	6.30
45	K3	-2.00	-1.00	0.60	1.80	3.40	5.00	6.60
46	K4	-2.10	-1.00	0.20	-	-	-	6.90
47	K5	-2.20	-1.00	0.00	-	-	-	7.50
48	M0	-2.40	-1.00	-1.10	-	-	-	8.90
49	M1	-2.50	-1.10	-0.40	-	-	-	9.60
50	M2	-2.50	-1.10	-0.60	-	-	-	10.30
51	M3	-2.50	-1.20	-0.70	-	-	-	10.80
52	M4	-2.50	-1.20	-0.80	-	-	-	11.40
53	M5	-2.50	-1.30	-0.90	-	-	-	12.30
54	M6	-2.50	-1.30	-1.00	-	-	-	13.20
55	M7	-2.50	-1.40	-1.10	-	-	-	14.00
56	M8	-2.50	-1.50	-1.20	-	-	-	16.50
57	M9	-	-	-	-	-	-	-

TABLE V. The $M_v(\beta)$ calibration.

β (mag)	$M_v(\beta)$ (mag)	β (mag)	$M_v(\beta)$ (mag)
2.560	-6.51	2.720	-0.27
2.570	-5.84	2.730	-0.10
2.580	-5.22	2.740	0.04
2.590	-4.65	2.750	0.18
2.600	-4.12	2.760	0.30
2.610	-3.62	2.770	0.41
2.620	-3.17	2.780	0.51
2.630	-2.75	2.790	0.60
2.640	-2.36	2.800	0.68
2.650	-2.01	2.810	0.76
2.660	-1.69	2.820	0.83
2.670	-1.39	2.830	0.90
2.680	-1.12	2.840	0.97
2.690	-0.87	2.850	1.03
2.700	-0.65	2.860	1.10
2.710	-0.45	2.870	1.17
		2.880	1.24
		2.890	1.31
		2.900	1.39

Crawford,
1976, AJ,
83, 48

Example
for the β
index

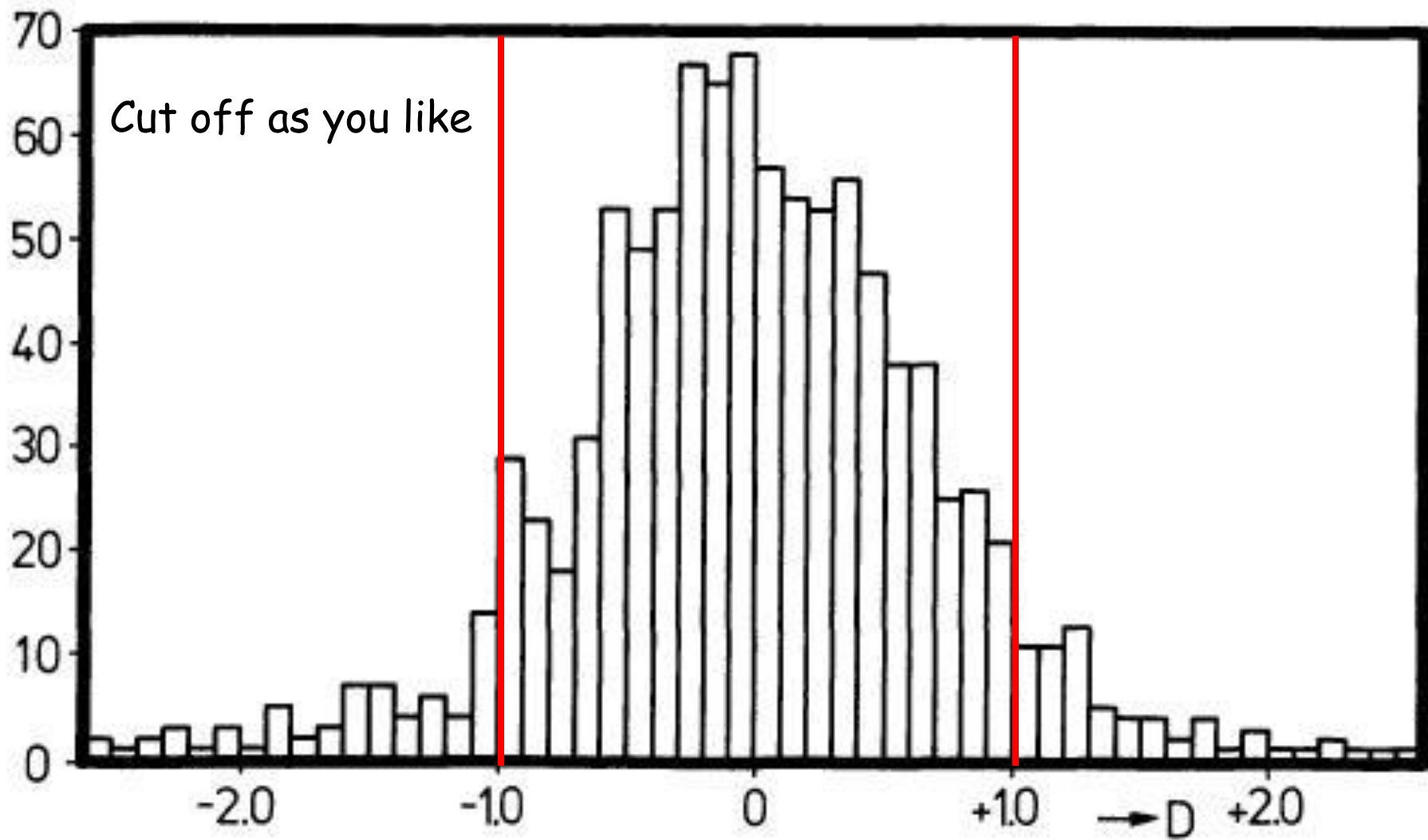


FIGURE 4. — Frequency distribution of the differences between the distance moduli derived from $UBV + MK$ and $UBV + \beta$ data.

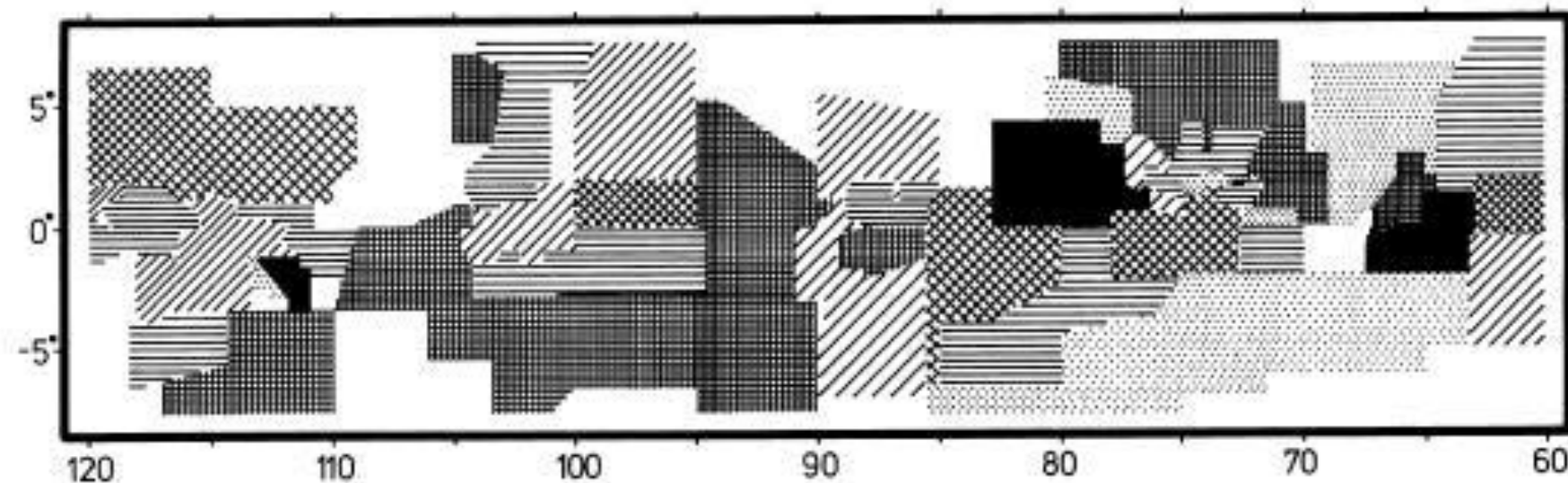
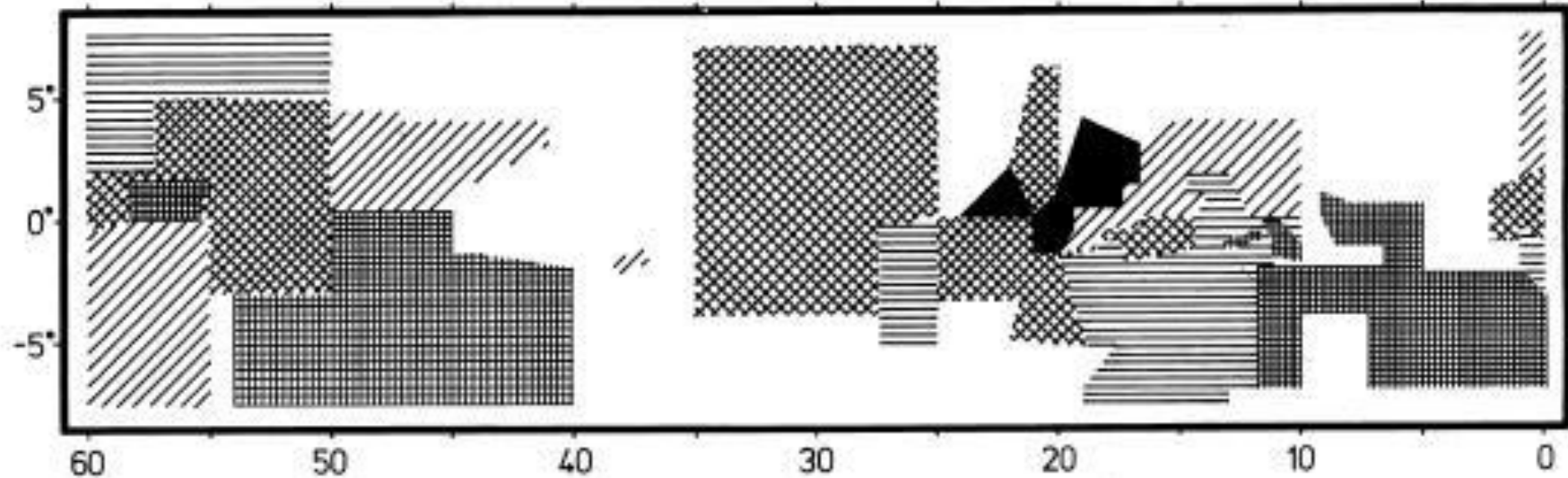
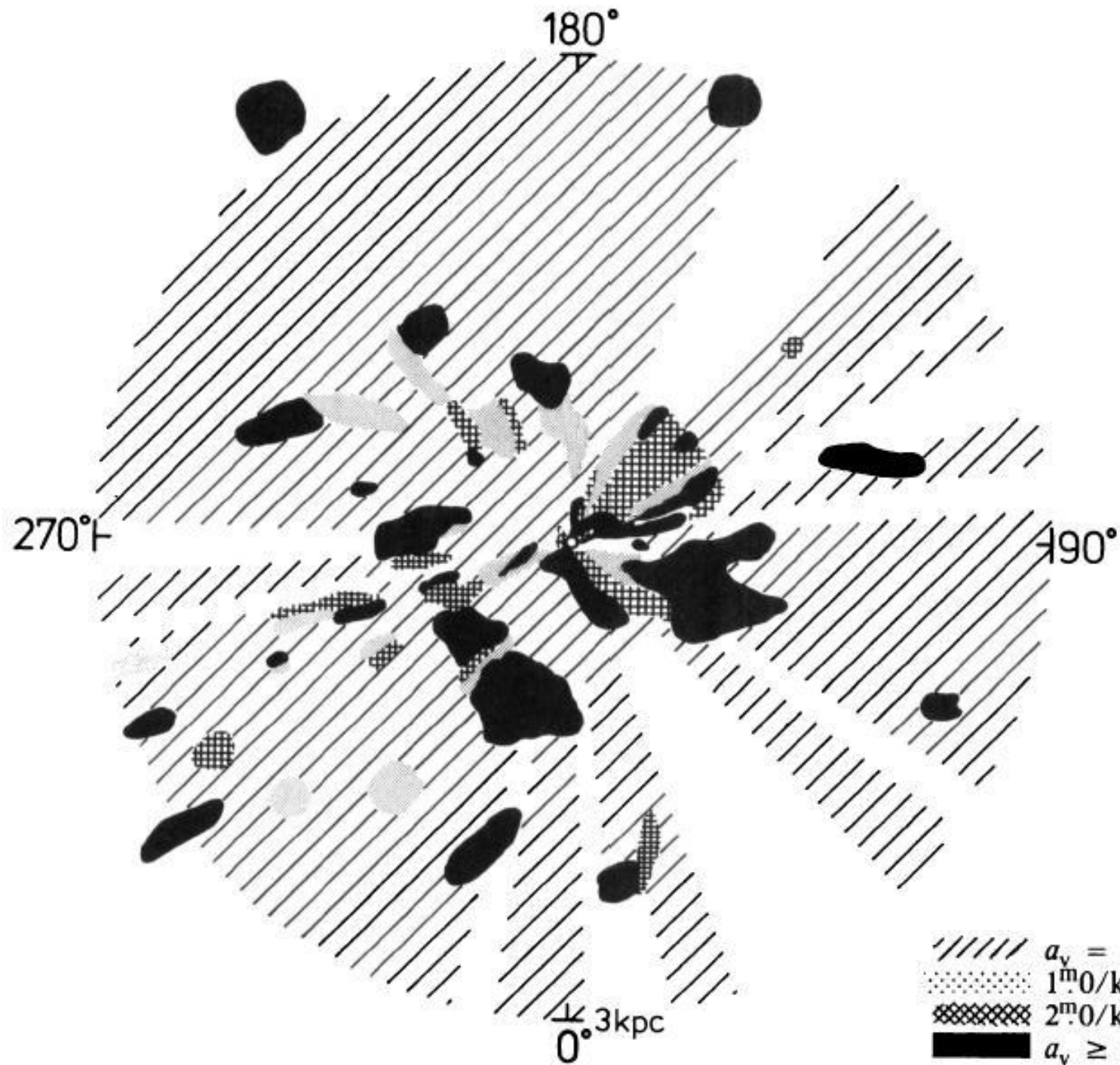
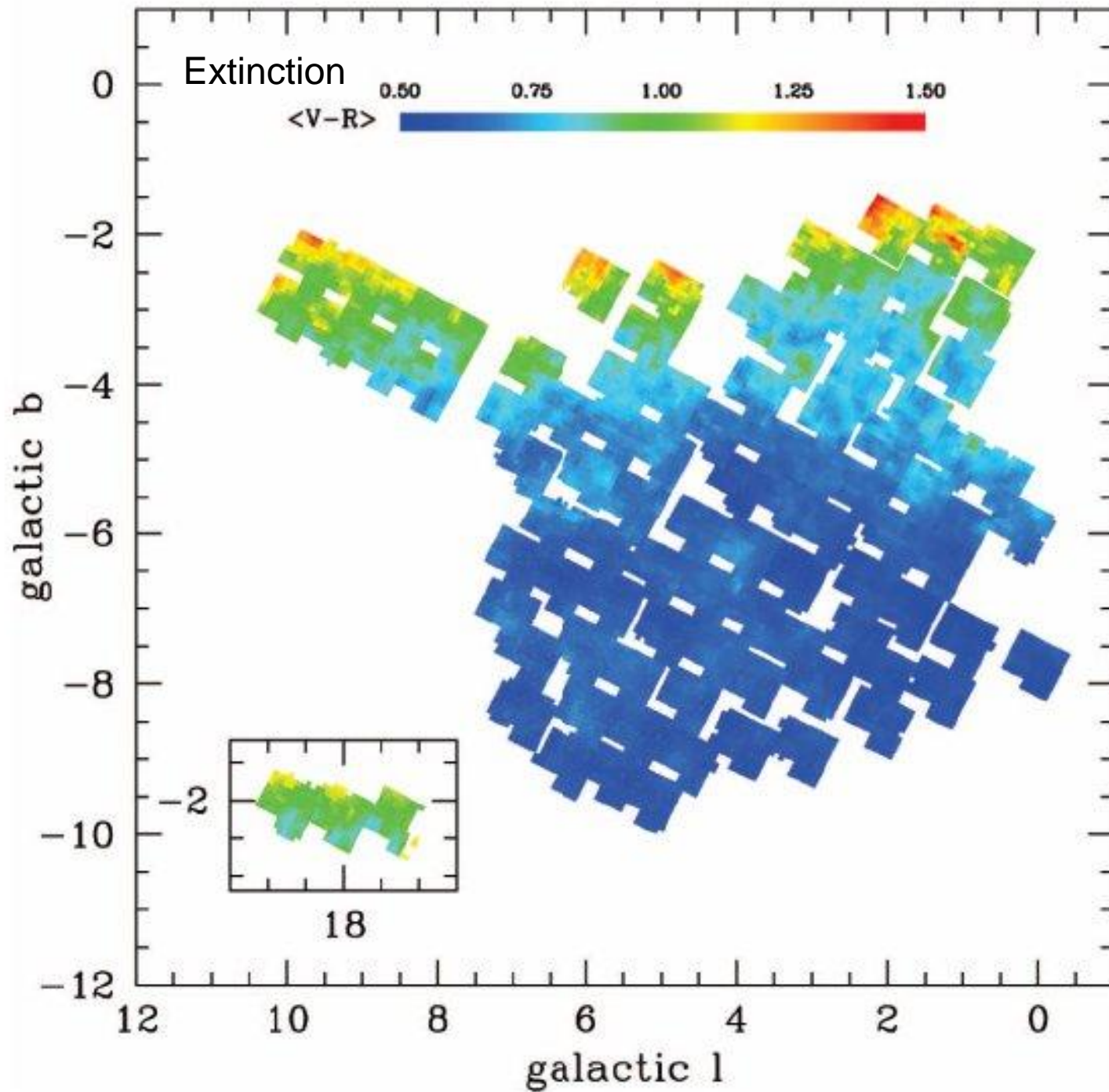
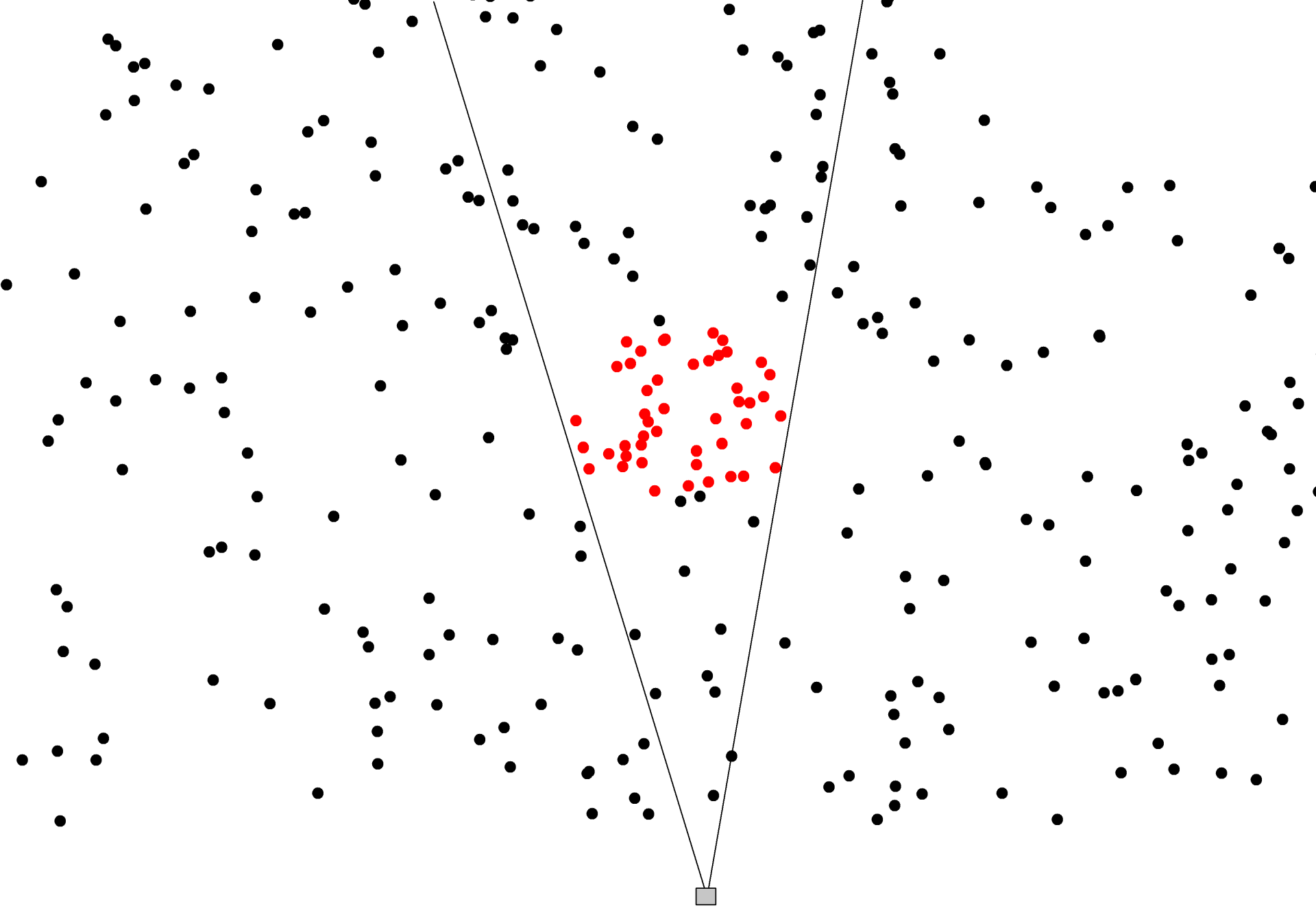


FIGURE 8. — The extinction at $r = 1$ kpc in the Milky Way.









- The absolute diameters are "constant", to about 20 pc
 1. 100 pc: 680'
 2. 1 000 pc: 68'
 3. 50 000 pc: 1.38'
- For near clusters => background
- For "intermediate" clusters => foreground + background
- For distant clusters => foreground

New all-sky surveys

- With all-sky surveys we are able to determine extinction maps in a statistical way
- Several filters in several wavelength regions are needed, for example
 - 2MASS: JHKs
 - UCAC-3: BVR
 - Gaia: filters?
 - More to come

The most simple approach of a colour excess method is to measure the apparent brightness of a star at two different wavelengths, m_{λ_1} and m_{λ_2} , and compare the colour $m_{\lambda_1} - m_{\lambda_2}$ with the theoretical value for main-sequence stars or the colour of stars measured in an extinction-free control field $m_{\lambda_1}^{\text{tr}} - m_{\lambda_2}^{\text{tr}}$ (e.g. Lada et al. 1994). The colour excess $\langle \lambda_1 - \lambda_2 \rangle$ is defined as

$$\langle \lambda_1 - \lambda_2 \rangle \equiv (m_{\lambda_1} - m_{\lambda_2}) - (m_{\lambda_1}^{\text{tr}} - m_{\lambda_2}^{\text{tr}}). \quad (7)$$

If we assume that this colour excess is entirely due to extinction and, as for the star count analysis, a constant β is valid, we can determine the extinction at λ_2 by

$$A_{\lambda_2} = \frac{\langle \lambda_1 - \lambda_2 \rangle}{(\lambda_2/\lambda_1)^\beta - 1}. \quad (8)$$

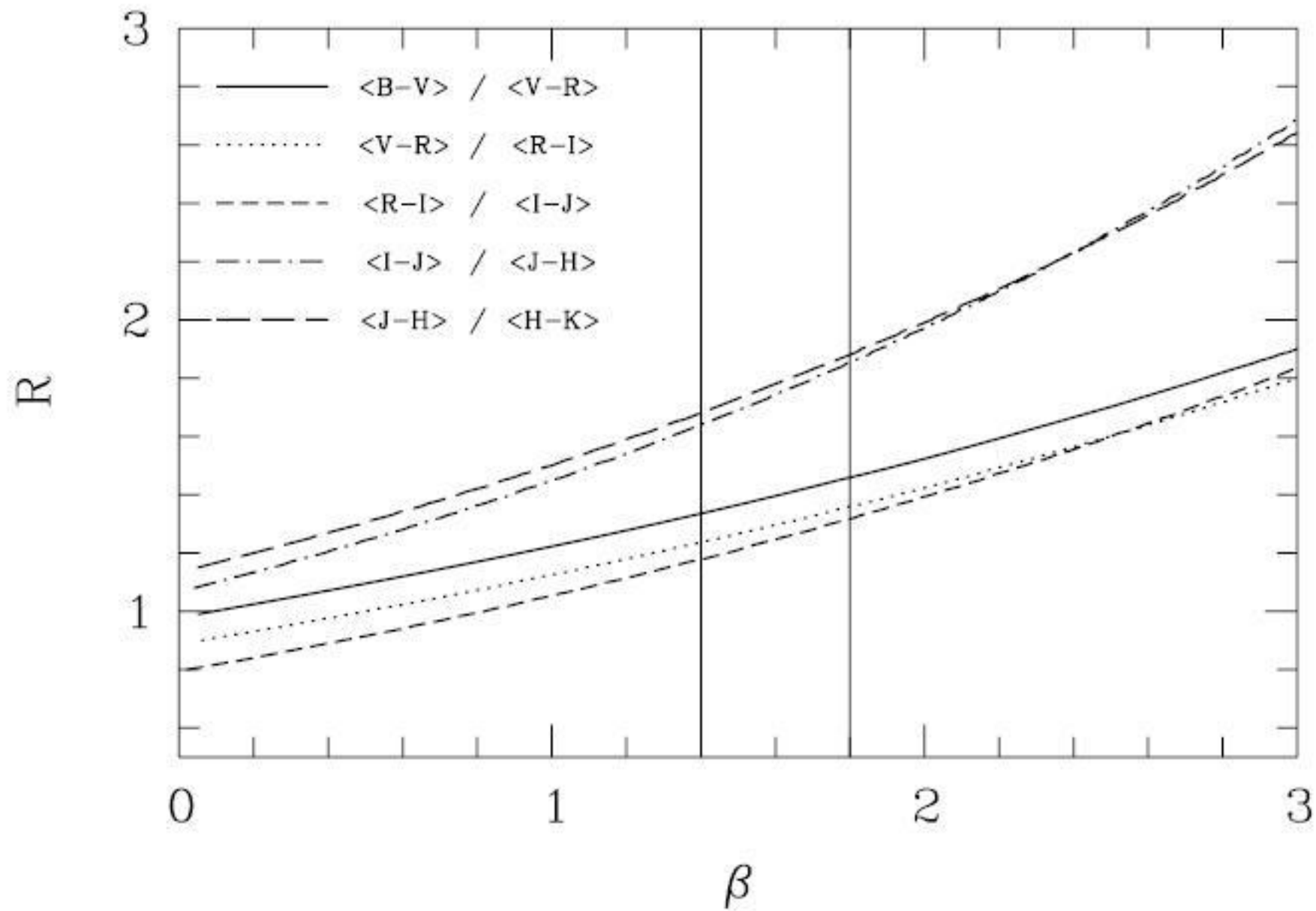
Measuring $\langle \lambda_2 - \lambda_3 \rangle$, with $\lambda_1 < \lambda_2 < \lambda_3$, we as well can determine the extinction at λ_2 :

$$A_{\lambda_2} = \frac{\langle \lambda_2 - \lambda_3 \rangle}{1 - (\lambda_3/\lambda_2)^{-\beta}}. \quad (9)$$

The right-hand side of both equations should essentially give the same value. We can define the colour excess ratio $R \equiv \langle \lambda_1 - \lambda_2 \rangle / \langle \lambda_2 - \lambda_3 \rangle$ and obtain the following equation for β :

$$0 = \left(\frac{\lambda_2}{\lambda_1} \right)^{\beta} + R \left(\frac{\lambda_3}{\lambda_2} \right)^{-\beta} - R - 1. \quad (10)$$

More filters mean more accurate results



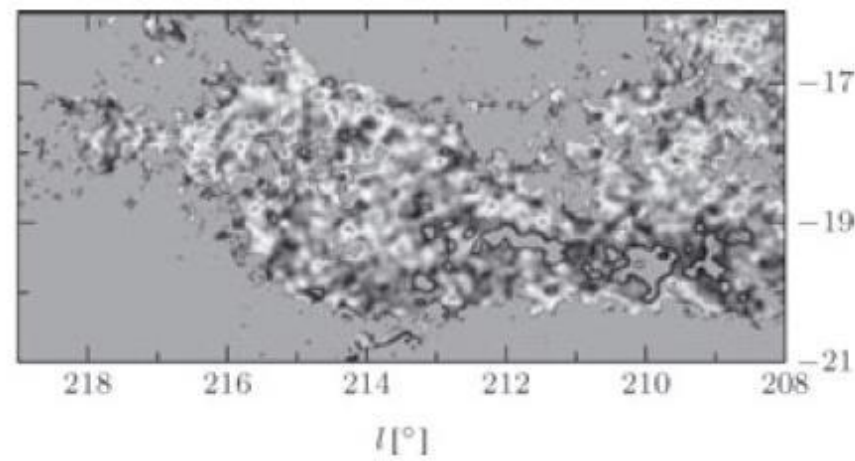
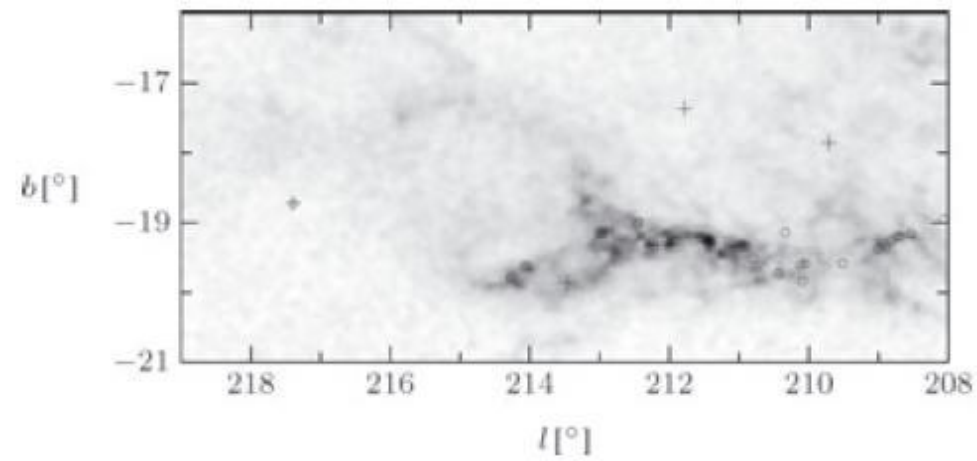
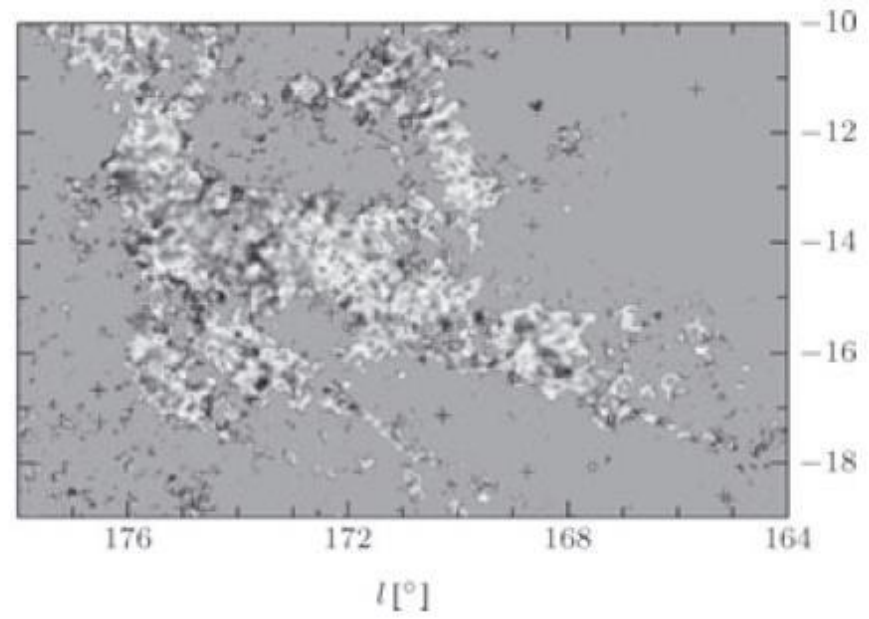
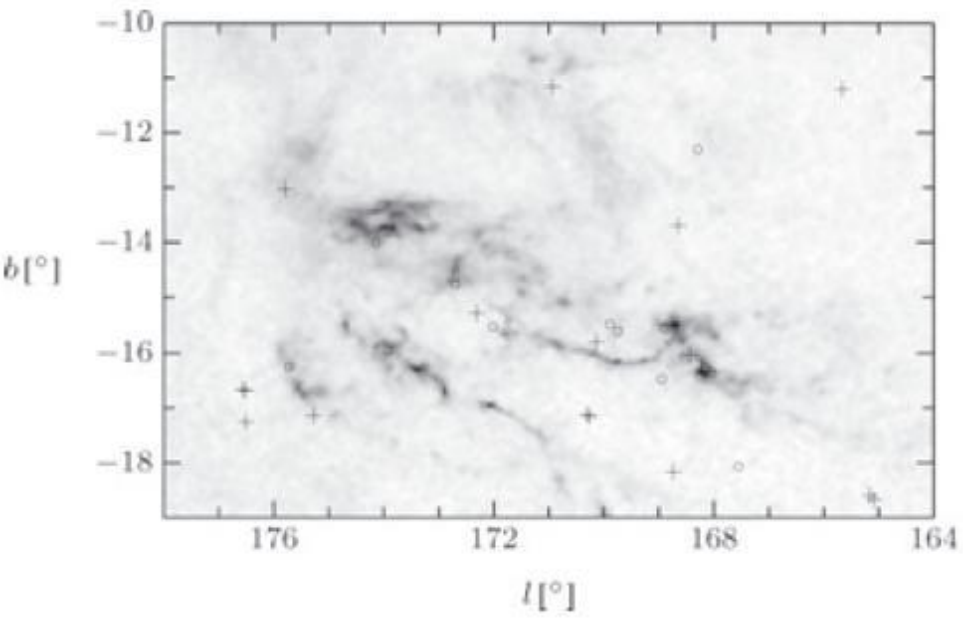
(i) Star count and colour excess extinction maps are calculated without foreground star corrections. These maps are used to determine the opacity index β , which is used to convert the colour excess maps into extinction maps.

(ii) Foreground stars have to be selected. Extinction maps from colour excess are usually less noisy but are less reliable for distant clouds. Thus the extinction map that possesses the larger extinction values should be used for the foreground star selection.

(iii) Now one needs to iterate the first two steps until no further foreground stars are found. Foreground stars cannot be identified in regions without extinction. We thus have to consider the accumulated star count diagram of the foreground stars when determining the extinction map using star counts. Using the colours of the identified foreground stars and Monte Carlo techniques, a colour offset for background regions can be determined.

(iv) The final star count and colour excess maps are used to determine β and to convert the colour excess into extinction maps.

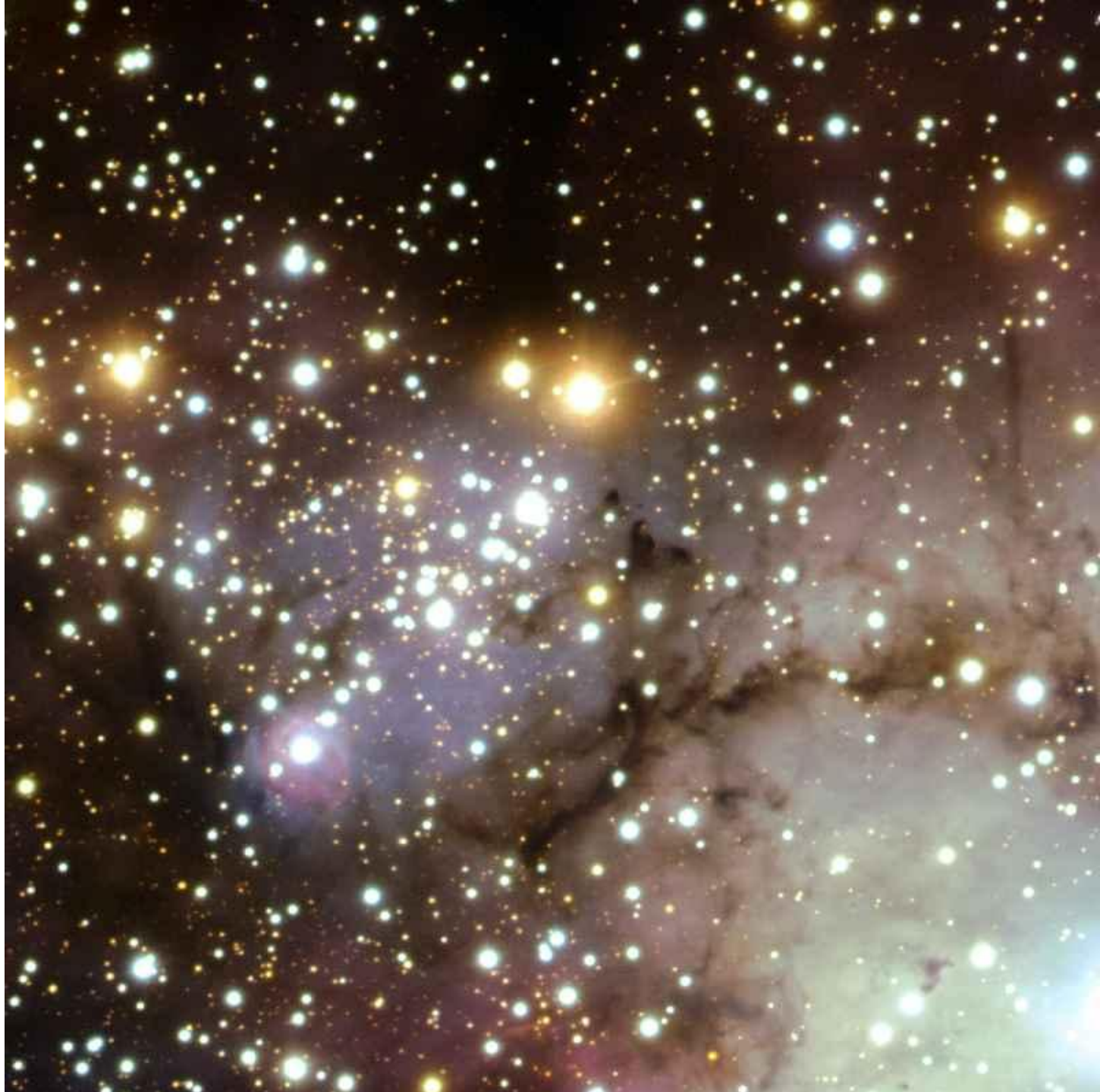
(v) For a most accurate calibration determine the distance correction using the cloud distance and coordinates, as well as the completeness limit of the observations.

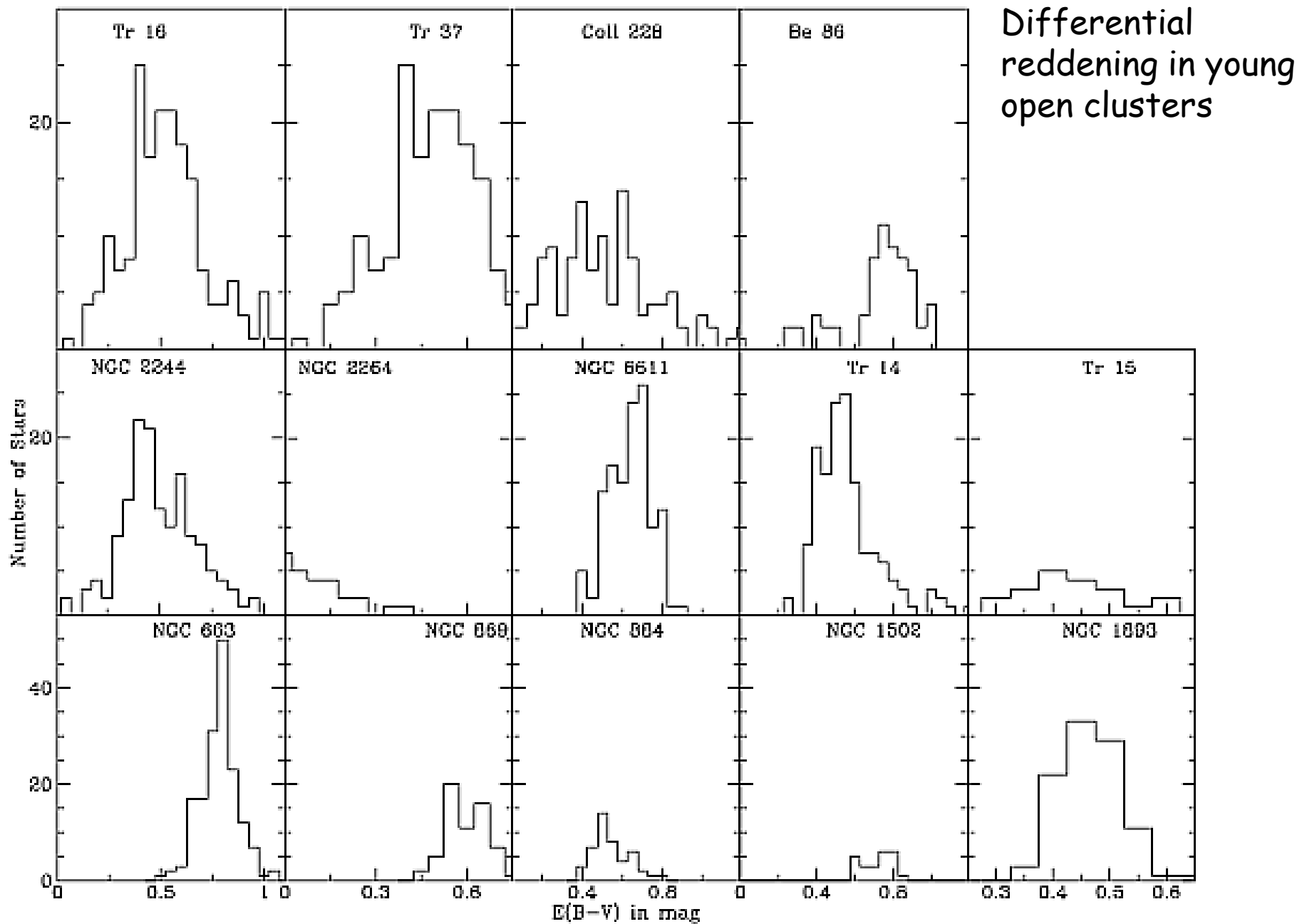


Haffner 18

Age about 8 Myr
 $d = 6000$ pc

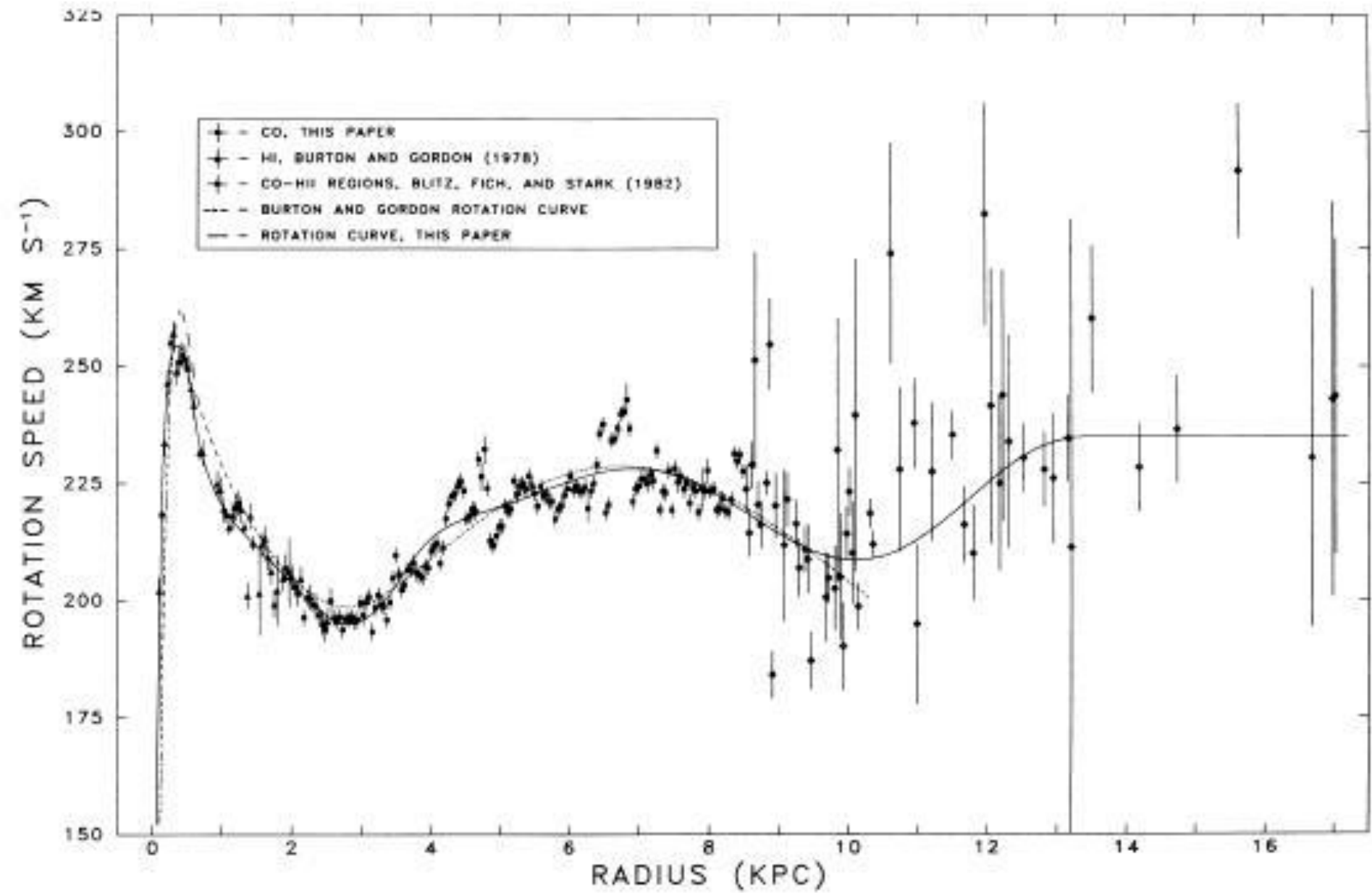
differential
extinction within
the cluster





Kinematical membership criteria

- Members follow the motion of the cluster center of gravity
- Internal velocity distribution
- From best to ...
 1. Radial velocity and proper motion
 2. Radial velocity
 3. Proper motion

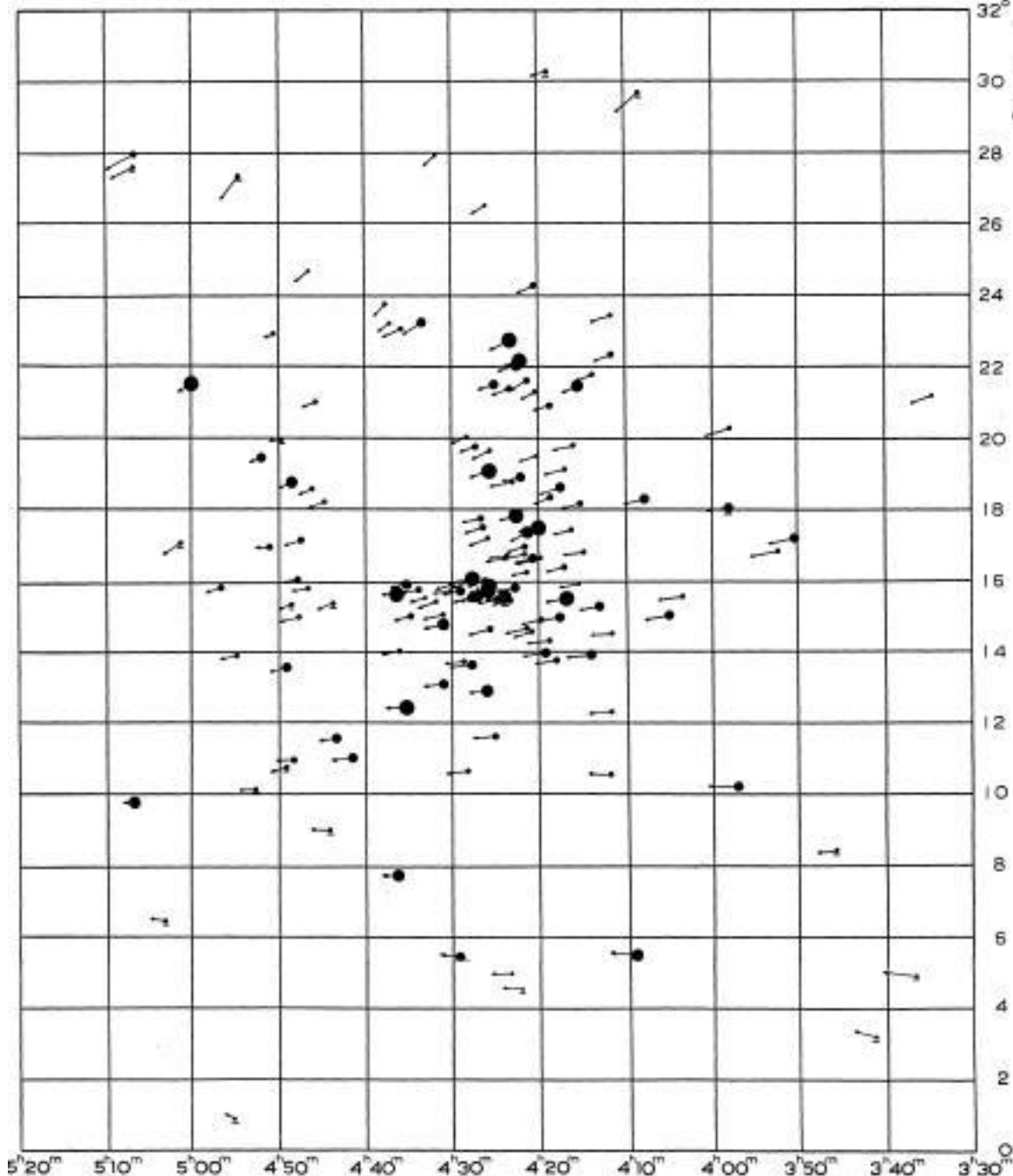


Clemens, 1985, ApJ, 295, 422

Hyades

Van Bueren, 1952, BAN,
11, 385

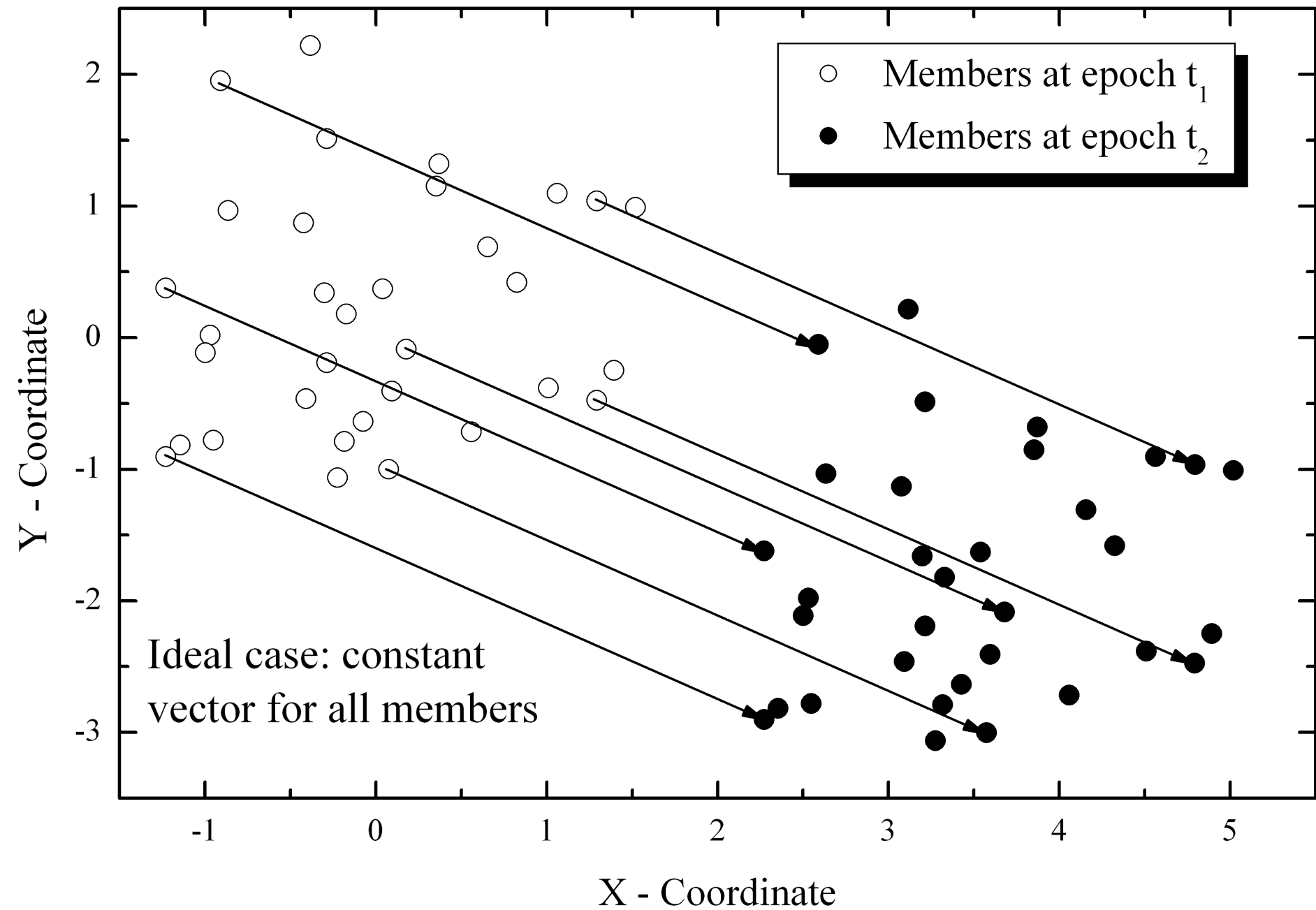
After the
correction of the
Solar motion



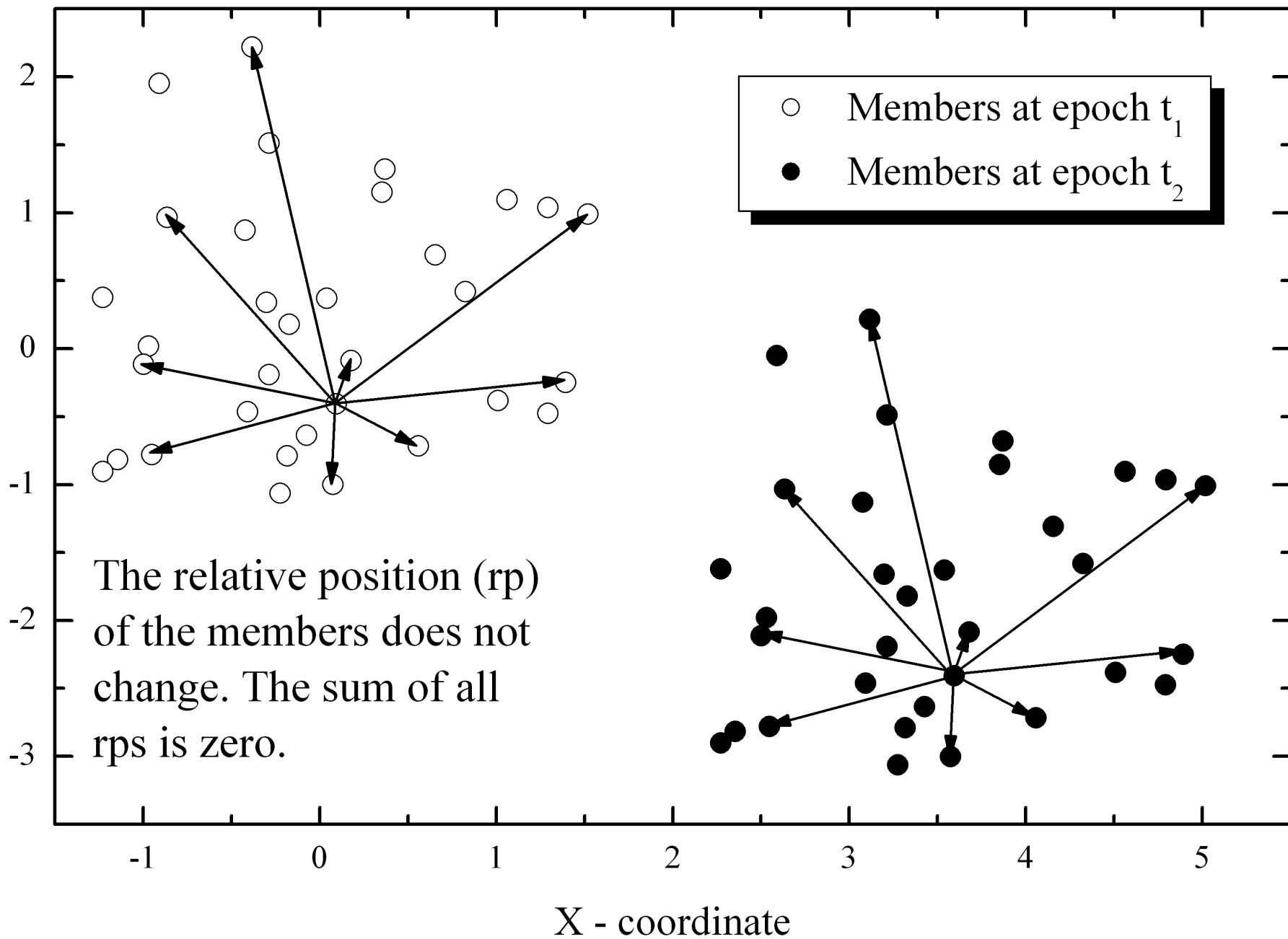
Map of the Hyades brighter than $9^m.6$ visual. The size of the dots is a measure for the magnitude of the stars; the arrows show the annual proper motion ($1 \text{ mm} \approx 7^m.030$). Five stars in the very outer regions of the cluster are not shown on the map. Underlined dots indicate stars of which no radial velocity is known.

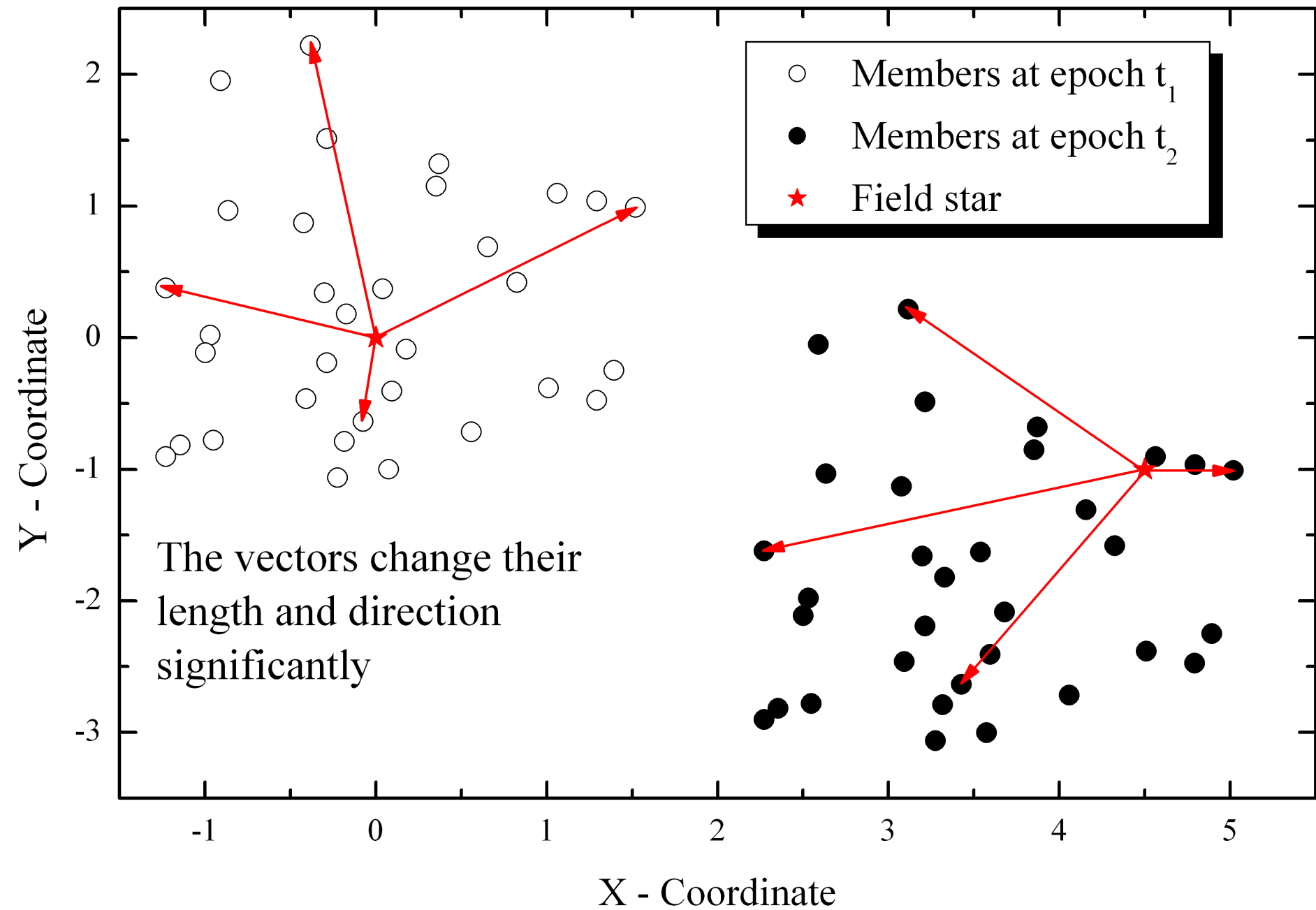
Determination of the kinematical membership

- Three possibilities:
 1. Observation of the position at two difference times (= epochs), with a very large time basis. First photographic plates around 1860, largest time scales about 150 years
 2. Proper motions of stars in the direction of the Declination α and Right Ascension δ
 3. Radial velocity measurements



Y - Coordinate





Mathematical method

- Measurement of the position (X, Y) at two different epochs t_1 (') and t_2 (' ') for each star
- Calculate the absolute distance in X and Y for both epochs and each star individually

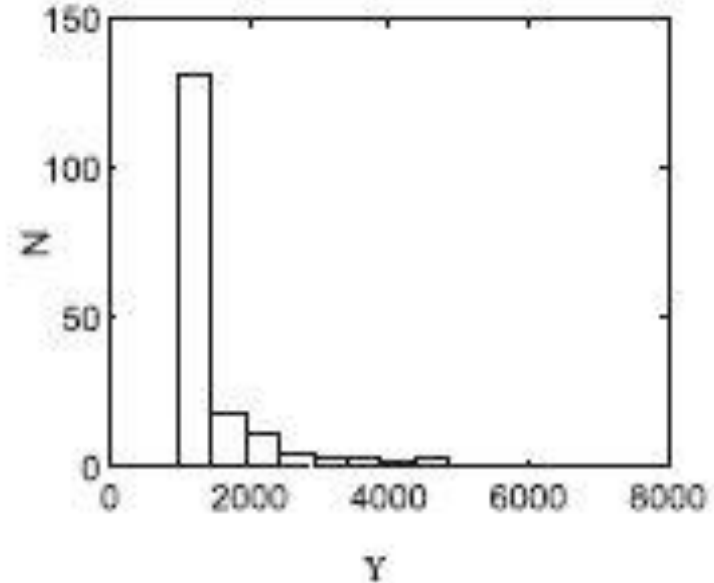
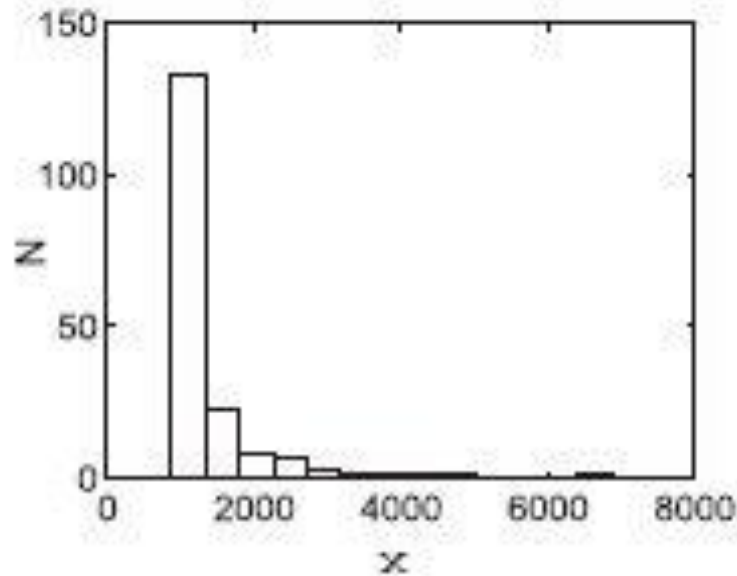
$$S'_{x_i} = \sum_{j=1}^N |x'_i - x'_j|, \quad S'_{y_i} = \sum_{j=1}^N |y'_i - y'_j|, \quad (1)$$

$$S''_{x_i} = \sum_{j=1}^N |x''_i - x''_j|, \quad S''_{y_i} = \sum_{j=1}^N |y''_i - y''_j|, \quad (2)$$

- Determine the differences of the absolute distances

$$\delta S_{x_i} = S'_{x_i} - S''_{x_i}, \quad \delta S_{y_i} = S'_{y_i} - S''_{y_i}, \quad i = 1, \dots, N. \quad (3)$$

- Plot the histograms of the differences of the absolute distances. The members have to group around the minimum of the distributions (ideal case: minimum = zero).



Example from Javakhishvili et al., 2006, *A&A*, 447, 915 for Collinder 121

Now we need a mathematical formalism to describe the membership probability from the distributions

- Calculate the absolute distance in X and Y for both epochs and each star individually

$$\bar{S}'_{x_i} = \sum_{j=1}^N (x'_i - x'_j), \quad \bar{S}'_{y_i} = \sum_{j=1}^N (y'_i - y'_j), \quad (4)$$

$$\bar{S}''_{x_i} = \sum_{j=1}^N (x''_i - x''_j), \quad \bar{S}''_{y_i} = \sum_{j=1}^N (y''_i - y''_j). \quad (5)$$

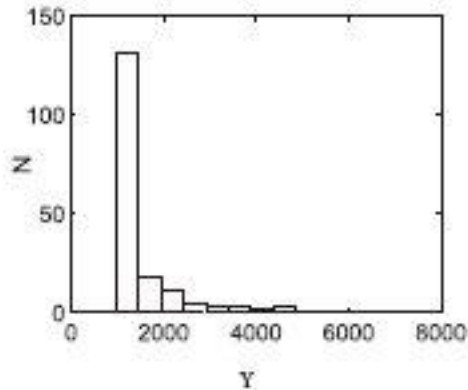
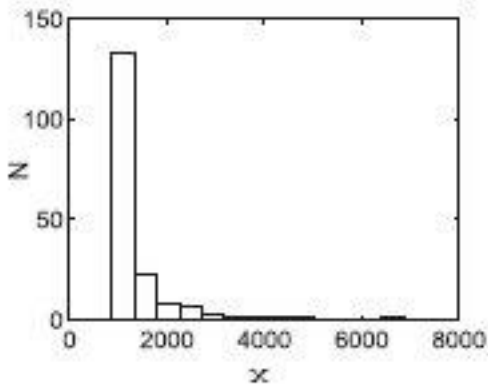
- Plot the histograms of the differences of the absolute distances
- The distributions are fitted with Gaussian functions

$$f(x) = \frac{A_x}{w_x \sqrt{\pi/2}} e^{-2\left(\frac{x-x_0}{\sigma_x}\right)^2}, \quad f(y) = \frac{A_y}{w_y \sqrt{\pi/2}} e^{-2\left(\frac{y-y_0}{\sigma_y}\right)^2}, \quad (6)$$

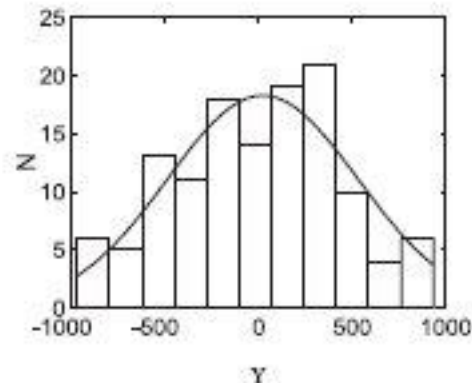
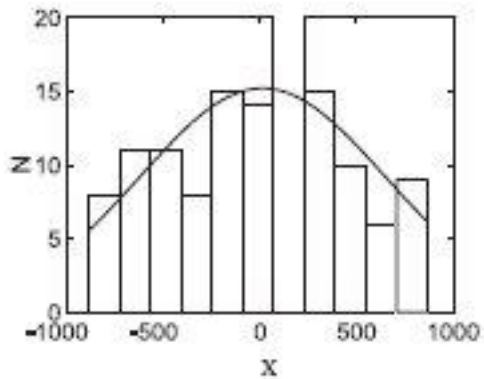
- The probability p , if a star is member of the star cluster is defined as

$$p_x = e^{-2\left(\frac{x-x_0}{\sigma_x}\right)^2}, \quad p_y = e^{-2\left(\frac{y-y_0}{\sigma_y}\right)^2}. \quad (7)$$

$$p = p_x * p_y. \quad (8)$$



Javakhishvili et al.,
2006, A&A, 447, 915 for
Collinder 121



From these diagrams, the
membership probability can
be exactly determined

- In the same way, the proper motions in α and δ can be used, the basic equations and the determination of the membership probability is exactly the same

$$\delta\mu_{\alpha_i} = \sum_{j=1}^N |\mu_{\alpha_i} - \mu_{\alpha_j}|, \quad \delta\mu_{\delta_i} = \sum_{j=1}^N |\mu_{\delta_i} - \mu_{\delta_j}| \quad (9)$$

$$\tilde{\delta}\mu_{\alpha_i} = \sum_{j=1}^N (\mu_{\alpha_i} - \mu_{\alpha_j}), \quad \tilde{\delta}\mu_{\delta_i} = \sum_{j=1}^N (\mu_{\delta_i} - \mu_{\delta_j}). \quad (10)$$

But the errors of ground based proper motions are rather large, most catalogues are complete to $V < 11$ mag only. This limits us, currently, to distances of about 1000 pc.

*GAI*A Satellite: Start 2011, up to 5000 pc (?)

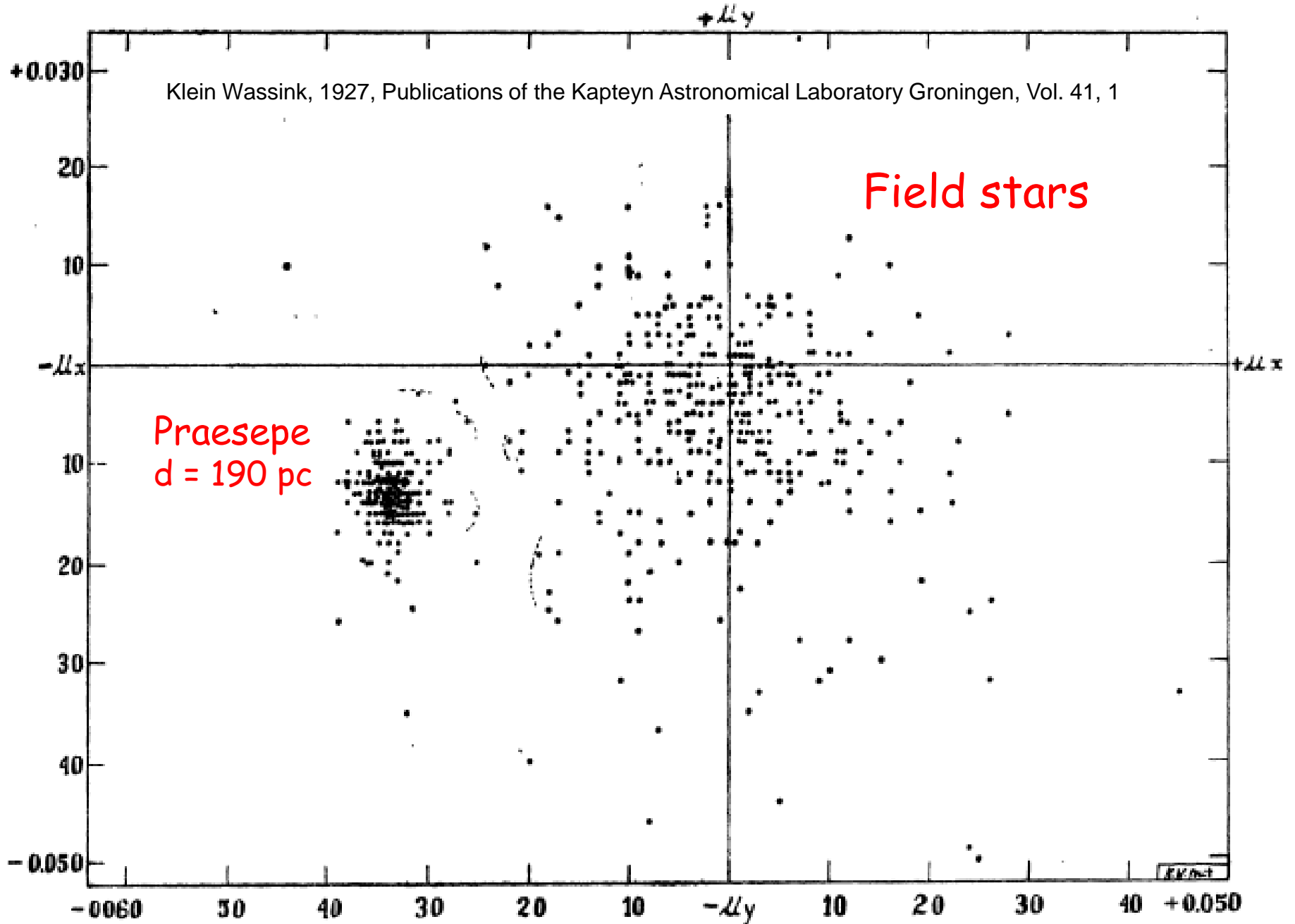
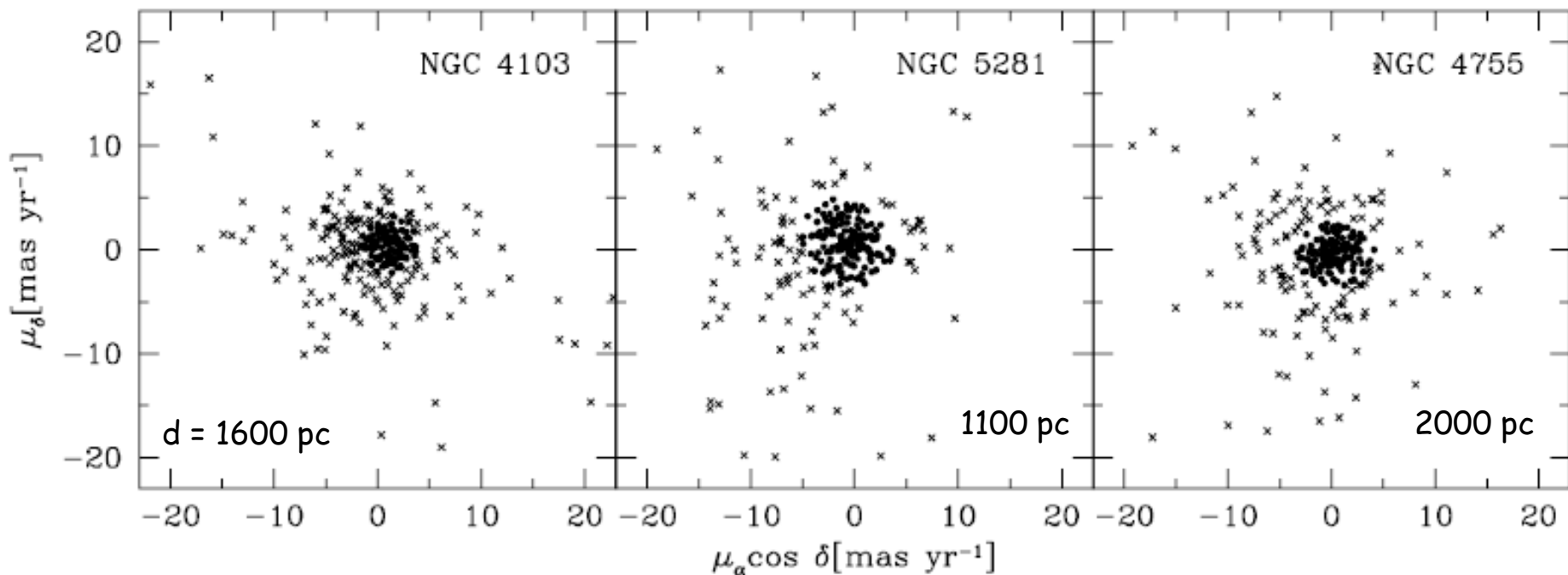


Figure 2. Diagram of the absolute proper motions of the Catalogue; photographic magnitude 6 to 14^o, numbers 1 to 531. The dotted lines separate the Praesepe stars from the backgroundstars.



object	$\mu_\alpha \cos \delta$ [mas yr ⁻¹]	μ_δ [mas yr ⁻¹]
NGC 4103	$+0.91 \pm 1.4$	$+0.36 \pm 1.4$
field	-0.92 ± 5.0	$+0.27 \pm 5.0$
NGC 5281	-0.70 ± 2.1	$+0.67 \pm 2.1$
field	-4.36 ± 7.0	-1.08 ± 7.0
NGC 4755	$+0.18 \pm 1.7$	-0.32 ± 1.7
field	-1.71 ± 6.5	-0.99 ± 6.5

Mean values

TYCHO2 data

$$\mu_\alpha \cos \delta = -6.4 \pm 4.6 \text{ mas yr}^{-1}$$

$$\mu_\delta = +0.3 \pm 3.9 \text{ mas yr}^{-1}$$

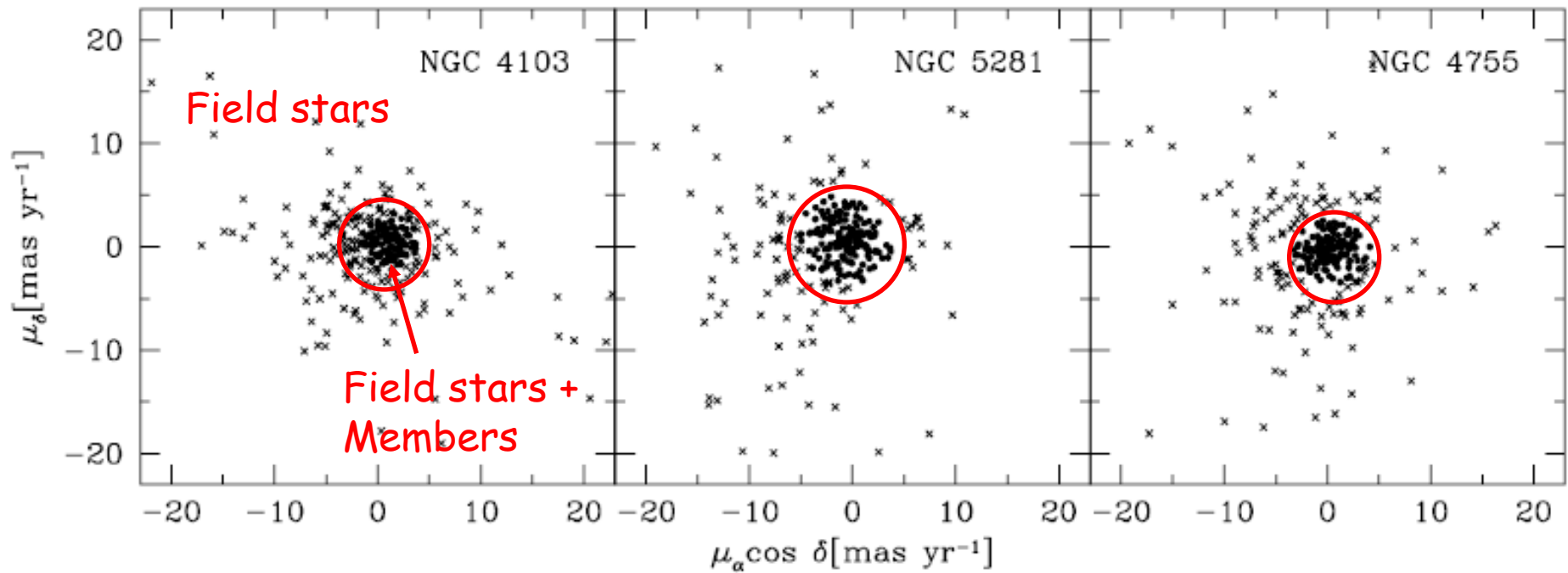
$$\mu_\alpha \cos \delta = -7.3 \pm 4.8 \text{ mas yr}^{-1}$$

$$\mu_\delta = -2.0 \pm 4.3 \text{ mas yr}^{-1}$$

$$\mu_\alpha \cos \delta = -2.9 \pm 3.9 \text{ mas yr}^{-1}$$

$$\mu_\delta = -1.3 \pm 4.3 \text{ mas yr}^{-1}$$

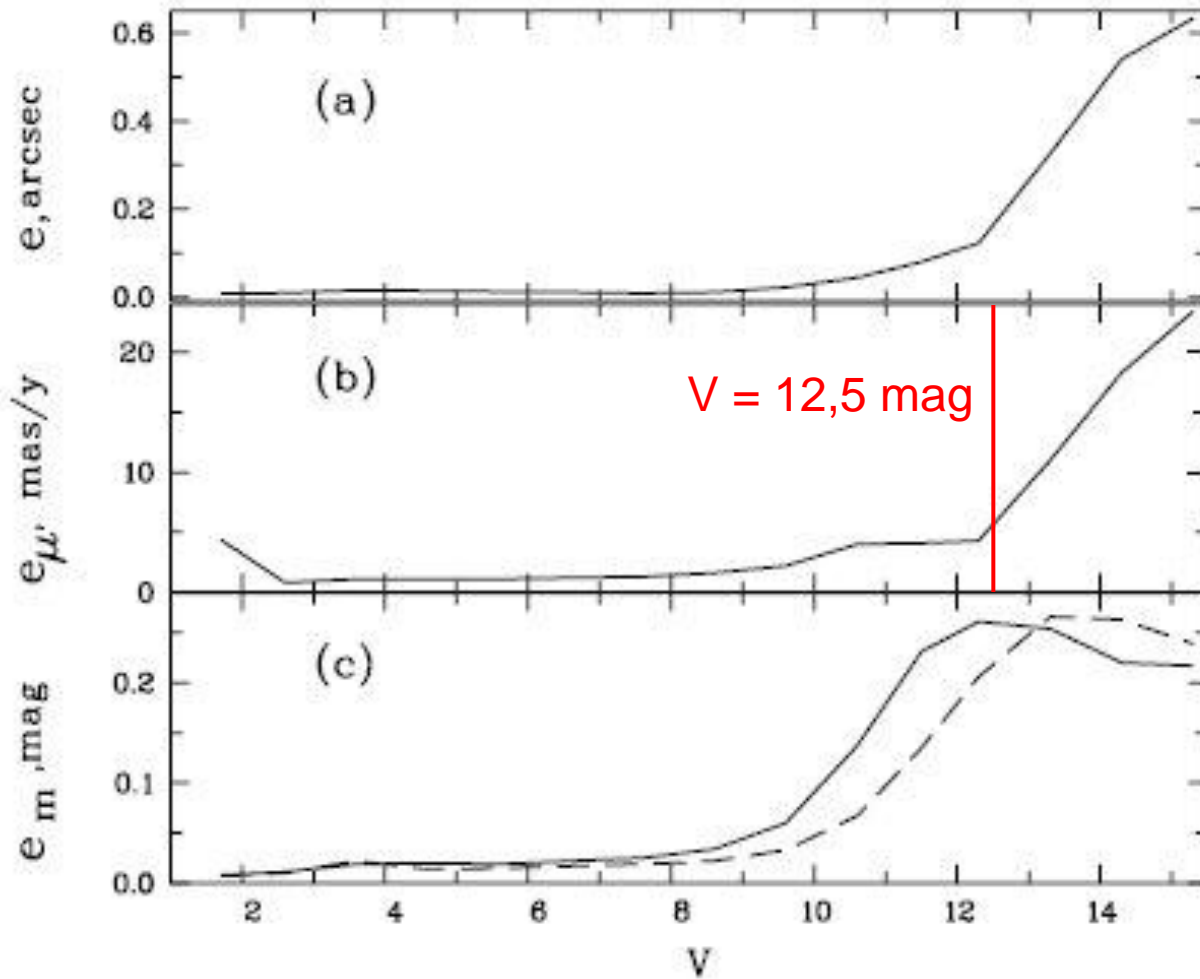
Absolute values after
„Sun correction“



The proper motion for „distant“ star clusters is almost zero.

Only field stars with **large** proper motions can be sorted out.

These are almost only foreground stars.



All-sky Compiled Catalogue
of 2.5 Million Stars:
ASCC-2.5

Includes Johnson BV
photometry, coordinates,
proper motions and
radial velocities

Useable limit at
 $V = 12.5$ mag

1000 pc: $M_V = +2.5$ mag (F0)
2500 pc: $+0.5$ mag (A0)
5000 pc: -1 mag (B5)

Without reddening =>
correlation with age

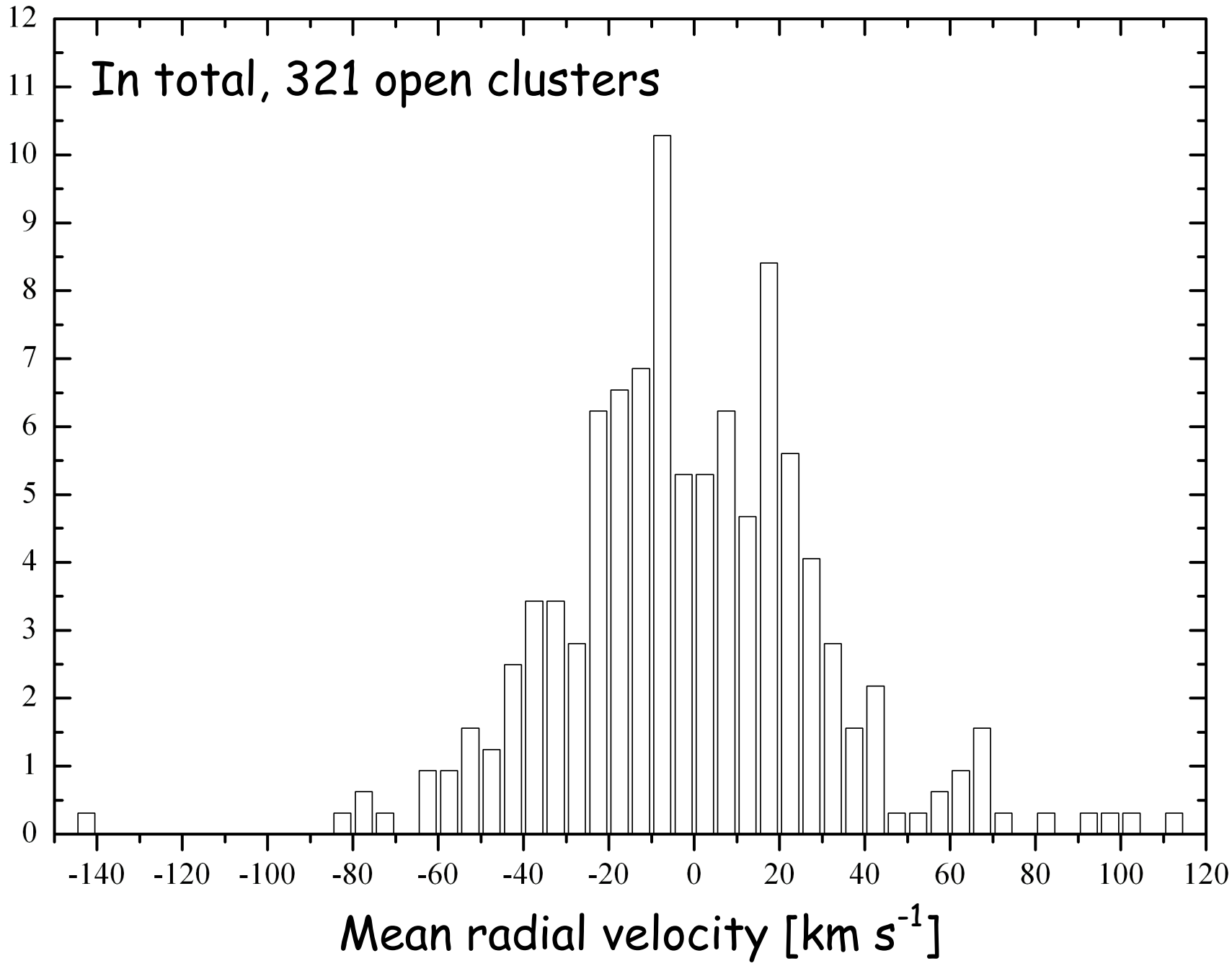
Fig. 1. The mean *rms* errors of equatorial coordinates (a), proper motions (b), stellar magnitudes V - solid line, and B - dashed line (c) in dependence on V magnitude in the ASCC-2.5.

Radial velocities

- **Advantages:**
 1. Correlated with the galactic rotation only
 2. Possible to measure for most distant cluster members
- **Disadvantages:**
 1. High-resolution high S/N spectrum needed
 2. Faintness of members for distant clusters

In total, 321 open clusters

Percentage of all open clusters



Determination of the radial velocity

- Doppler shift of spectral lines

$$\Delta\lambda = \frac{v_R \lambda}{c}$$

- Determine the central wavelength of the shifted line
- Better accuracy if
 1. Instrumental resolution ($\lambda/\Delta\lambda$) is higher
 2. Signal-To-Noise ration (S/N) is higher
 3. $v \sin i$ of star is lower
 4. The number of measured lines is higher

λ [Å]	5	10	30	100	R_V [km s ⁻¹]
3500	0,058	0,117	0,350	1,167	
4000	0,067	0,133	0,400	1,333	
4500	0,075	0,150	0,450	1,500	
5000	0,083	0,167	0,500	1,667	
5500	0,092	0,183	0,550	1,833	
6000	0,100	0,200	0,600	2,000	
6500	0,108	0,217	0,650	2,167	
7000	0,117	0,233	0,700	2,333	
7500	0,125	0,250	0,750	2,500	
8000	0,133	0,267	0,800	2,667	$\Delta\lambda$ [Å]

Instrumental profile defined by the resolution:

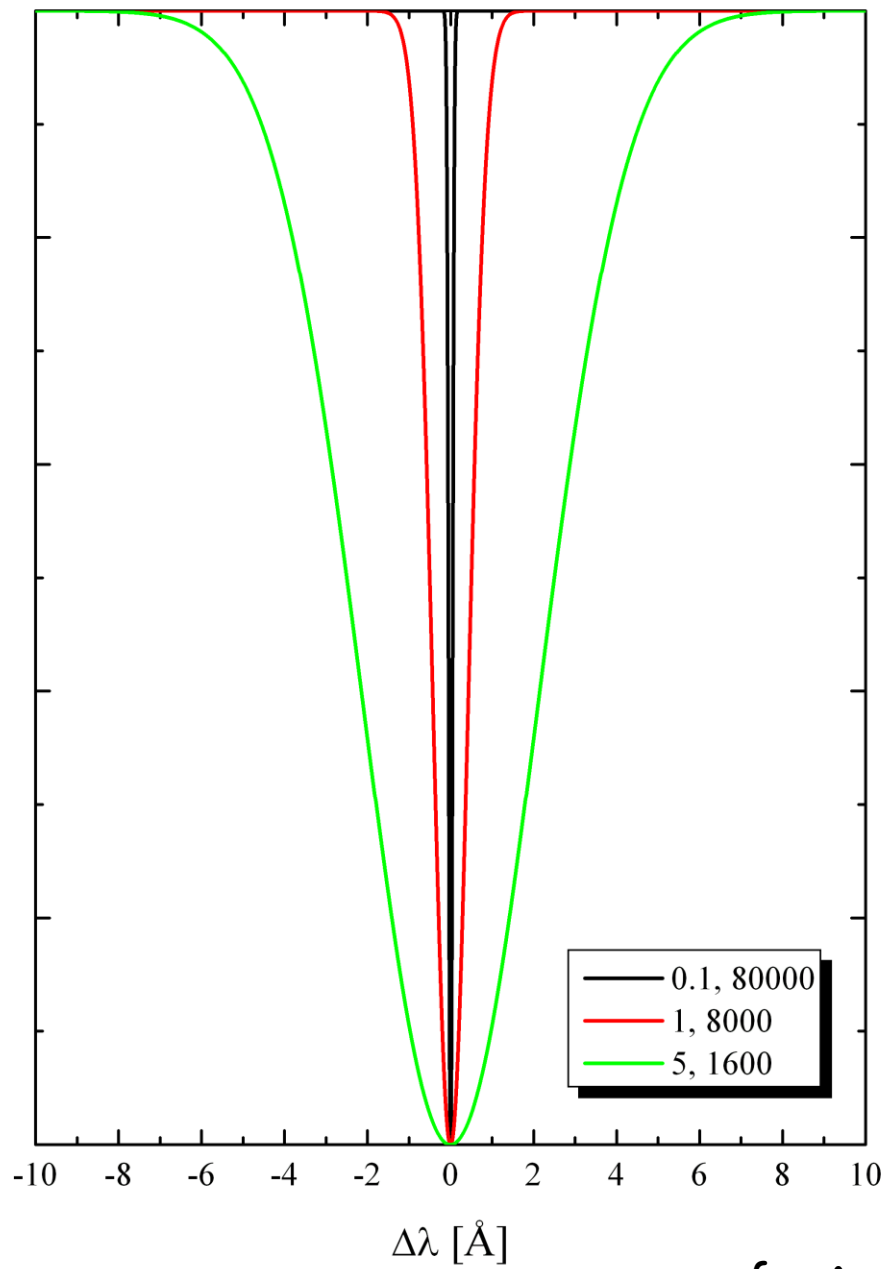
$$IP(\Delta\lambda) = \exp\left[-0.5\left(\frac{(\lambda - \Delta\lambda)}{\sigma}\right)^2\right] \text{ with } \sigma = \frac{FWHM}{2.355}$$

Rotational broadening:

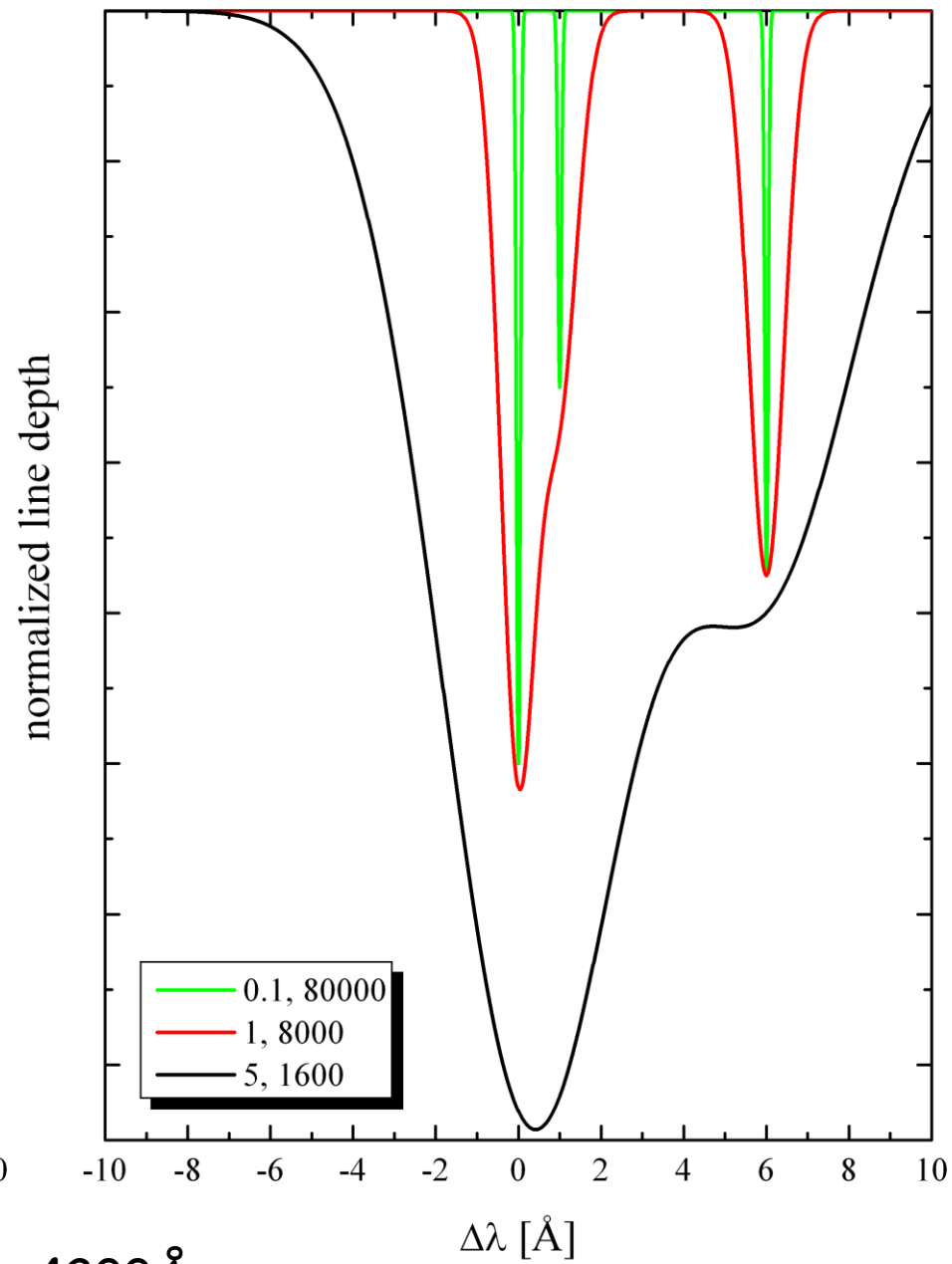
$$RP(\Delta\lambda) = c_1\sqrt{x} + c_2x \text{ with } x = 1 - \left(\frac{\Delta\lambda}{\Delta\lambda_L}\right)^2$$

$$\Delta\lambda_L = \lambda \frac{v \sin i}{c}$$

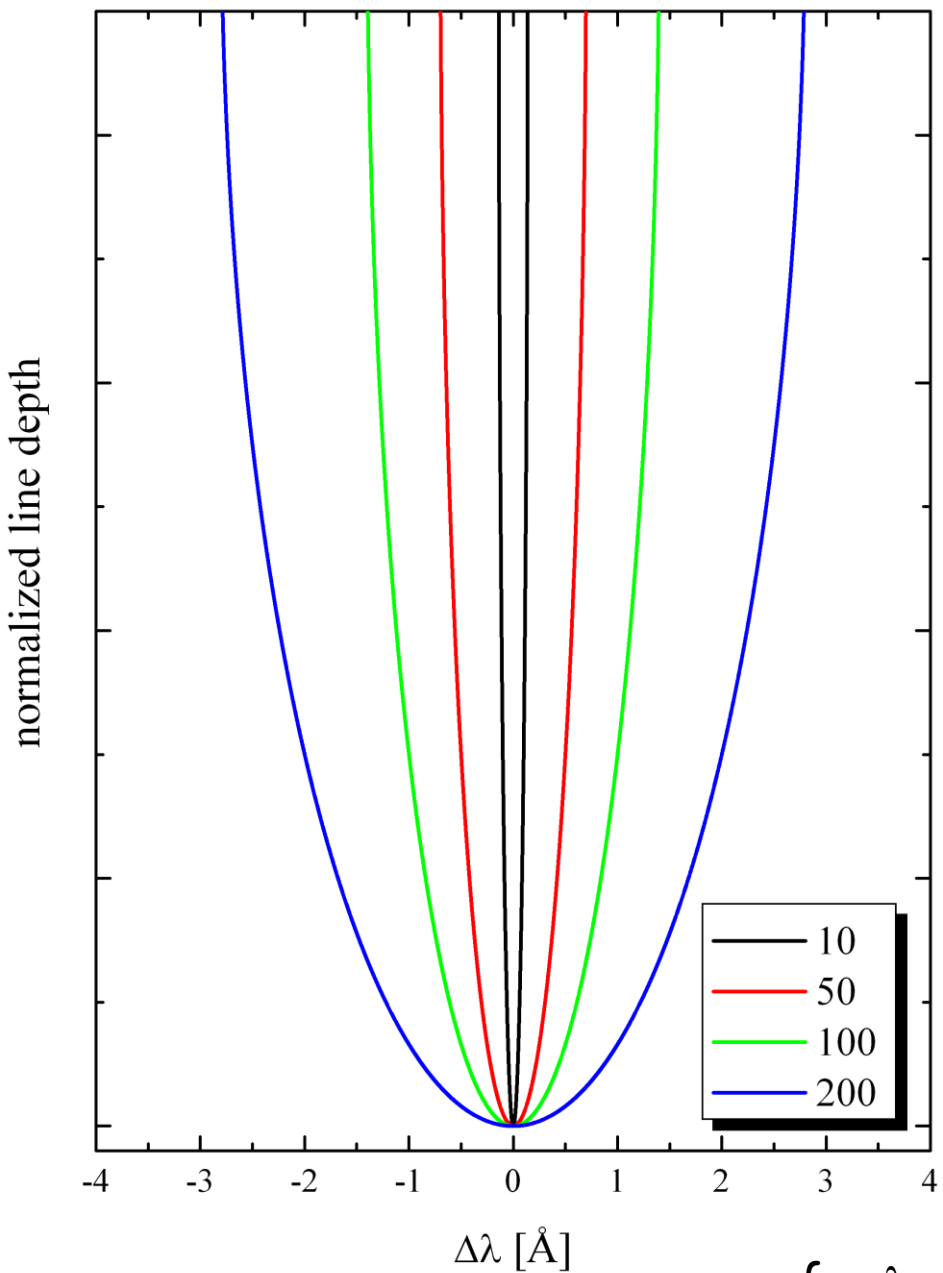
Instrumental profile



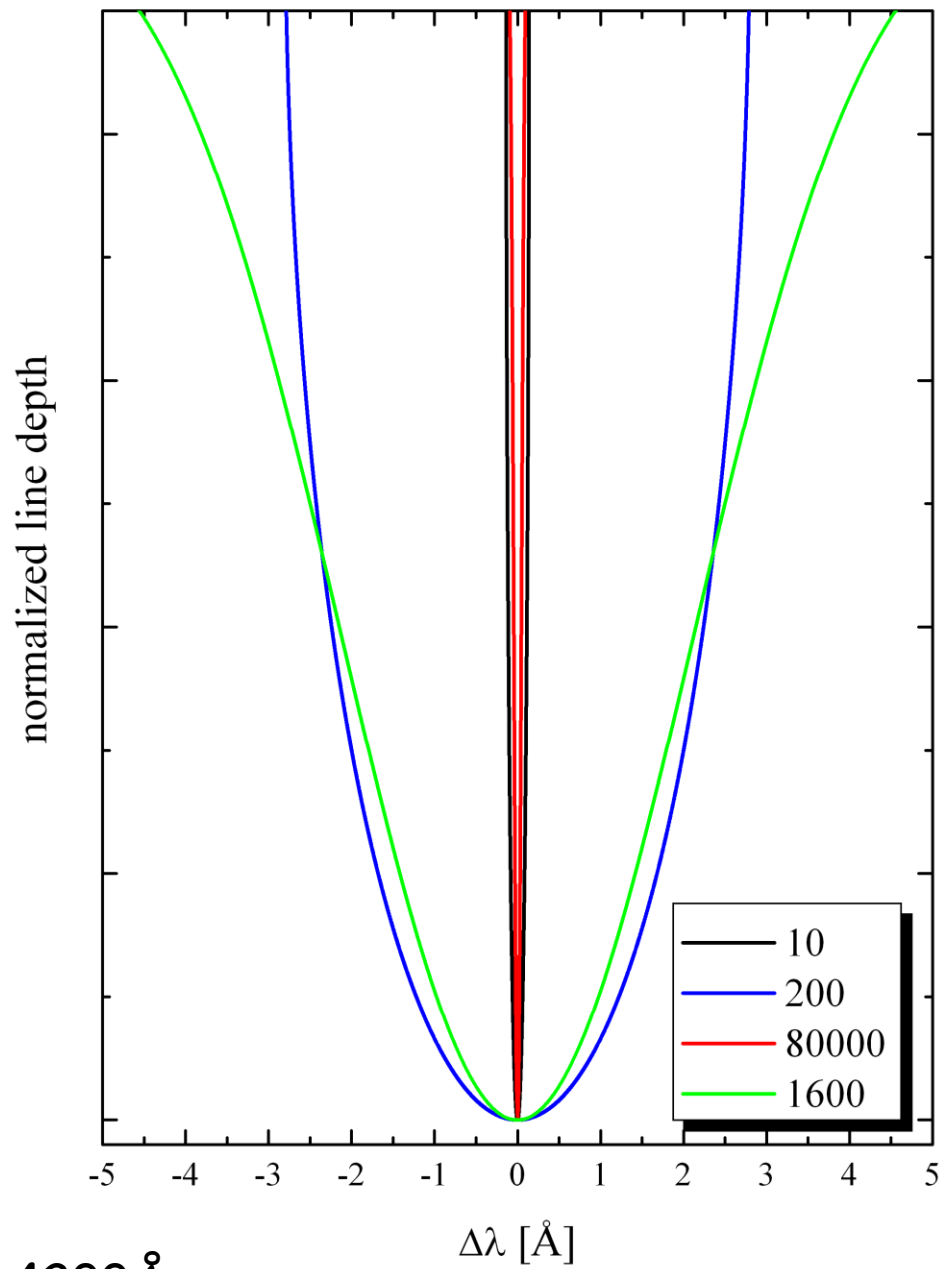
Instrumental profile, resolution of three lines

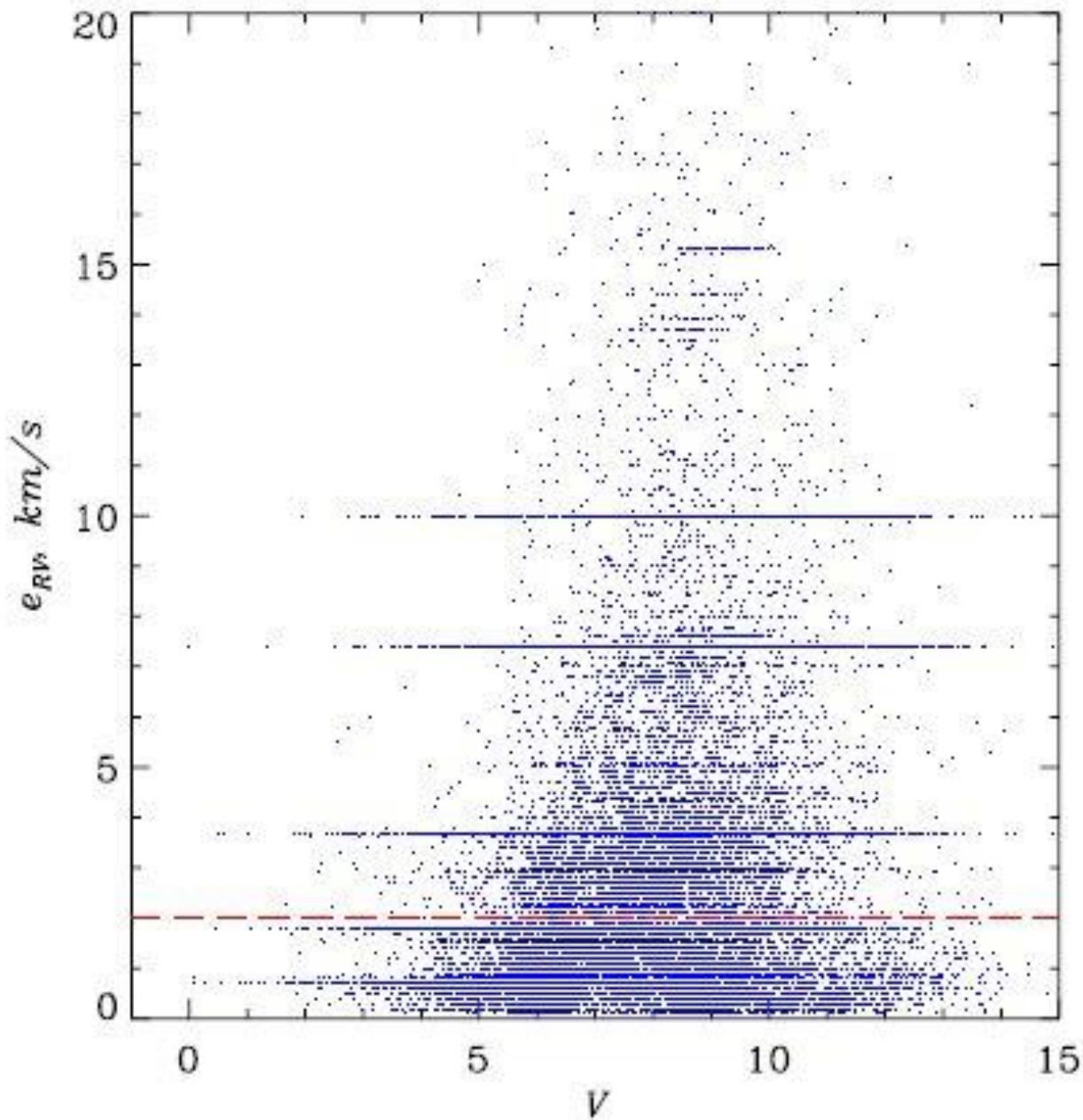
for $\lambda = 4200 \text{\AA}$

Rotational profile



Rotational- and instrumental profile

for $\lambda = 4200\text{\AA}$



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ASCC-2.5

No correlation of the
error with the V
magnitude